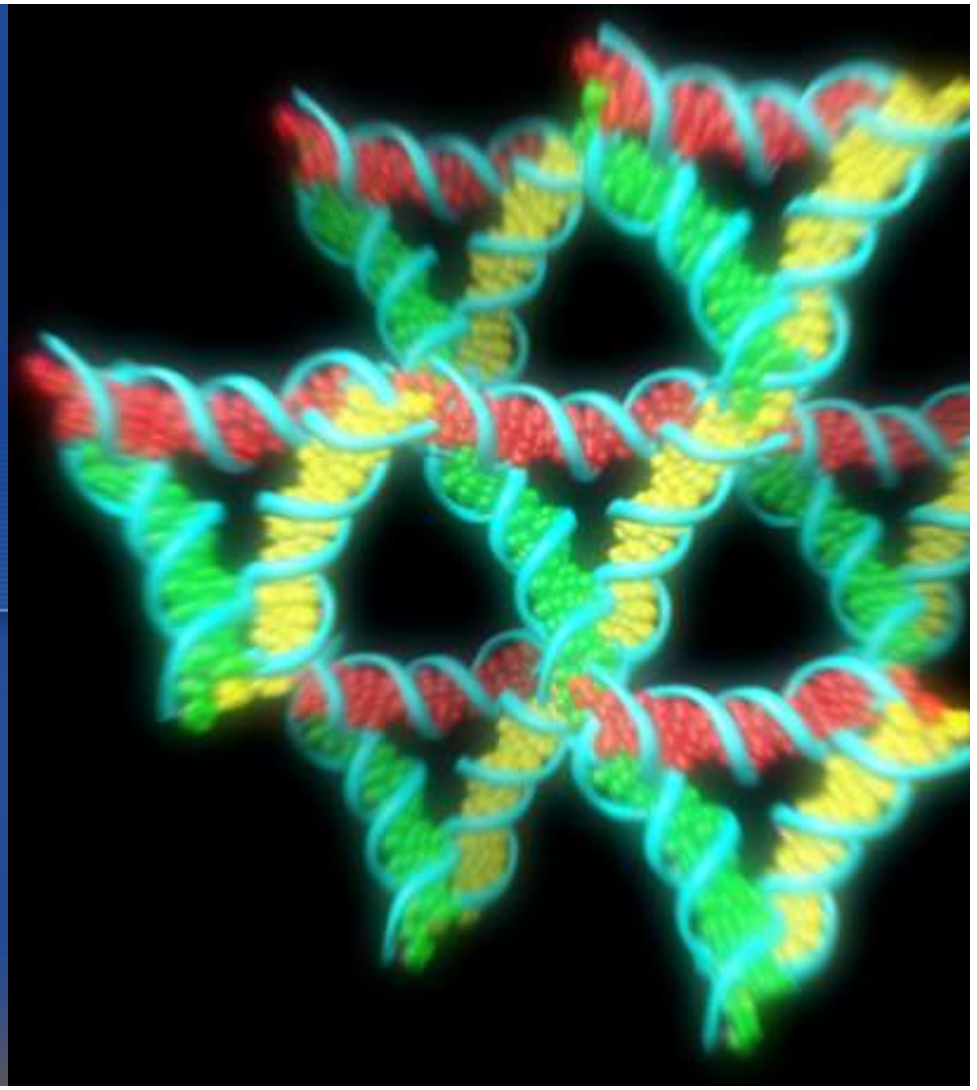
Molecular Programming

Luca Cardelli

University of Oxford

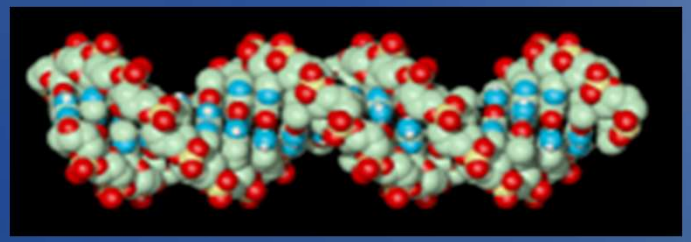
2021-08-30, ACM Summer School on HPC Architectures for AI and Dedicated Applications, Barcelona (virtual)



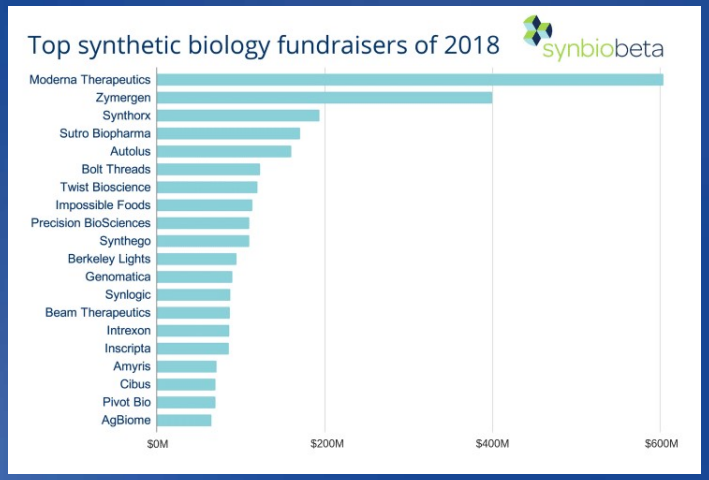
Objectives

- The promises of Molecular Programming:
  - In Science & Medicine
  - In Engineering
  - In Computing

- The current practice of Molecular Programming
  - DNA technology
  - Molecular languages and tools
  - Molecular algorithms



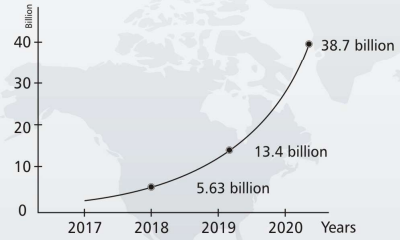
Synthetic Biology Market



SYNTHETIC BIOLOGY TECHNOLOGY INNOVATIONS LANDSCAPE

pintels™ | VajraSoft Inc.

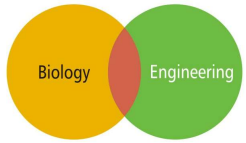
Synthetic Biology Market Size & Growth



Timeline - Years

Synthetic Biology

Intersection of



Key Enabling Technologies

- DNA Synthesis
- Sequencing Technologies
- Genome Engineering
- Microfluidies Technologies
- Bioinformatics technologies
- Biological Components & integrated Systems
- Pathway engineering
- Biofuels Technologies

Synthetic Biology : Core Market Segments

- DNA Synthesis
- Oligonucleotide Synthesis
- Pharmaceuticals
- Chemicals
- Biofuels
- Agriculture
- Synthetic DNA
- Synthetic Genes
- Synthetic Cells
- XNA
- Chassis organisms
- Enabling Products

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Some (ongoing) successes stories

JUNO THERAPEUTICS

- ($4Bn) Reprogram a patient's own blood cells to recognise and destroy specific cancers.
- 90% remission in terminally ill leukemia patients

AMYRIS

- ($300M) Reprogra… …ise chemicals
- Antimalaria… …th Sanofi)
- Jet f… …lights (with Total)

GIN… BIO… THE C… …ISM COMPANY

- Supply custom organisms for bio fabrication

Modern Meadow

- Grow meat, leather ($100Bn market) in the lab
- Proofs of concept already in production

Molecular "hacking"

Hacking Yoghurt

Tuur van Balen - Hacking Yoghurt
- genetically modify your yoghurt in your own kitchen

https://www.youtube.com/watch?v=Co8NOnErrPU

Live Clothing

Scientists Sew Genetically Modified E. Coli into Living Clothing

Harnessing the hygroscopic and biofluorescent behaviors of genetically tractable microbial cells to design biohybrid wearables

Wen Wang[1,2], Lining Yao[2], Chin-Yi Cheng[2,3], Teng Zhang[4], Hiroshi Atsumi[5], Luda Wang[4], Guanyun Wang[2], Oksana Anilionyte…
+ See all authors and affiliations

Molecular Programming

A *technology* (and theory of computation)
based on information-bearing molecules
of historically biological origin (DNA/RNA)
non necessarily involving living matter

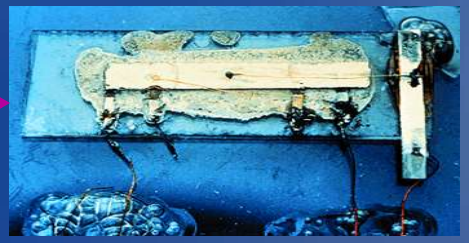
Molecular Programming:
The Hardware Aspect

Smaller and smaller things can be built

Smaller and Smaller

Very few Moore's cycles left!

First working transistor
John Bardeen and Walter Brattain , Dec. 23, 1947



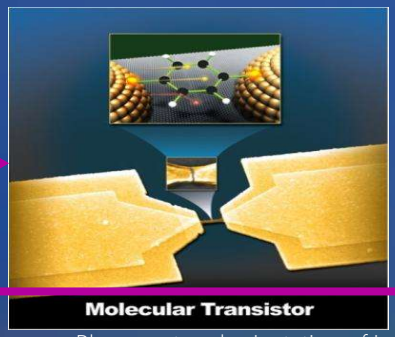
First integrated circuit
Jack Kilby, Sep. 1958.

50+ years later

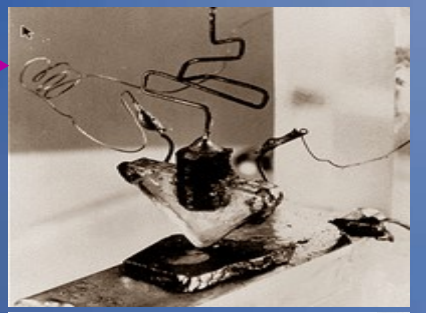
Jan 2010 25nm NAND flash
Intel&Micron. ~50atoms

Jun 2018 7nm (54nm pitch)
TSMC, Intel, Samsung, GlobalFoundries - mass production

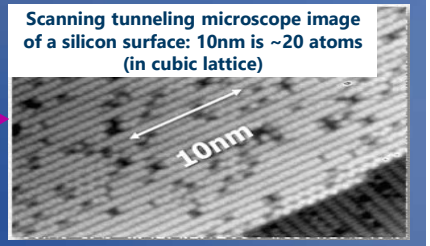
Single molecule transistor
Observation of molecular orbital gating
Nature, 2009; 462 (7276): 1039

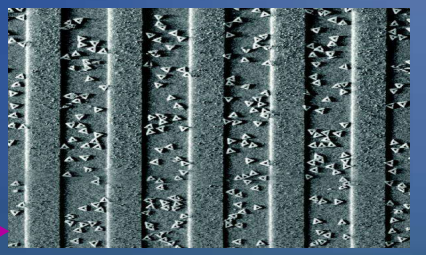


Molecules on a chip



Scanning tunneling microscope image of a silicon surface: 10nm is ~20 atoms (in cubic lattice)





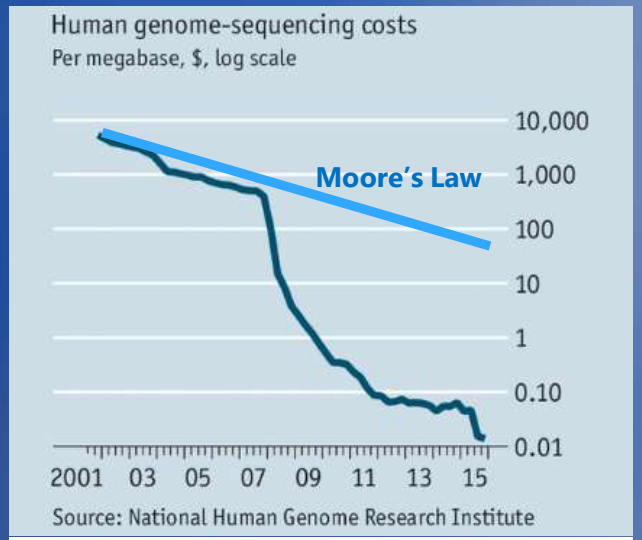
Placement and orientation of individual DNA shapes on lithographically patterned surfaces. Nature Nanotechnology 4, 557 - 561 (2009).

Race to the Bottom

Moore's Law is approaching the single-molecule limit

Carlson's Curve is the new exponential growth curve in technology

In both cases, we are now down to *molecules*



The Pace and Proliferation of Biological Technologies

March 4, 2004 by Rob Carlson

Waiter! There is fly DNA in my soup!

The SmidgION: A portable DNA sequencer that runs on an Iphone

Oxford Nanopore

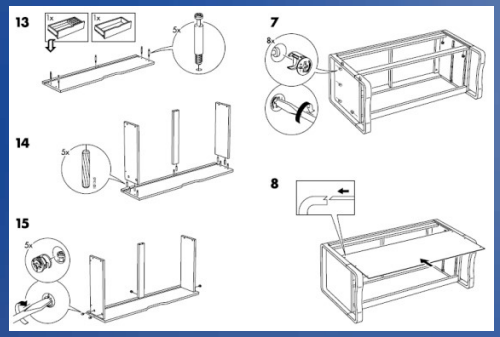
Building the *Smallest* Things

- How do we build structures that are by definition smaller than your tools?
- Basic answer: you can't. Structures (and tools) should build themselves!
- By *programmed self-assembly*

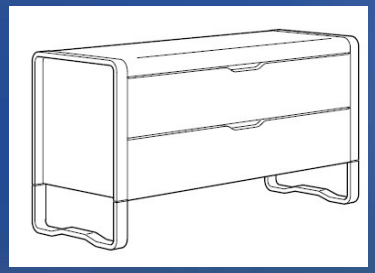
www.youtube.com/watch?v=Ey7Emmddf7Y

Molecular IKEA

- Nature can self-assemble.
  Can we?
- *"Dear IKEA, please send me a chest of drawers that assembles itself."*
- We need a magical material where the pieces are pre-programmed to fit into to each other.
- At the molecular scale many such materials exist…



Add water

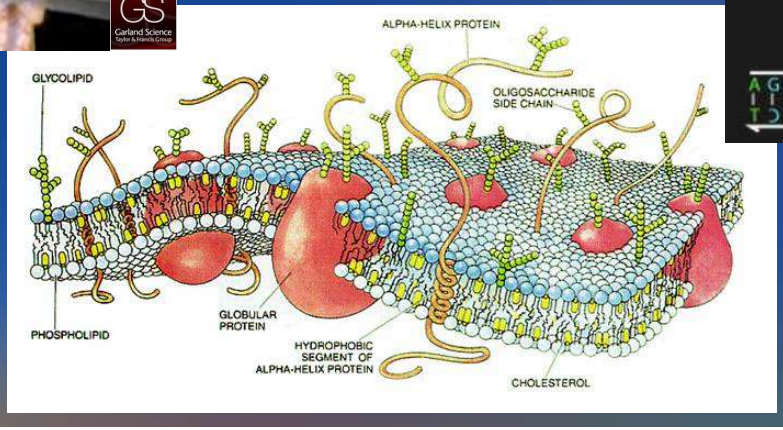


http://www.ikea.com/ms/en_US/customer_service/assembly_instructions.html

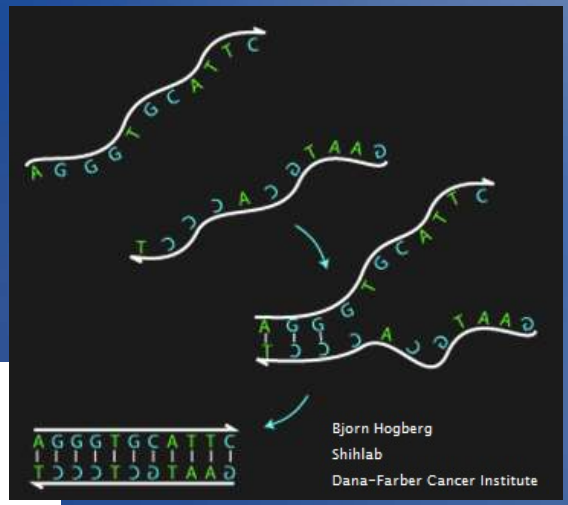
Programmed Self-Assembly

Proteins

Membranes



DNA/RNA

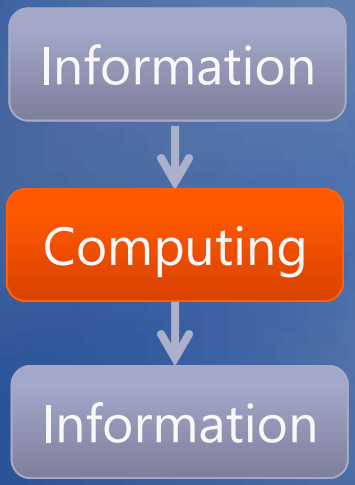


Molecular Programming:
The Software Aspect

Smaller and smaller things can be programmed

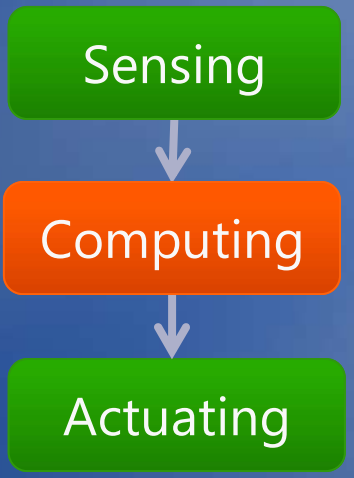
We can program…

- Information
  - Completely!



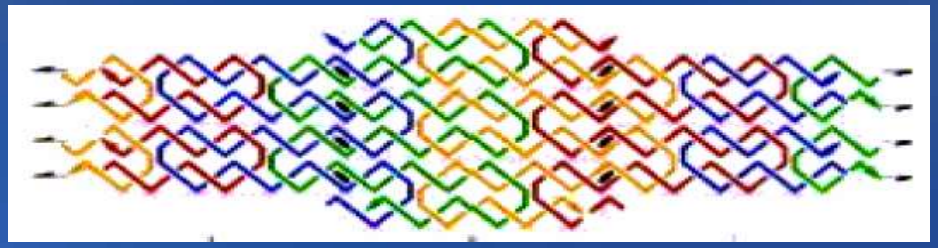
We can program…

- Forces
  - Completely!
    (Modulo sensors/actuators)

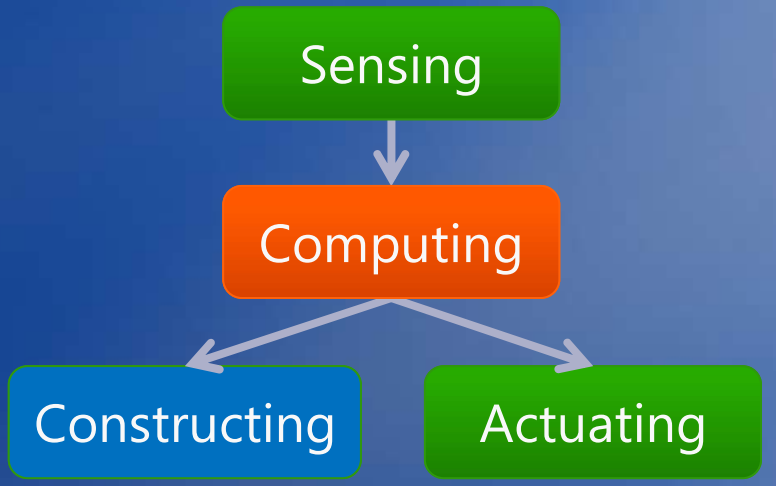


We can program…

- Matter
  - Completely and directly! By self-assembly.
  - Currently: only DNA/RNA.

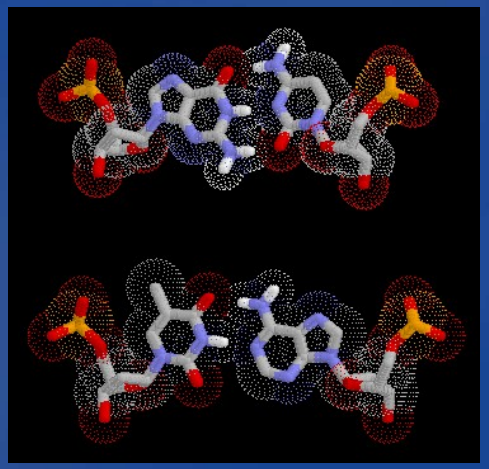


- But DNA is an amazing *material*



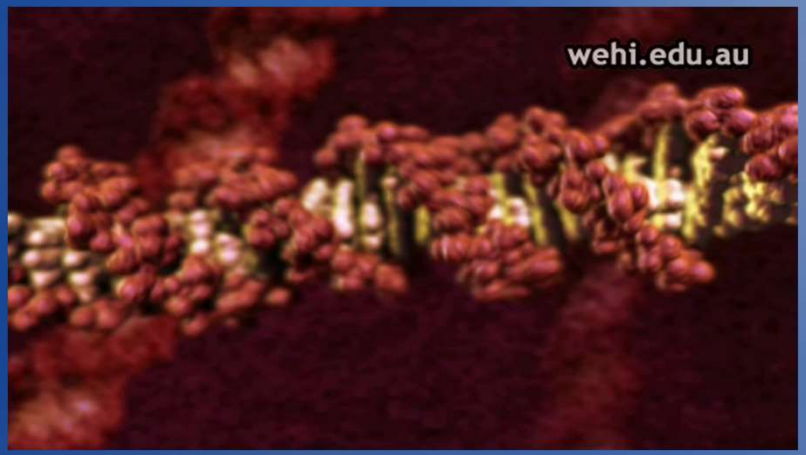
It's like a 3D printer without the printer!
[Andrew Hellington]

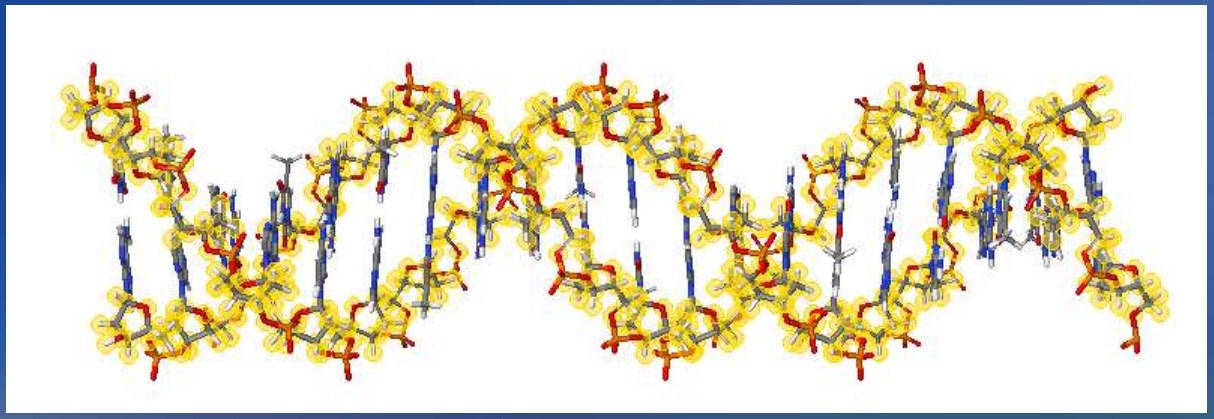
DNA



G-C Base Pair
Guanine-Cytosine

T-A Base Pair
Thymine-Adenine



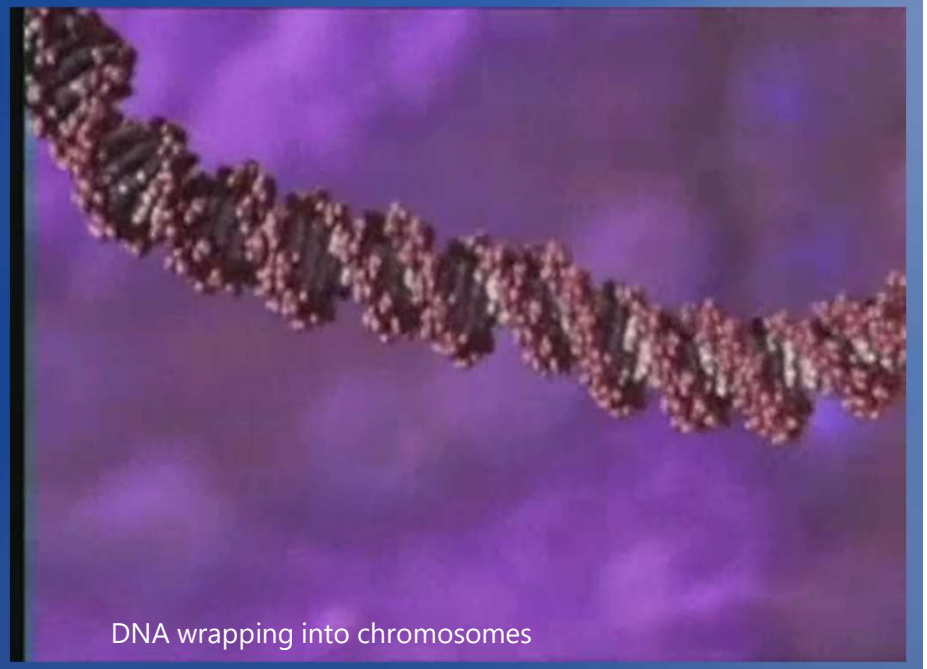


Sequence of Base Pairs (GACT alphabet)

Interactive DNA Tutorial
(http://www.biosciences.bham.ac.uk/labs/minchin/tutorials/dna.html)

DNA Specs

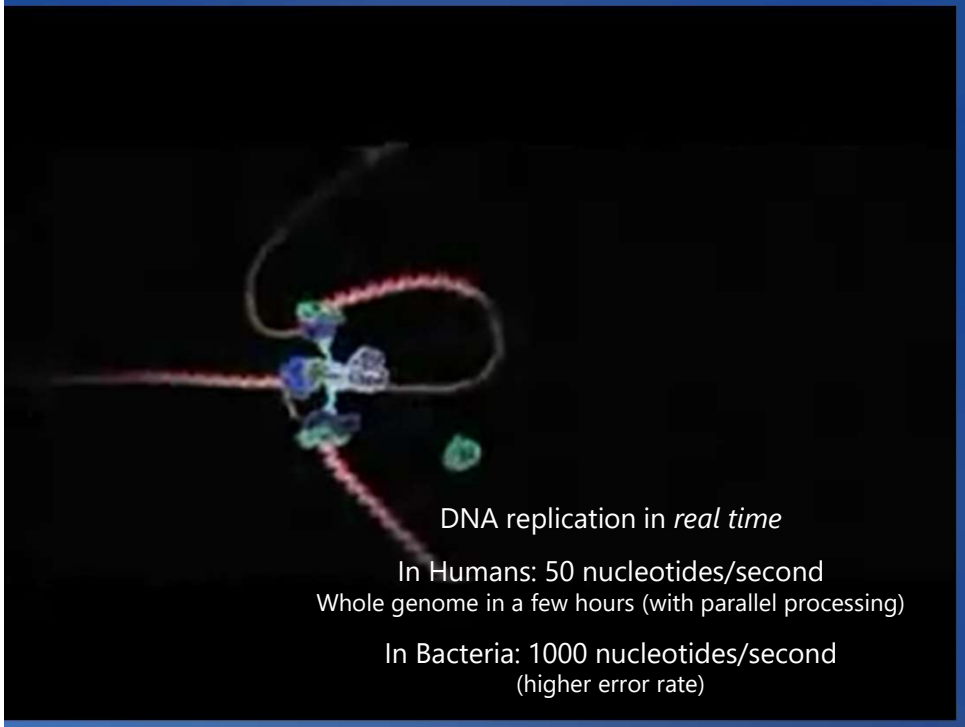
- DNA in each human cell
  - 3 billion base pairs
  - 2nm thick = 4 silicon atoms (in silicon lattice)!
  - 0.34nm per basepair = 2 bits in 2/3 silicon atom!
  - 2 meters long
    copied in parallel at each cell division!
  - 750 megabytes
    80% functional, but only 1.5% protein coding
  - folded into a 6μm spherical nucleus
    = 140 exabytes (million terabytes)/mm^3
    => *all* the data on the internet fits in a shoebox!
- DNA in each human body
  - 10 trillion cells
  - 133 Astronomical Units long
  - 7.5 octabytes (replicated)
- DNA in human population
  - 20 million light years long



DNA wrapping into chromosomes

Andromeda Galaxy
2.5 million light years away

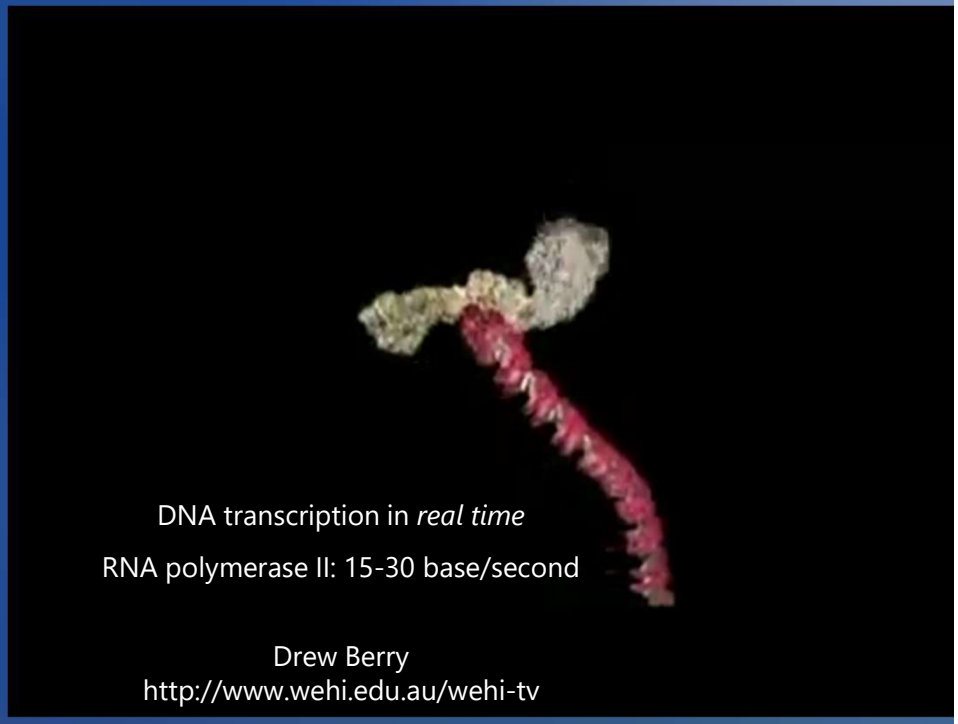
DNA Benchmarks



DNA replication in *real time*

In Humans: 50 nucleotides/second
Whole genome in a few hours (with parallel processing)

In Bacteria: 1000 nucleotides/second
(higher error rate)



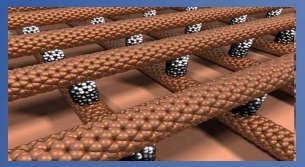
DNA transcription in *real time*

RNA polymerase II: 15-30 base/second

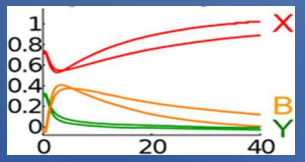
Drew Berry
http://www.wehi.edu.au/wehi-tv

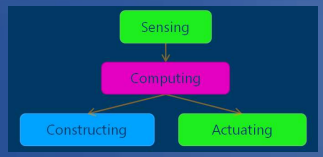
One molecule to rule them all

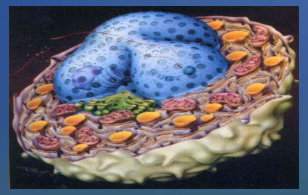
- There are many, many nanofabrication techniques and materials



- But only DNA (and RNA) can:
  - Organize ANY other matter [caveats apply]
  - Execute ANY kinetics [caveats: up to time scaling]
  - Assemble Nano-Control Devices
  - Interface to Biology



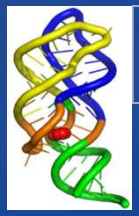




H.Lodish & al. Molecular Cell Biology 4th ed.

Building Nano-Control Devices

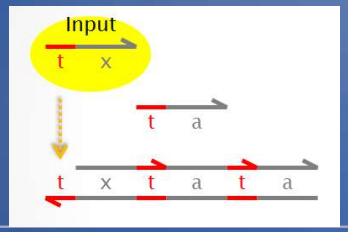
All the components of nanocontrollers can already be built entirely and solely with DNA, and interfaced to the environment



DNA Aptamers

Sensing

Computing

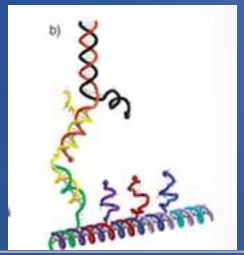


DNA Logical Gates

Constructing

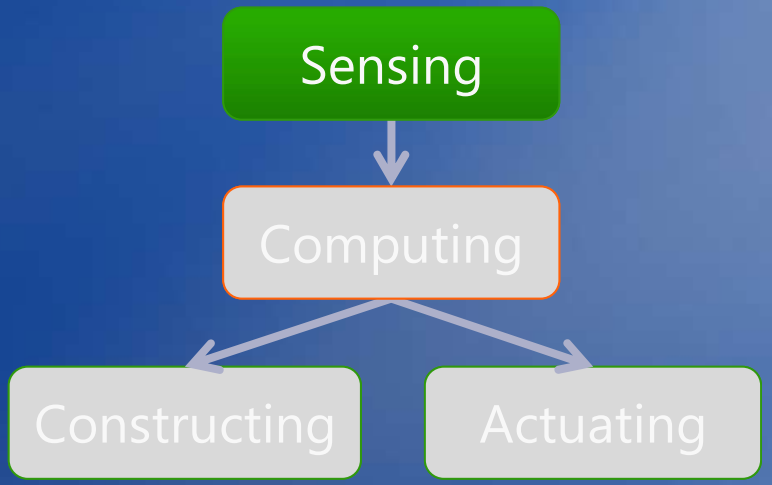
Actuating

Self-assembling DNA Tiles



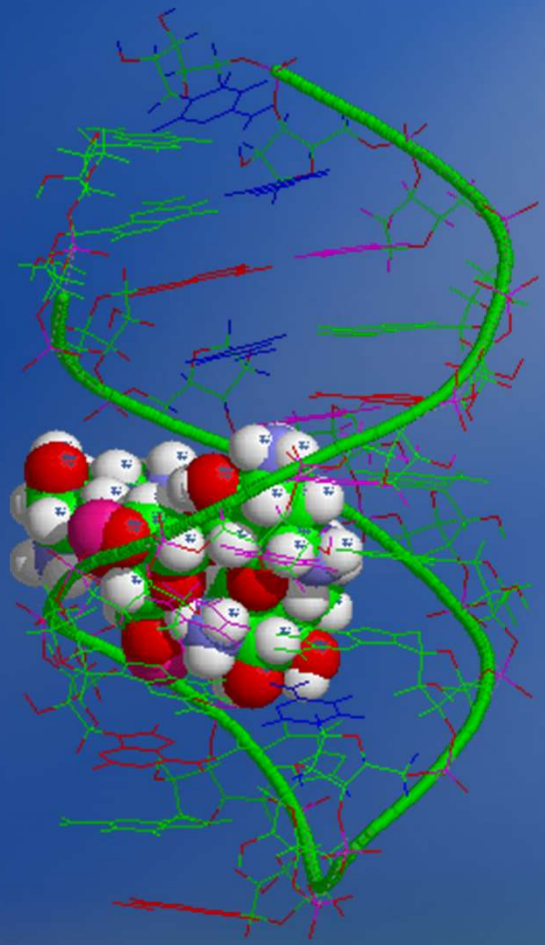
DNA Walkers & Cages

Sensing



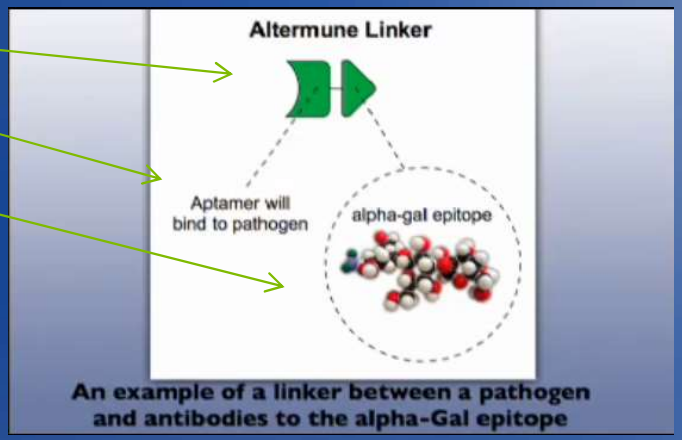
Aptamers

Artificially evolved DNA molecules that stick to (almost) anything you like highly selectively

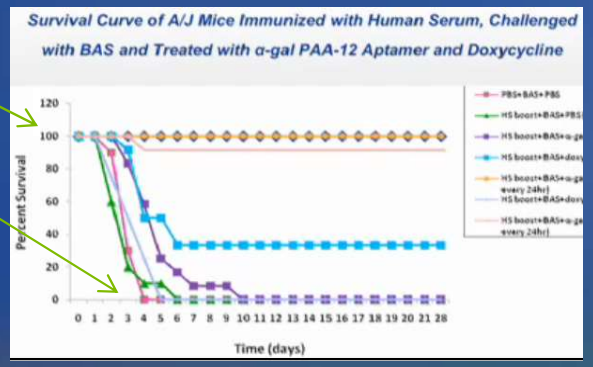


Pathogen Spotlights

- DNA aptamer binds to:
  - A) a pathogen
  - B) a molecule our immune system (when allergic) hates and immediately removes (eats) along with anything attached to it!

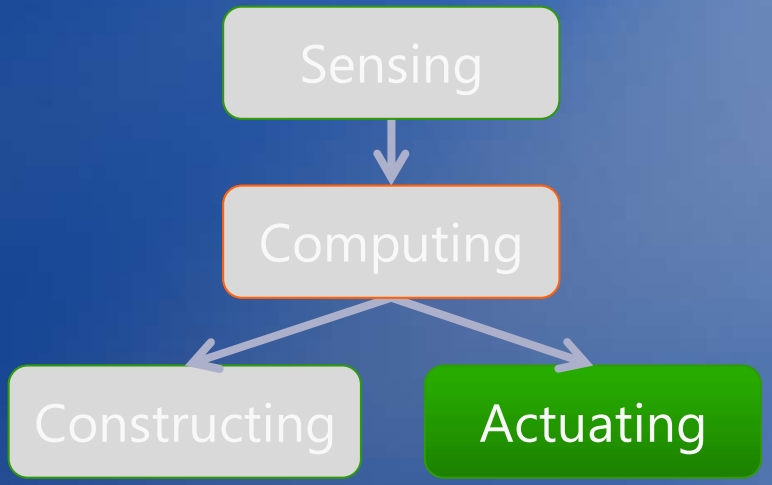


- Result: instant immunity
  - Mice poisoned with Anthrax plus aptamer (100% survival)
  - Mice poinsoned with Anthrax (not so good)



Kary Mullis (incidentally, also Nobel prize for inventing the Polymerase Chain Reaction)

Actuating



DNA Walkers

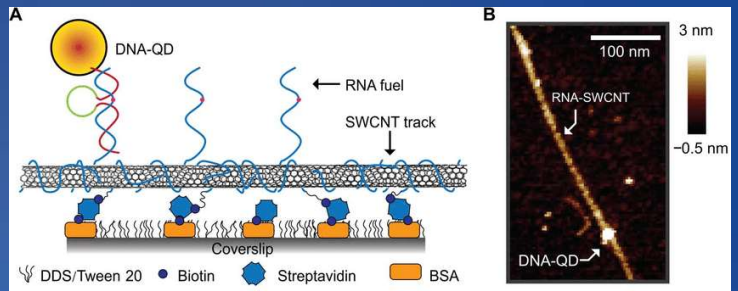
J|A|C|S
COMMUNICATIONS

Published on Web 08/17/2004

A Synthetic DNA Walker for Molecular Transport

Jong-Shik Shin† and Niles A. Pierce*,†,‡

Departments of Bioengineering and Applied & Computational Mathematics, California Institute of Technology, Pasadena, California 91125



Visible/near-infrared subdiffraction imaging reveals the stochastic nature of DNA walkers

January 2017 · Science Advances 3(1):e1601600

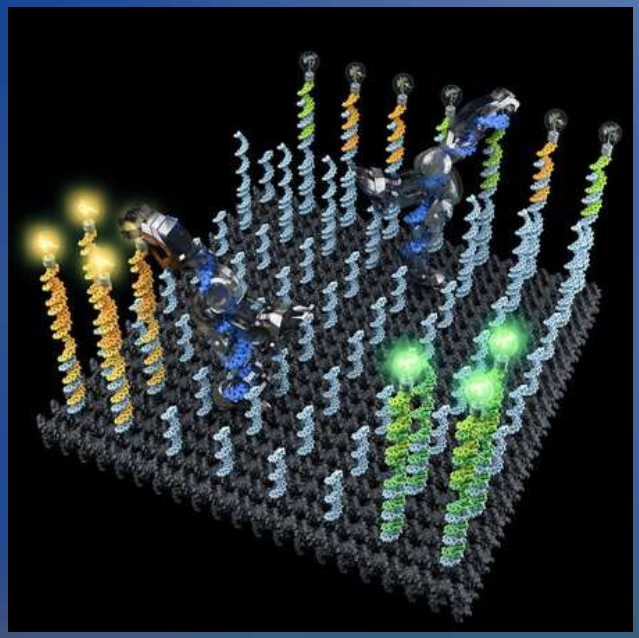
DOI: 10.1126/sciadv.1601600

Jing Pan · Tae-Gon Cha · Feiran Li · Show all 6 authors · Jong Hyun Choi

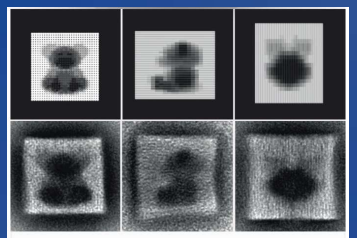
DNA Robotics

A cargo-sorting DNA robot

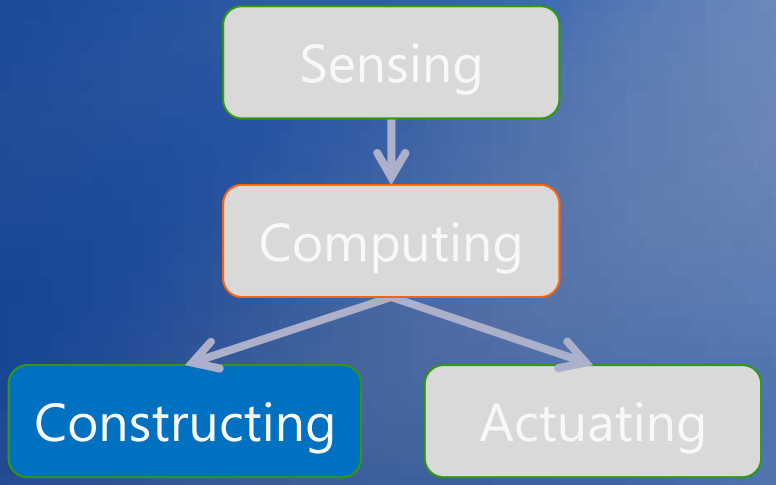
Thubagere, Anupama J. and Li, Wei and Johnson, Robert F. and Chen, Zibo and Doroudi, Shayan and Lee, Yae Lim and Izatt, Gregory and Wittman, Sarah and Srinivas, Niranjan and Woods, Damien and Winfree, Erik and Qian, Lulu (2017) *A cargo-sorting DNA robot.* Science, 357 (6356). Art. No. eaan6558. ISSN 0036-8075.



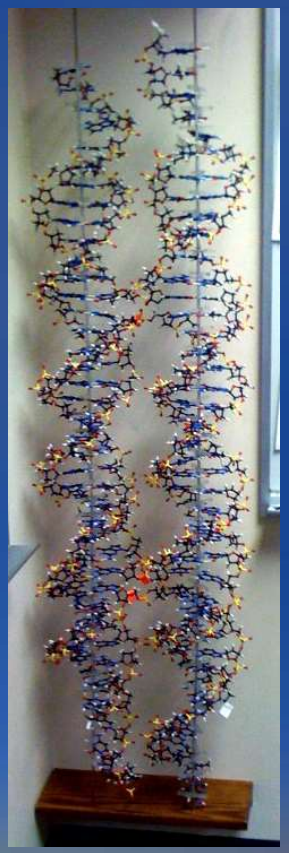
Constructing

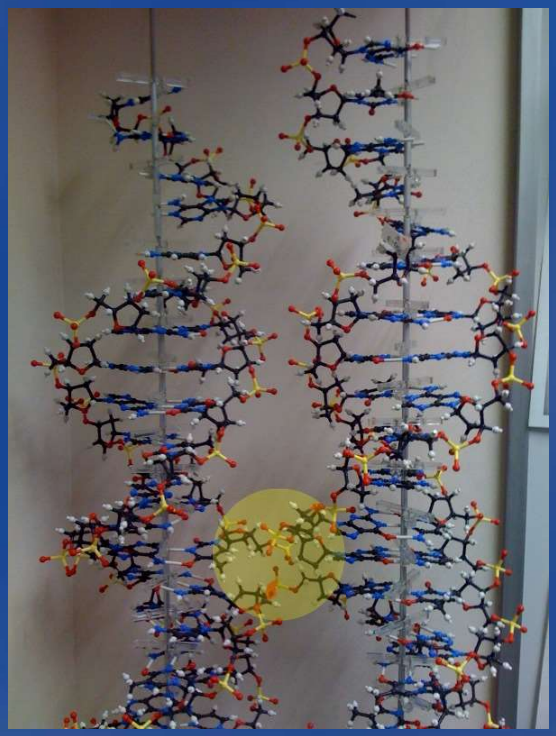


The 3D model of the computer-designed bear shape shown on top was fabricated into the nanostructures visualized with transmission electron microscopy (below). Credit: Wyss Institute at Harvard University



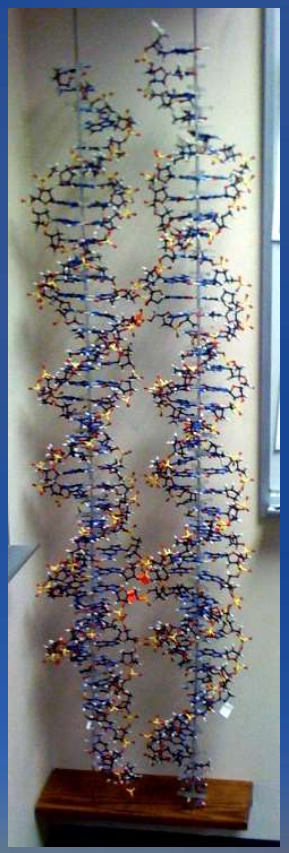
Crosslinking

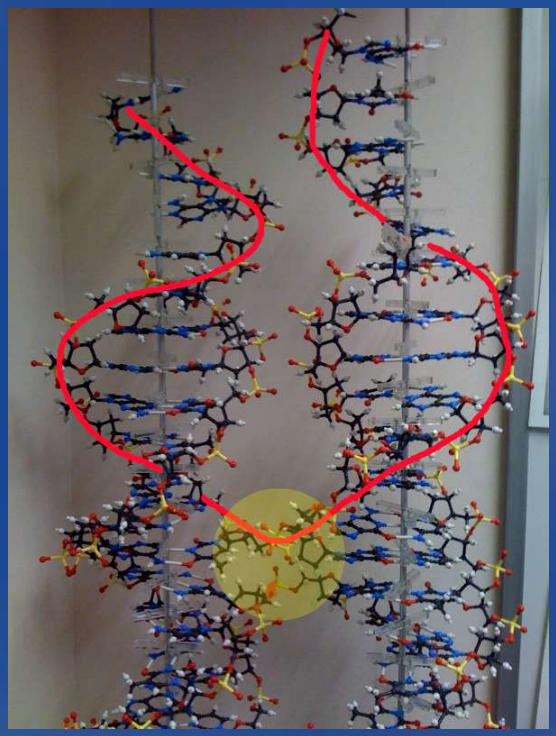




the dawn of structural DNA nanotechnology

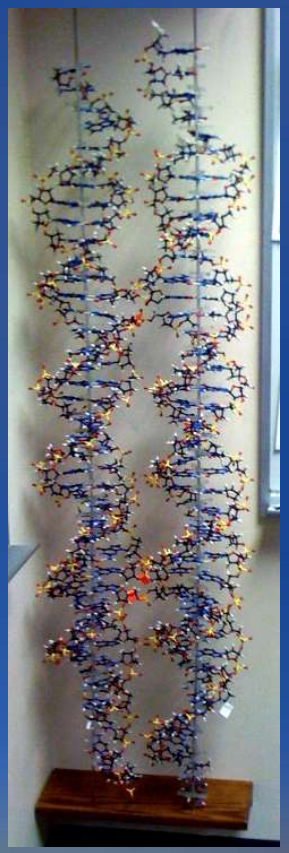
Crosslinking

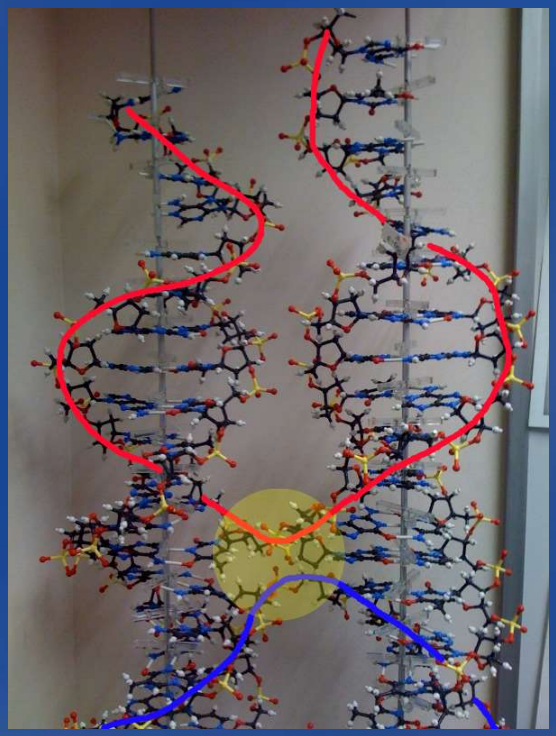




the dawn of structural DNA nanotechnology

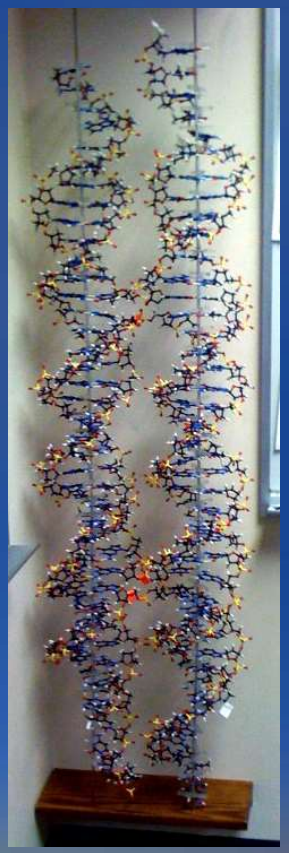
Crosslinking

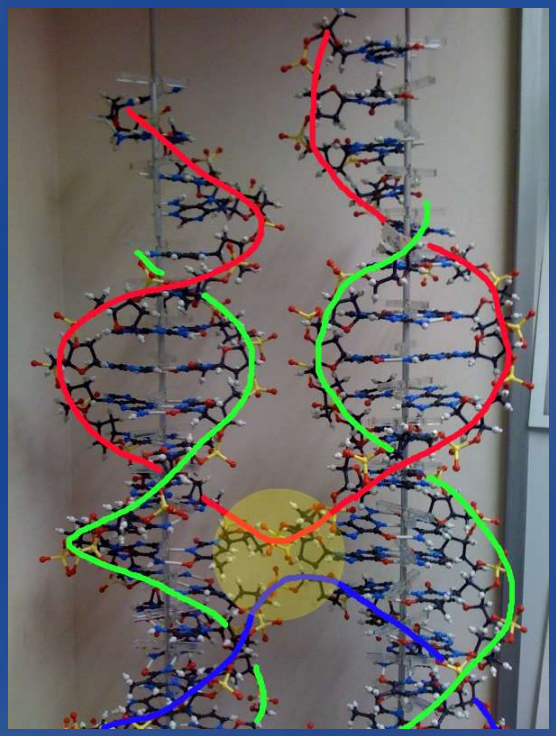




the dawn of structural DNA nanotechnology

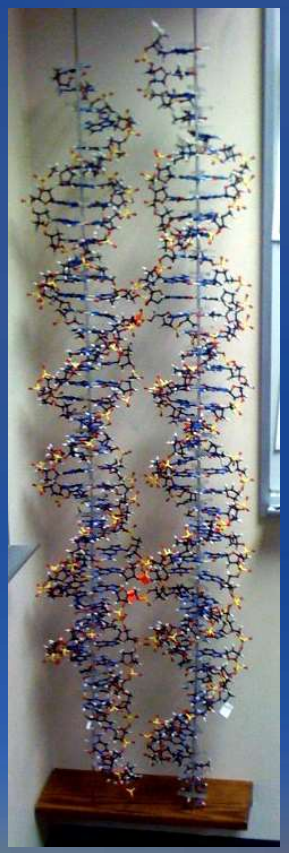
Crosslinking

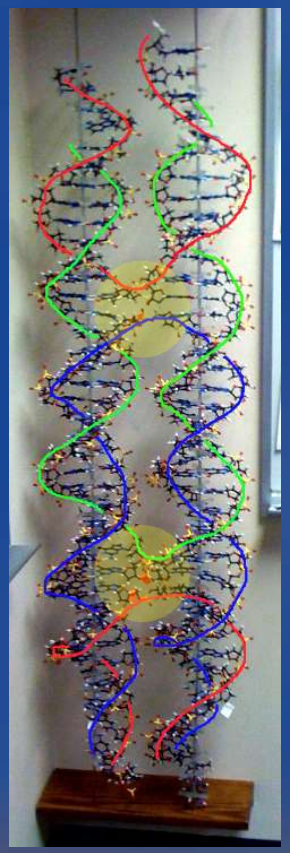




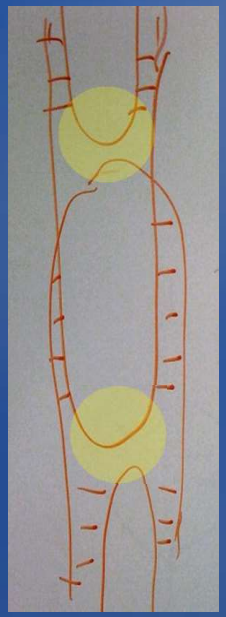
the dawn of structural DNA nanotechnology

Crosslinking



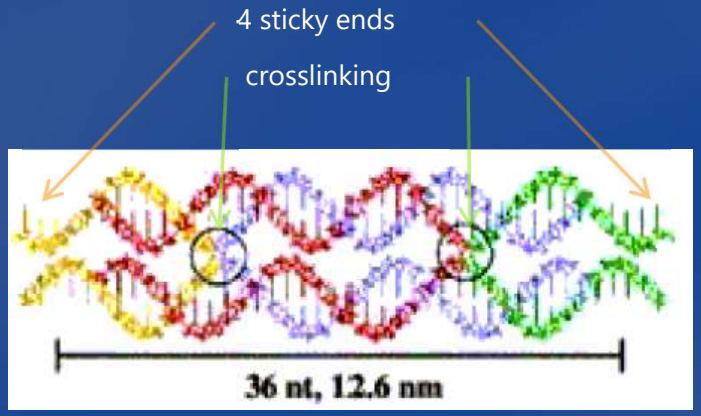


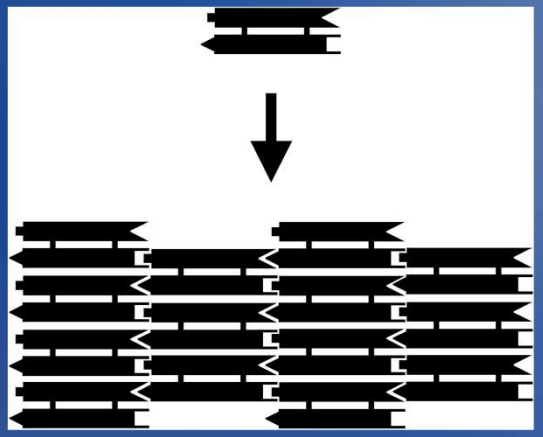
In nature, crosslinking is deadly (blocks DNA replication).

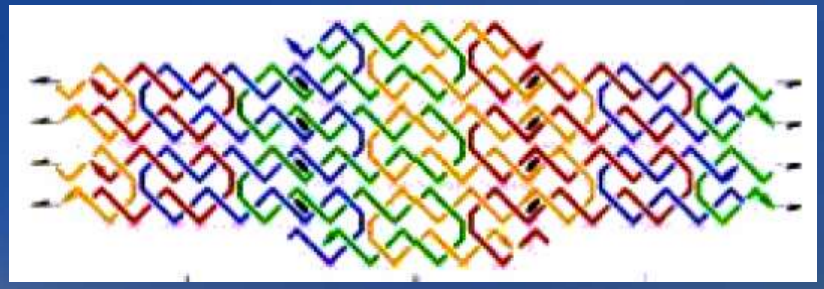


In engineering, crosslinking is the key to using DNA as a construction material.

DNA Tiling



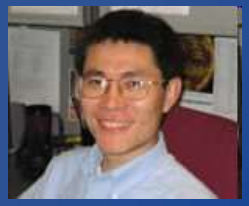




Construction and manipulation of DNA tiles in free space

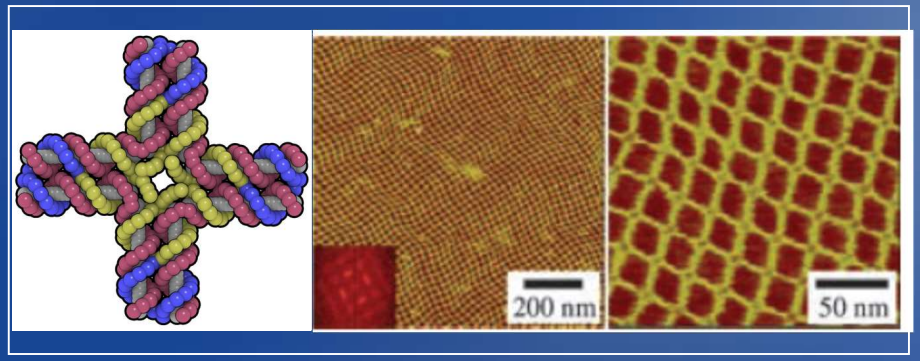
Pankhudi

2D DNA Lattices

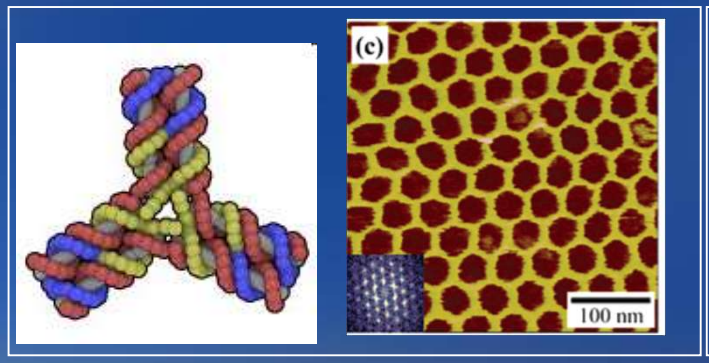


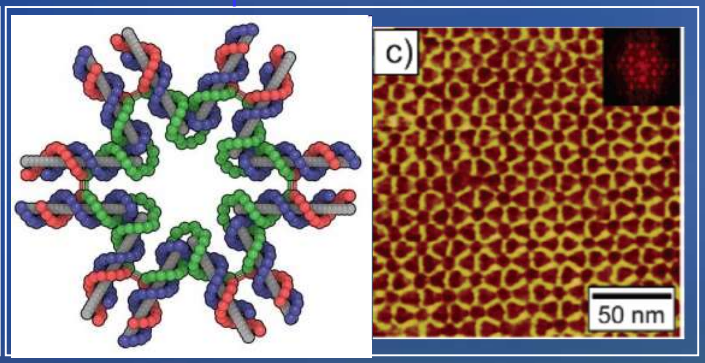
Chengde Mao

Purdue University, USA



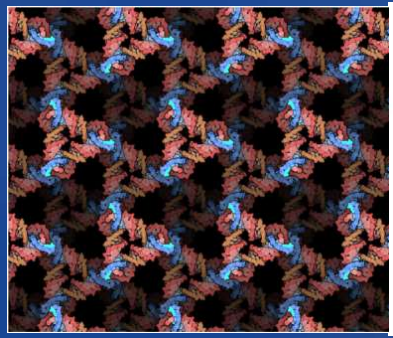
N-point Stars



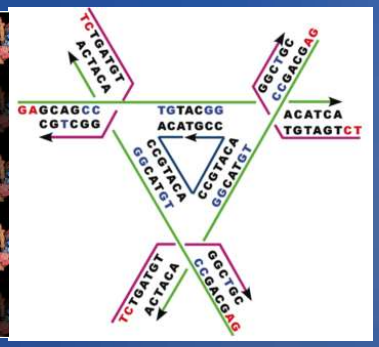


3D DNA Structures

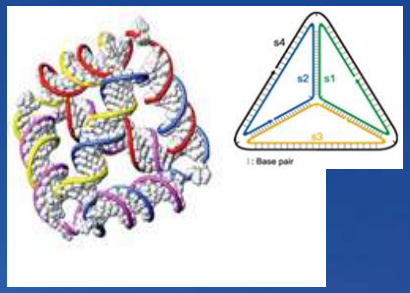
Ned Seeman
NYU



3D Cyrstal

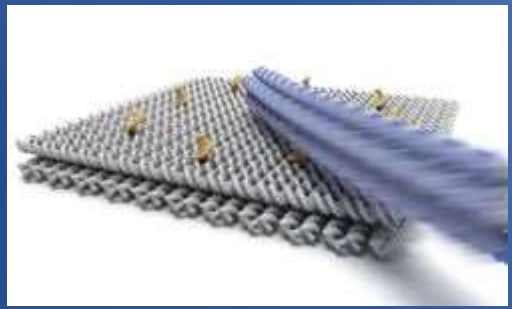


Andrew Tuberfield
Oxford



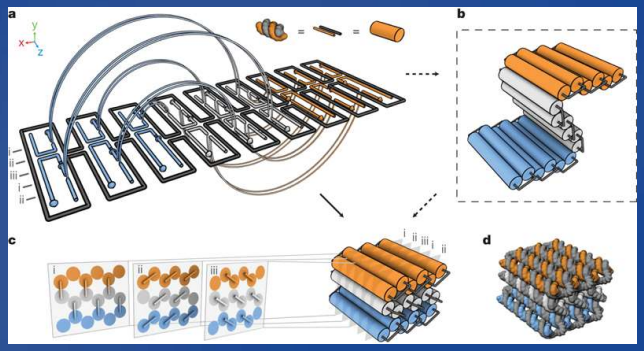
Tetrahedron

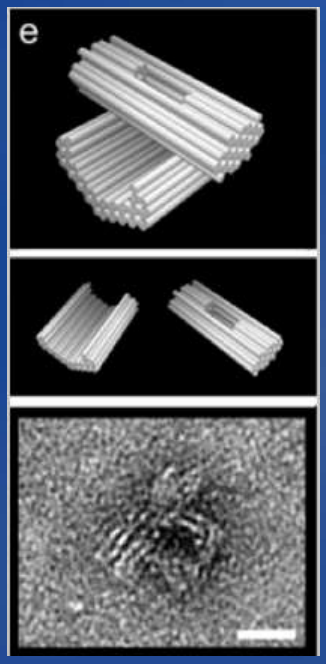
Friedrich Simmel
Munich

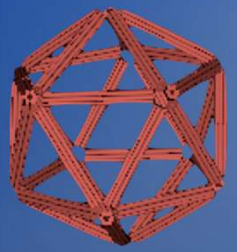


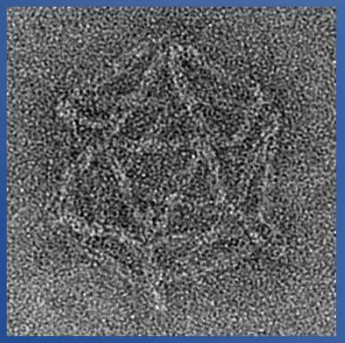
Robotic Arm

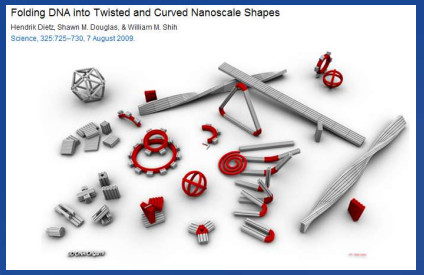
CADnano











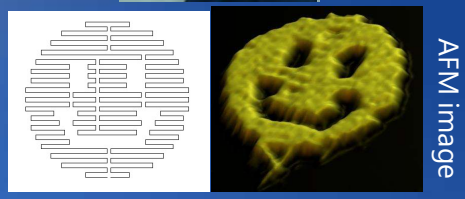
William Shih
Harvard

https://www.youtube.com/watch?v=Ek-FDPymyyg

S.M. Douglas, H. Dietz, T. Liedl, B. Högberg, F. Graf and W. M. Shih
Self-assembly of DNA into nanoscale three-dimensional shapes, Nature (2009)

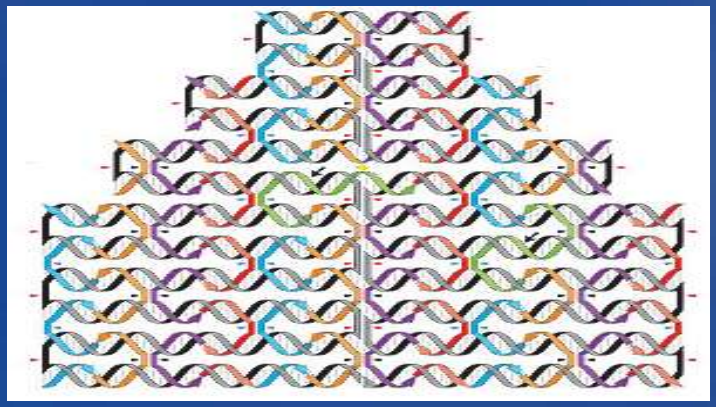
DNA Origami

Folding a long (6407bp) naturally occurring circular ssDNA (from bacteriophage M13) via lots of short 'staple' strands that constrain its shape

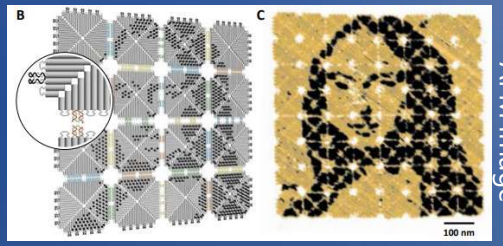


AFM image

Paul Rothemund's
"Disc with three holes" (2006)
Nature 440, 297, 2006



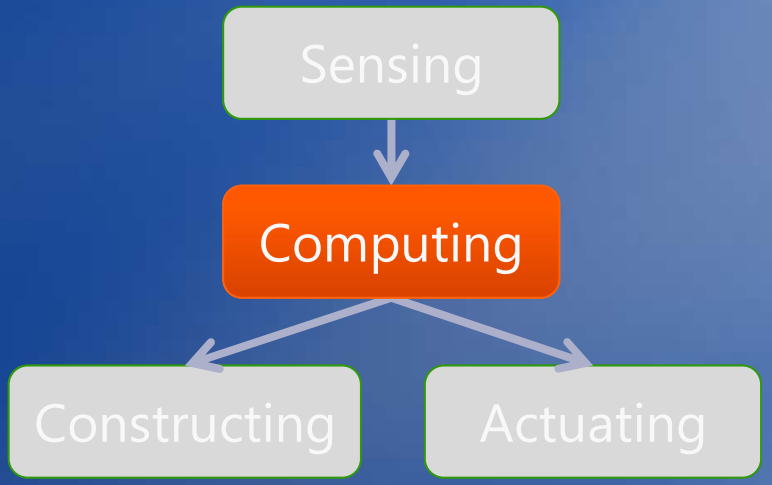
Black/gray: 1 long viral strand (natural DNA)
Color: many short staple strands (synthetic DNA)



AFM image

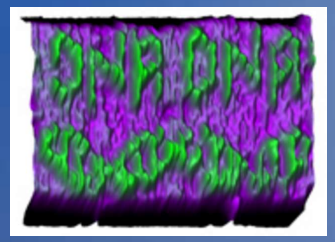
Lulu Qian's
Hierarchical assembly (2017)
Nature, 552(7683):67–71, 2017

Computing



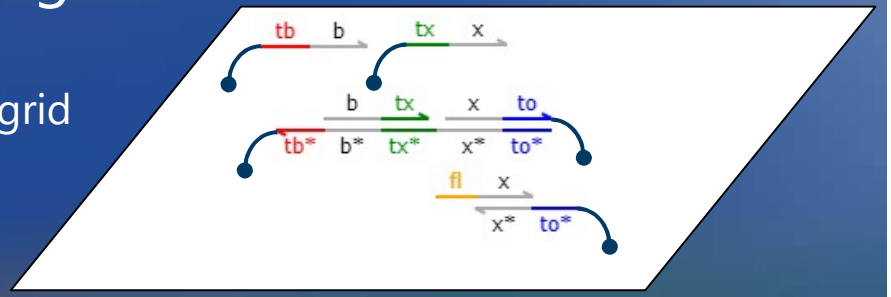
DNA Circuit Boards

- DNA origami are arrays of uniquely-addressable locations
  - Each staple is different and binds to a unique location on the origami
  - It can be extended with a unique sequence so that something else will attach uniquely to it.



Some staples are attached to "green blobs" (as part of their synthesis) Other staples aren't

- More generally, we can bind "DNA gates" to specific locations
  - And so connect them into "DNA circuits" on a grid
  - Only neighboring gates will interact

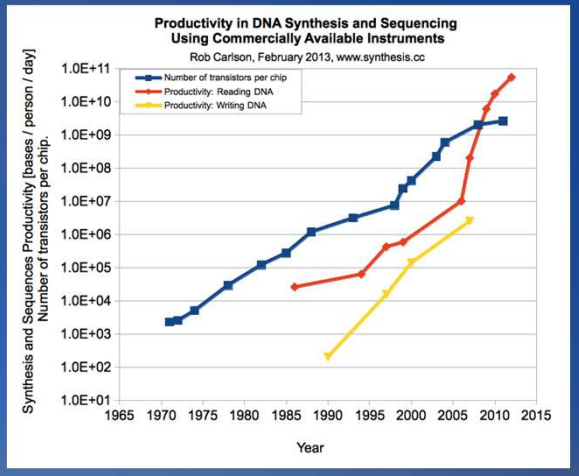


Dalchau, Chandran, Gopalkrishnan, Reif, Phillips. 2014

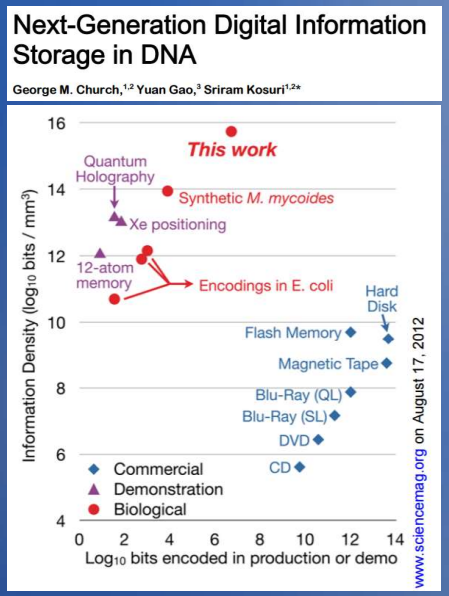
DNA Storage (Read/Write)

Information-rich physical structures can be used for storage.

DNA has a data density of 140 exabytes (1.4×10^{20} bytes) per mm^3 compared to state-of the art storage media that reaches ~500 megabytes (5×10^{8} bytes) per mm^3
DNA has been shown to be stable for millions of years



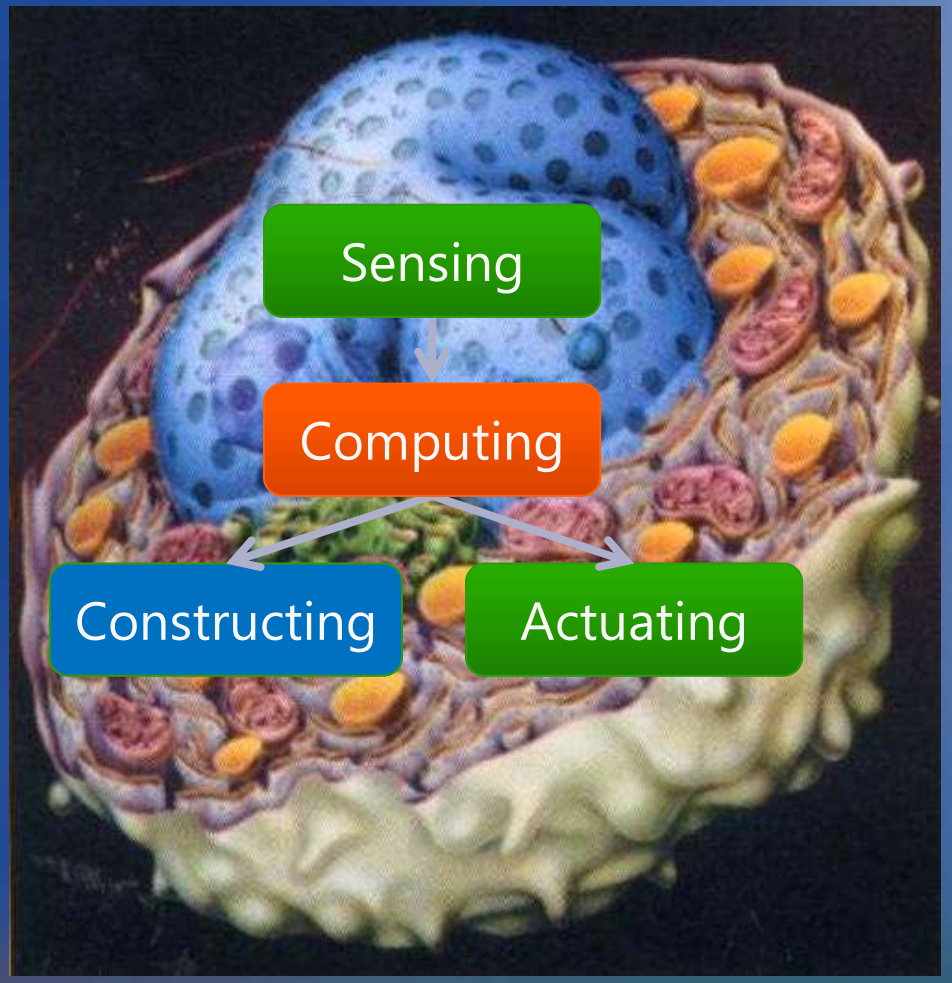
The Pace and Proliferation of Biological Technologies
March 4, 2004 by Rob Carlson



We have machines that can read (sequence) and write (synthesize) DNA. The Carslon Curve of "productivity" is growing much faster than Moore's Law.

Cost of sequencing is decreasing rapidly ($1000 whole human genome), while cost of synthesis is decreasing very slowly.
[Rob Carlson, www.synthesis.cc]

Curing



H.Lodish & al. Molecular Cell Biology 4th ed.

Interfacing to Biology

- A doctor in each cell

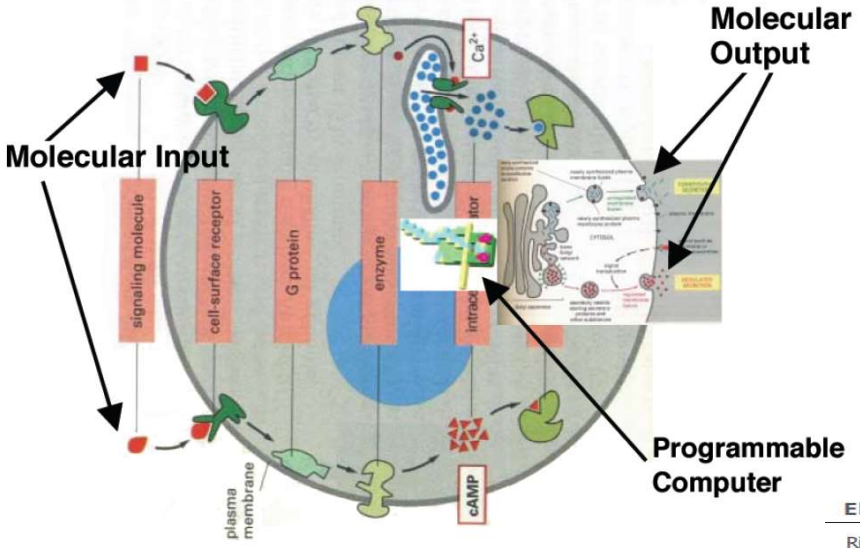


Fig. 1 Medicine in 2050: "Doctor in a Cell"

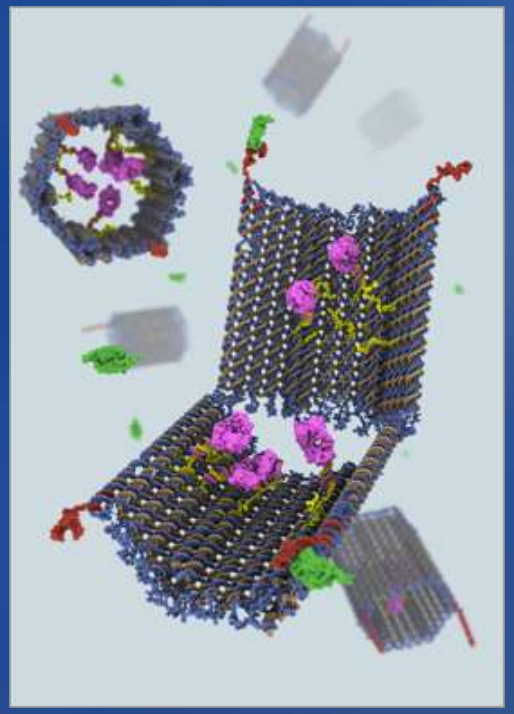
Ehud Shapiro

Rivka Adar
Kobi Benenson
Gregory Linshitz
Aviv Regev
William Silverman

Molecules and computation

~2002

Programmed Drug Delivery



A Logic-Gated Nanorobot for Targeted Transport of Molecular Payloads

Shawn M. Douglas[+], Ido Bachelet[+], George M. Church[†]
+ See all authors and affiliations

Science 17 Feb 2012:
Vol. 335, Issue 6070, pp. 831-834
DOI: 10.1126/science.1214081

Molecular Programming:
The Execution Aspect

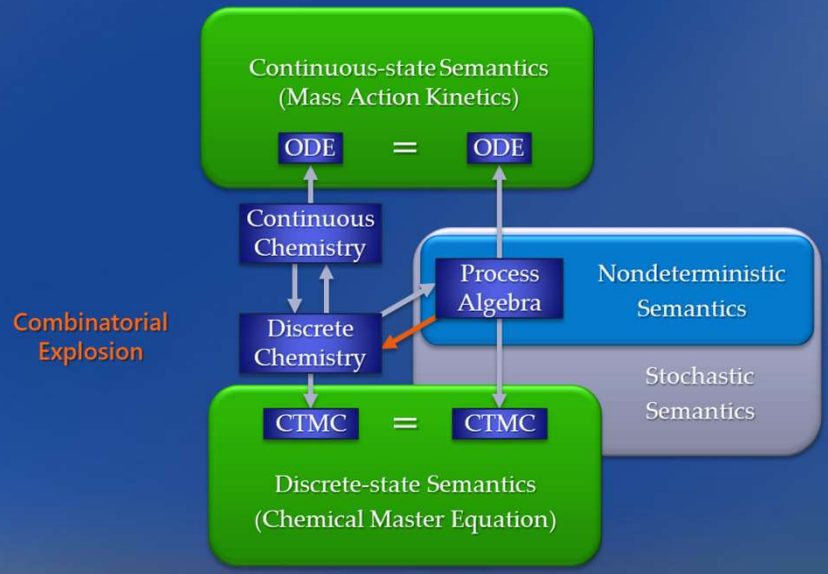
How do we "run" a molecular program?

Programming Language: Chemistry

- A Lingua Franca between Biology, Dynamical Systems, and Concurrent Languages
- Chemical Reaction Networks
  - $A + B \rightarrow_r C + D$ (the program)
- Ordinary Differential Equations
  - $d[A]/dt = -r[A][B]$ … (the behavior)
- Rich analytical techniques based on Calculus and more recently on stochastic models

Chemistry as a Concurrent Language

- A connection with the theory of concurrency
  - Via Process Algebra and Petri Nets



Chemical Programming Examples

specification

Y := min(X1, X2)

Y := max(X1, X2)

program

X1 + X2 -> Y

X1 -> L1 + Y
X2 -> L2 + Y
L1 + L2 -> K
Y + K -> 0

max(X1,X2)=
(X1+X2)-min(X1,X2)

(but is not computed "sequentially": it is a form of concurrent computation)

chemical reaction network

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Chemical Reaction Networks

- Finite list of chemical reactions over a finite set of species
  - N.B.: "abstract" species, not specific atoms/molecules that physically exist
- Computationally Powerful
  - Turing-complete up to an arbitrarily small error
- Full Turing Completeness
  - When including complexation (polymerization), which DNA enables (complexation encodes an actual infinity of chemical reactions by finite means)

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How do we "run" Chemistry?

- Chemistry is not easily executable
  - "Please Mr Chemist, execute me this bunch of reactions that I just made up"
- Most molecular languages are not executable
  - They are descriptive (modeling) languages
- How can we execute molecular languages?
  - With real molecules?
  - That we can design ourselves?
  - And that we can buy on the web?

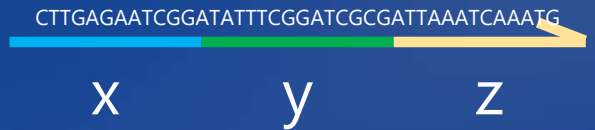
DNA Strand Displacement

An "unnatural" use of DNA for emulating *any* system of chemical reactions with real molecules

Domains

- Subsequences on a DNA strand are called domains
  - *provided* they are "independent" of each other

- Differently named domains must not hybridize
  - With each other, with each other's complement, with subsequences of each other, with concatenations of other domains (or their complements), etc.



oriented DNA single strand

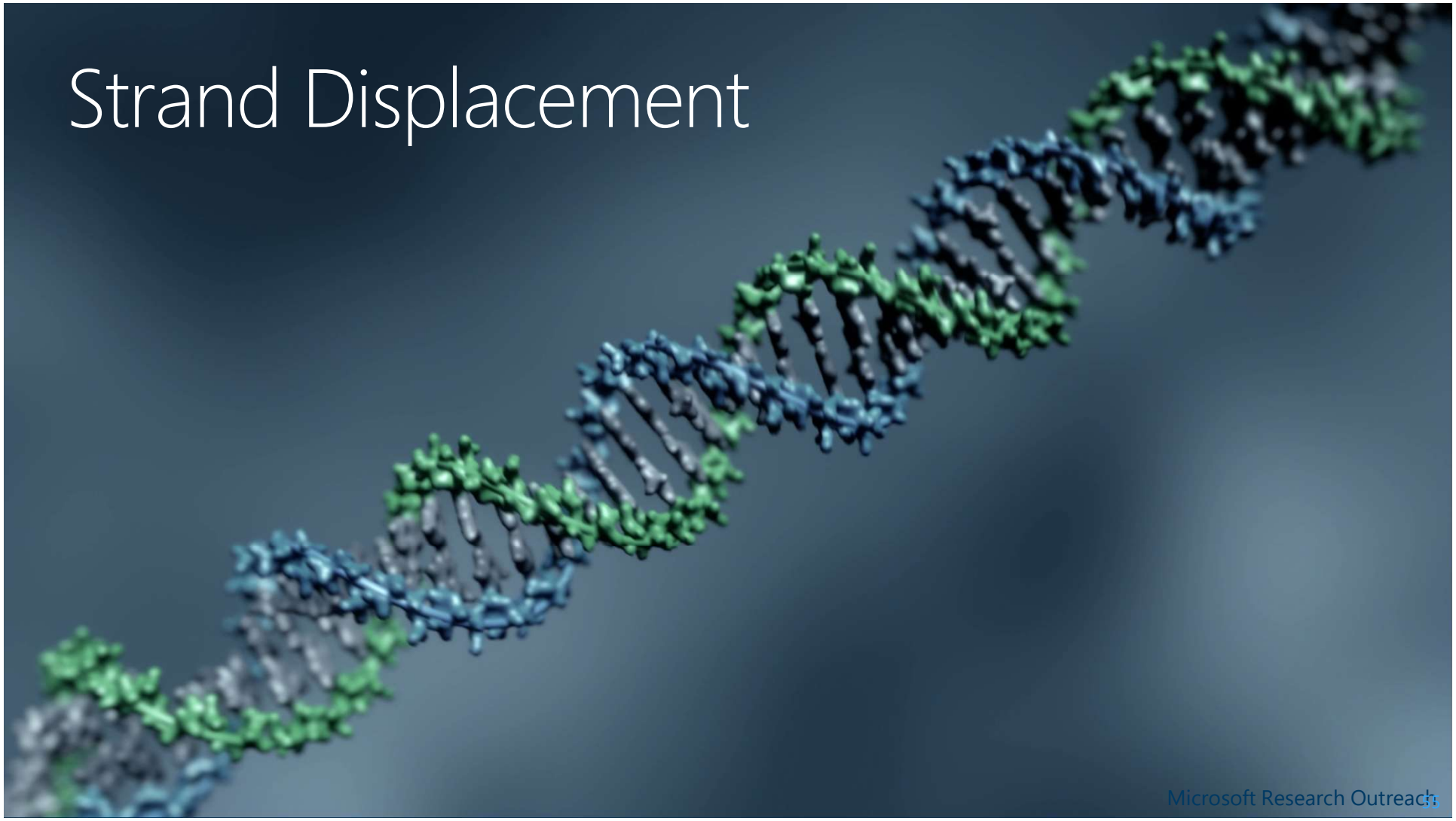
Short Domains

Reversible Hybridization

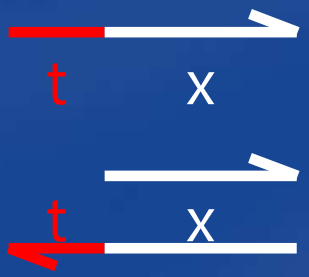
Long Domains

Irreversible Hybridization

Strand Displacement

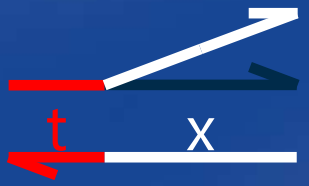


Strand Displacement



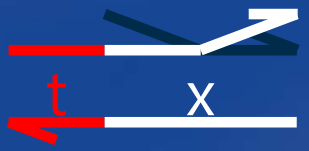
"Toehold Mediated"

Strand Displacement



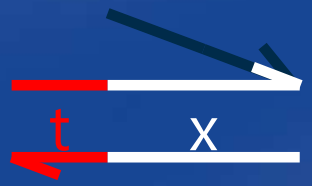
Toehold Binding

Strand Displacement



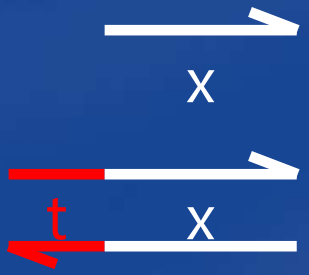
Branch Migration

Strand Displacement



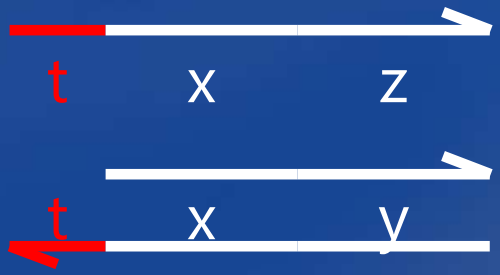
Displacement

Strand Displacement



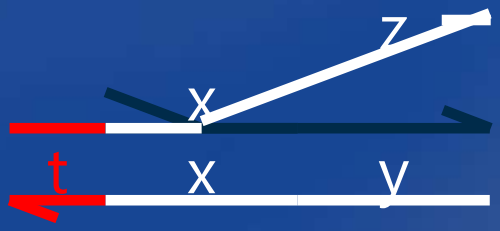
Irreversible release

Bad Match



Bad Match

Bad Match



Bad Match

Cannot proceed
Hence will undo

Two-Domain Architecture

- Signals: 1 toehold + 1 recognition region

- Gates: "top-nicked double strands" with open toeholds

Garbage collection "built into" the gate operation

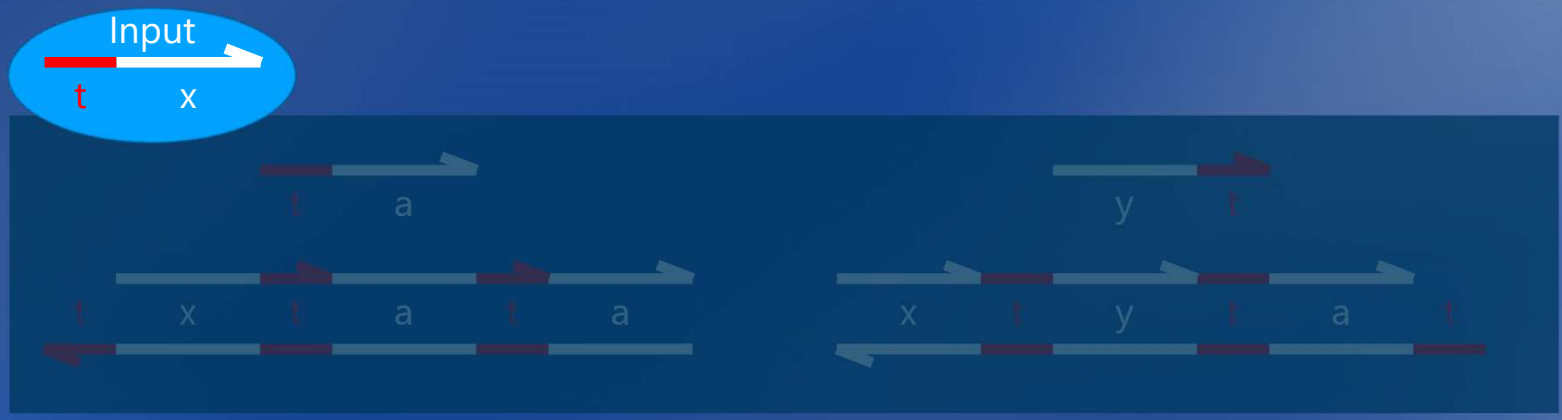
Two-Domain DNA Strand Displacement

Luca Cardelli

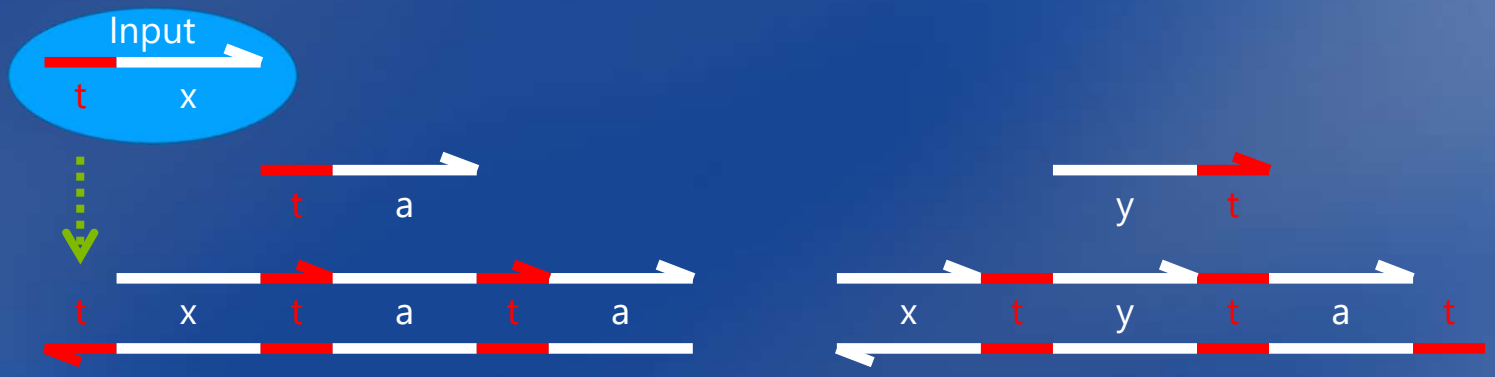
In S. B. Cooper, E. Kashefi, P. Panangaden (Eds.): Developments in Computational Models (DCM 2010). EPTCS 25, 2010, pp. 33-47. May 2010.

Transducer

Transducer x→y



Transducer x→y

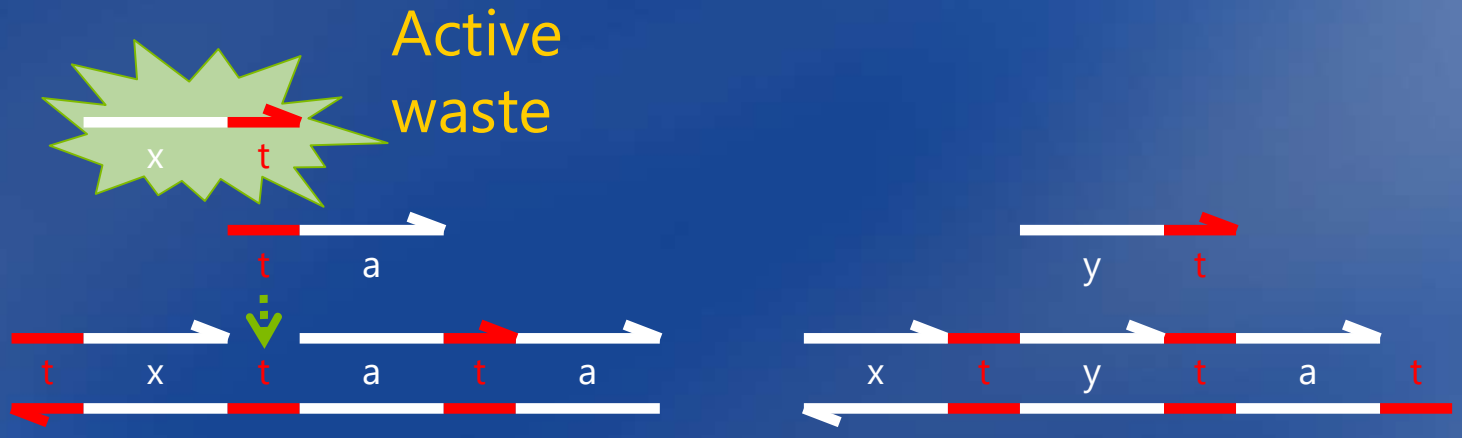


Built by self-assembly!

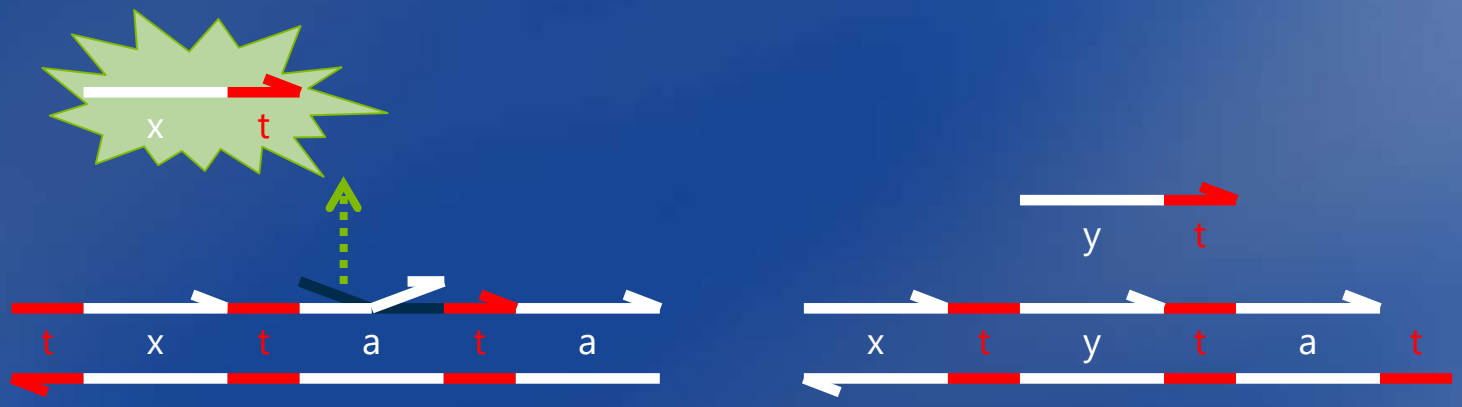
ta is a *private* signal (a different ‘a’ for each xy pair)

Transducer x→y

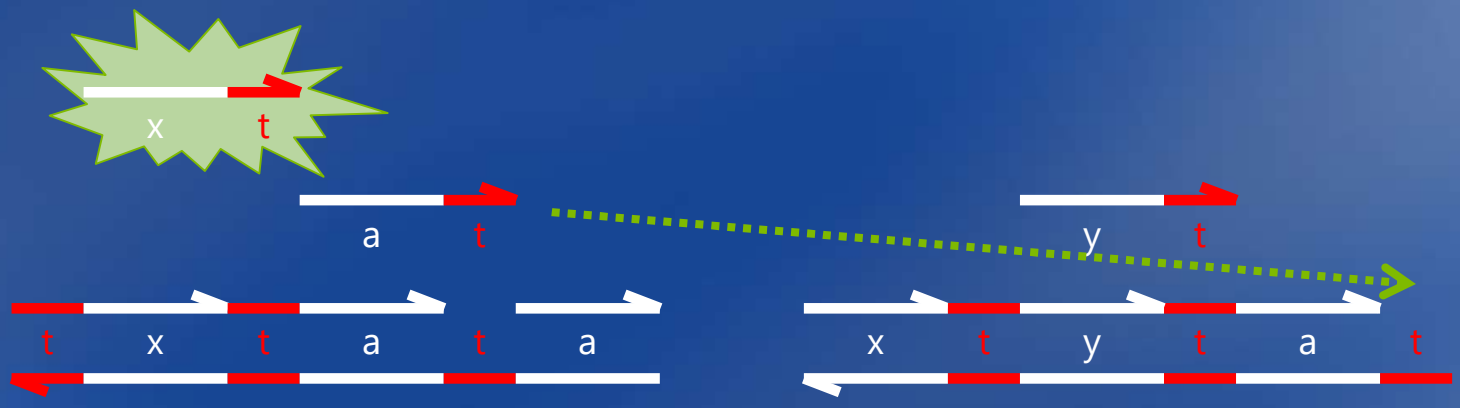
Transducer x→y



Transducer x→y

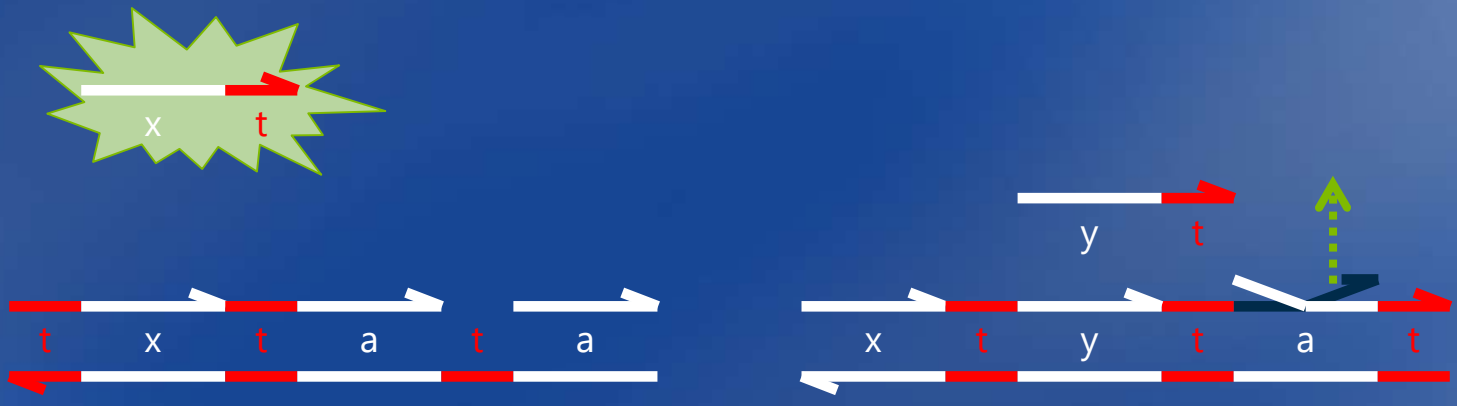


Transducer x→y

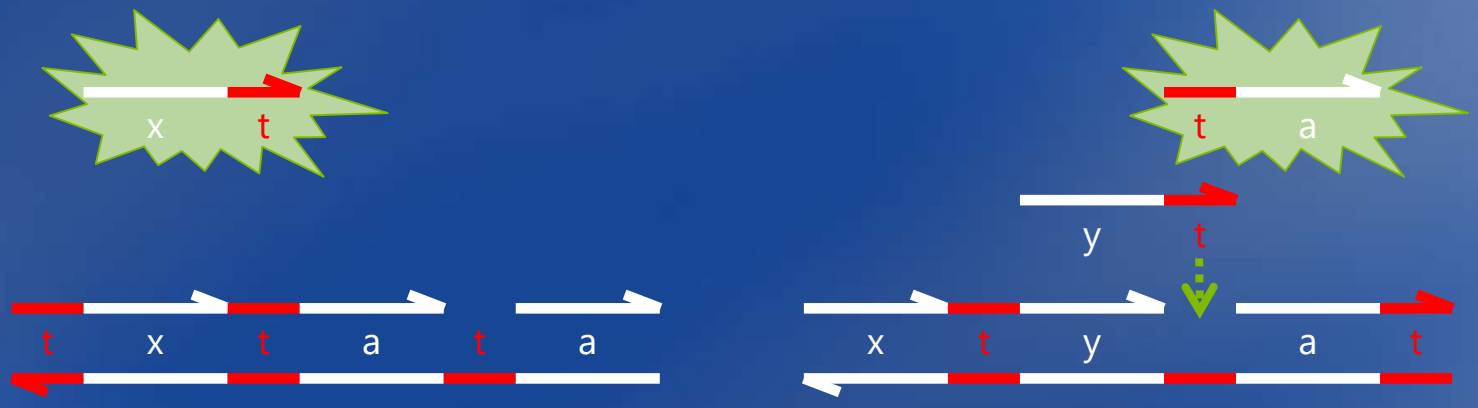


So far, a **tx** *signal* has produced an **at** *cosignal*.
But we want signals as output, not cosignals.

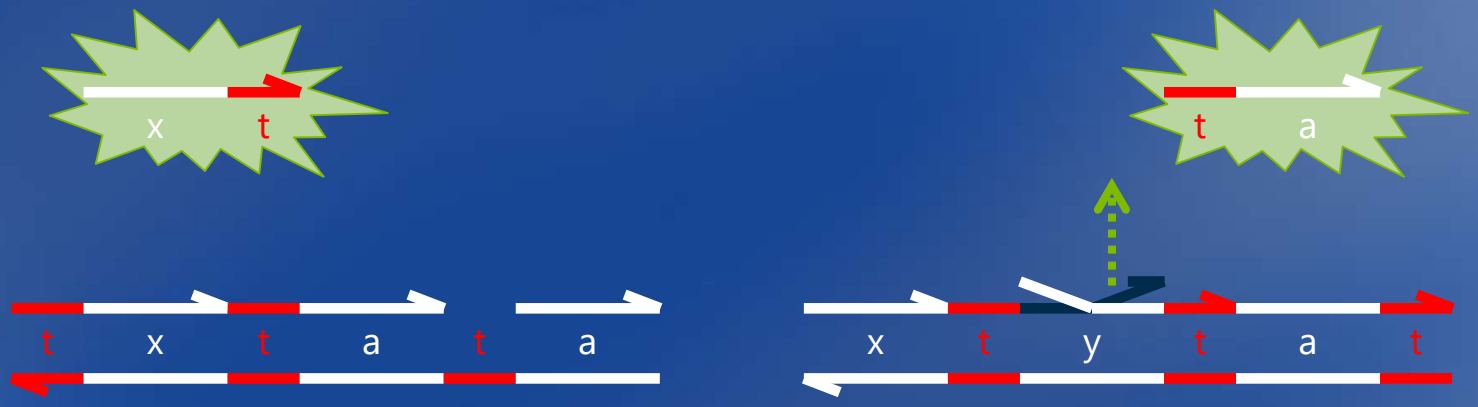
Transducer x→y



Transducer x→y



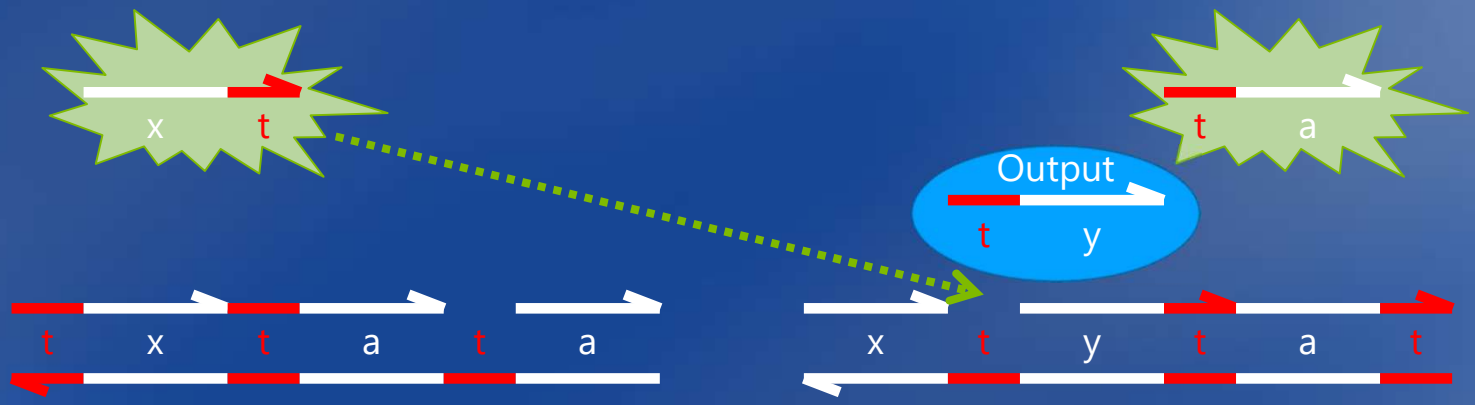
Transducer x→y



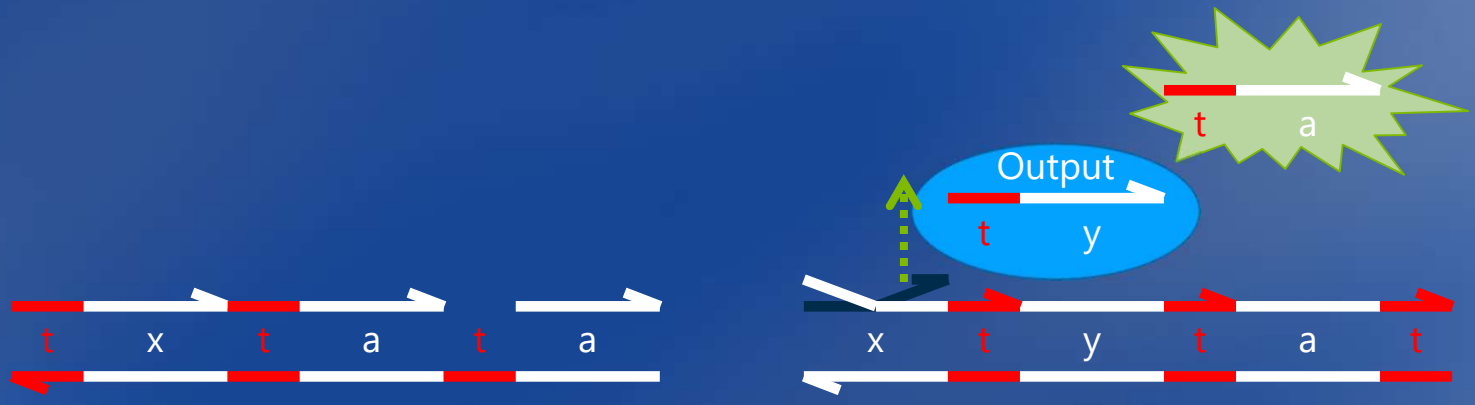
Transducer x→y

Here is our output **ty** *signal*.
But we are not done yet:
1) We need to make the output irreversible.
2) We need to remove the garbage.
We can use (2) to achieve (1).

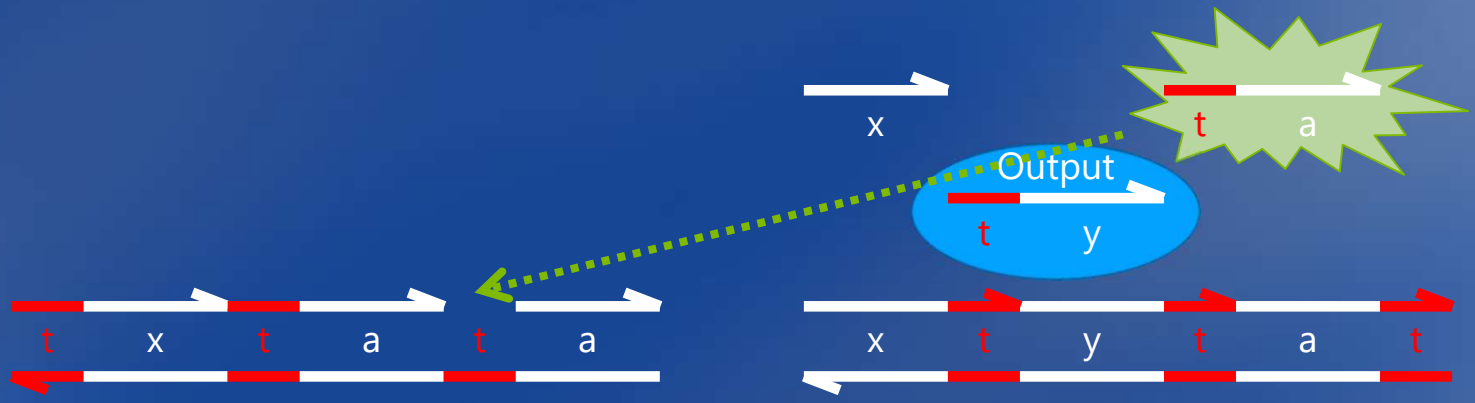
Transducer x→y



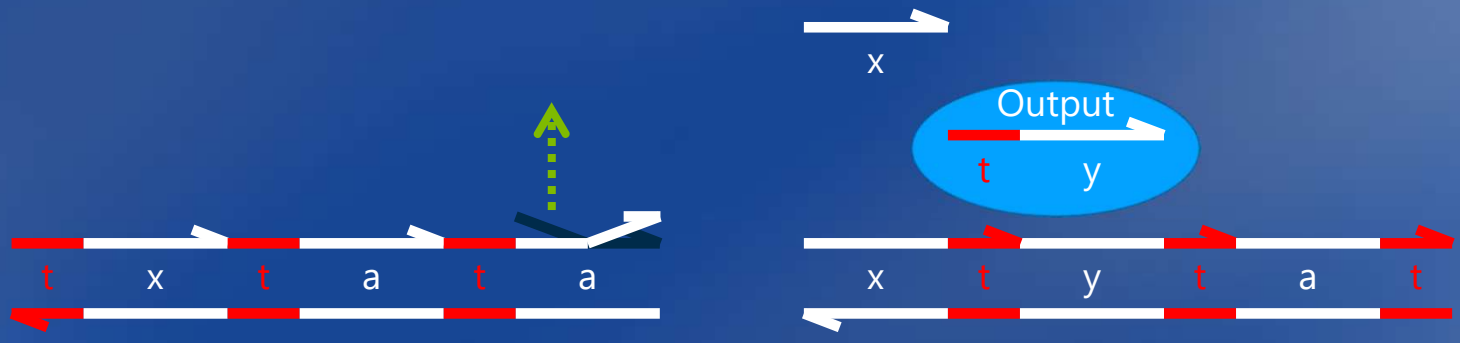
Transducer x→y



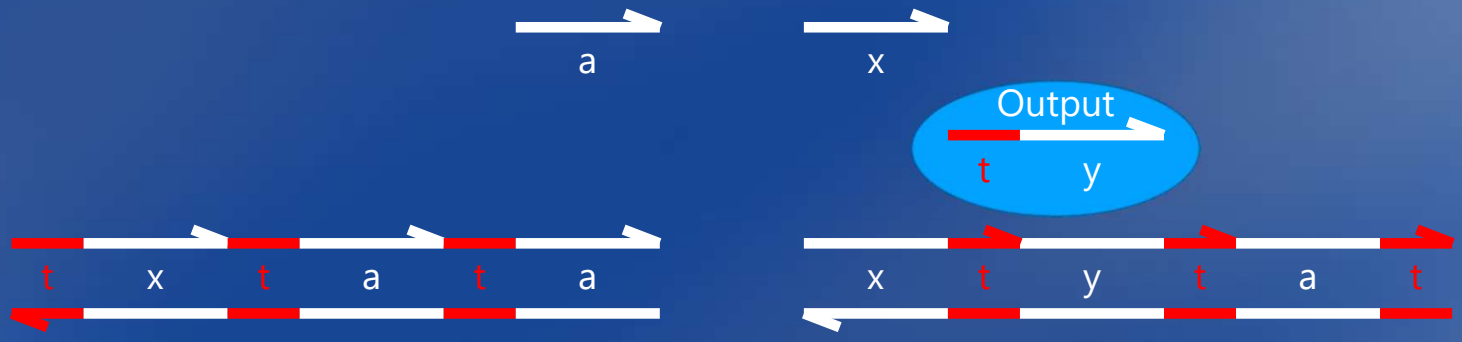
Transducer x→y



Transducer x→y



Transducer x→y



Transducer x→y

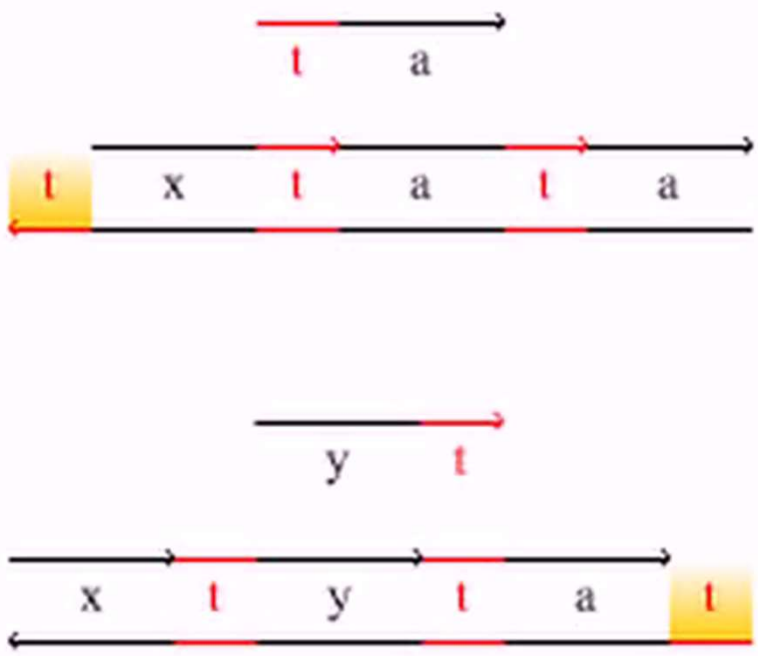
Done.

N.B. the gate is consumed: it is the energy source

(no proteins, no enzymes, no heat-cycling, etc.; just DNA in salty water)

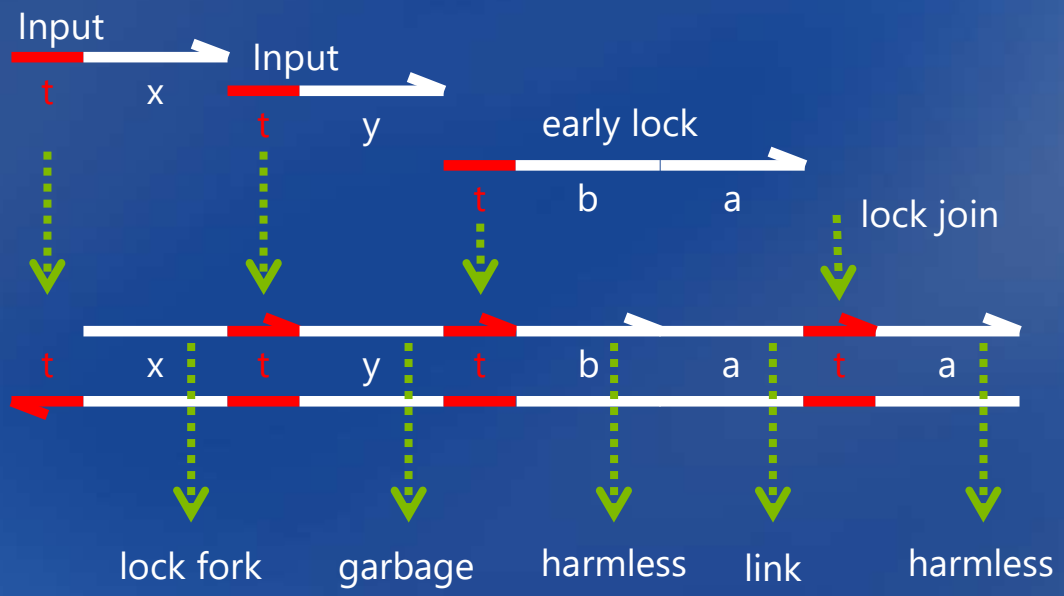
Powered by Sothink

Transducer x → y



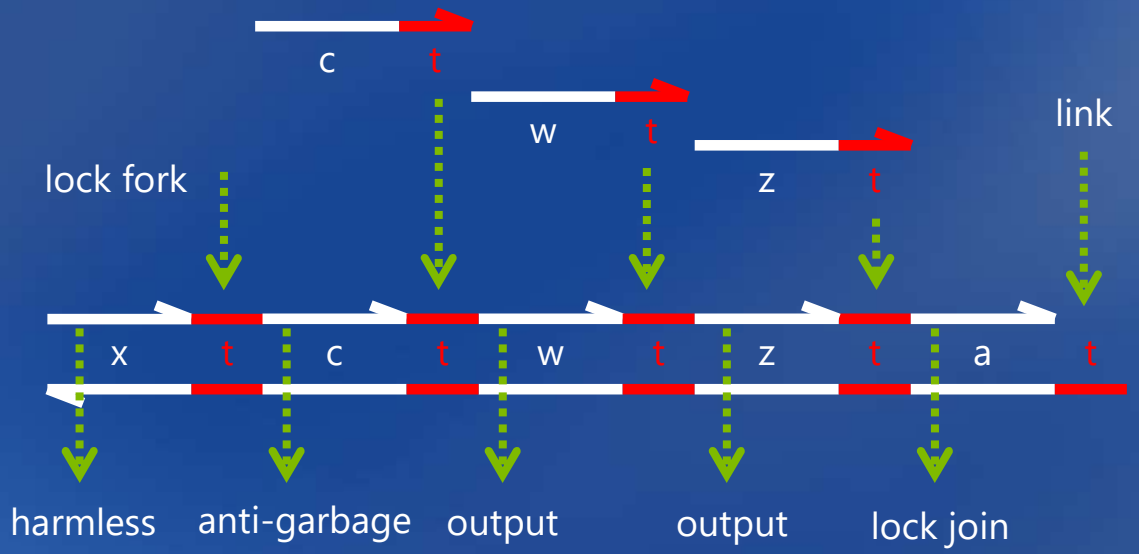
Reaction $x + y \rightarrow z + w$

join
half



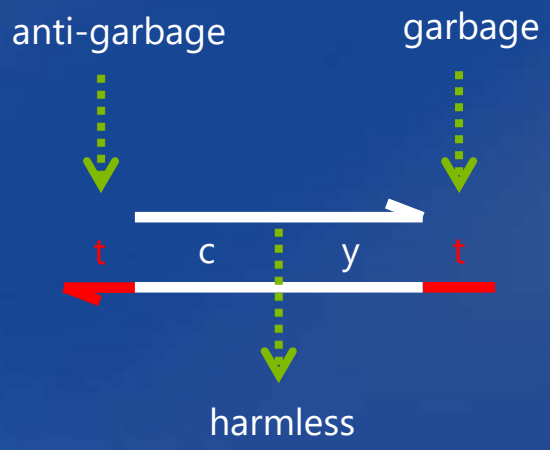
Reaction $x + y \rightarrow z + w$

fork
half



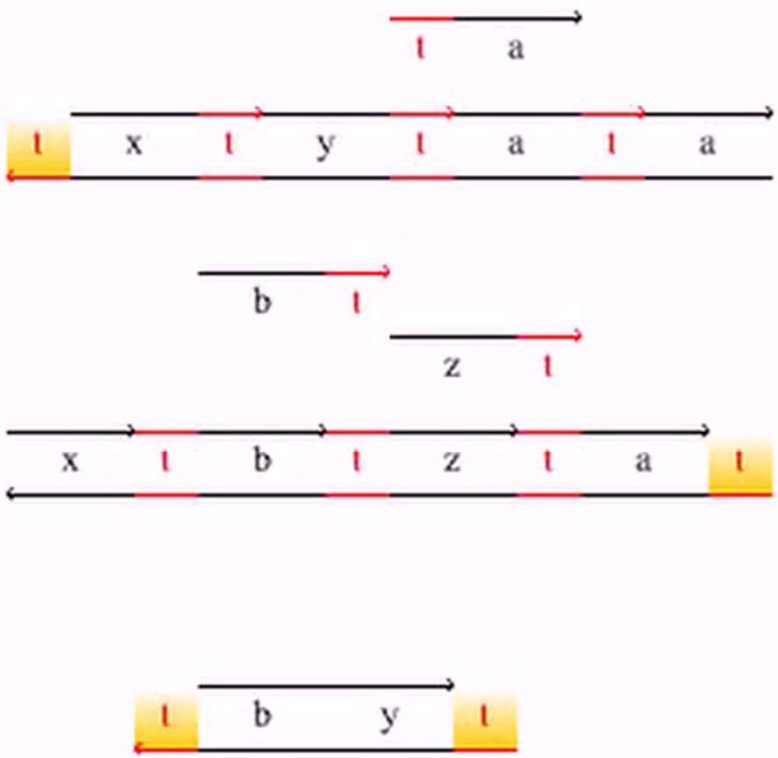
Reaction $x + y \rightarrow z + w$

garbage collection



Powered by Sothink

Join x+y → z

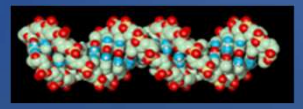


Approximate Majority Algorithm

- Given two populations of agents (or molecules)
  - Randomly communicating by radio (or by collisions)
  - Reach an agreement about which population is in majority
  - By converting all the minority to the majority
    [Angluin et al., Distributed Computing, 2007]

- 3 rules of agent (or molecule) interaction
  - $X + Y \rightarrow B + B$
  - $B + X \rightarrow X + X$
  - $B + Y \rightarrow Y + Y$

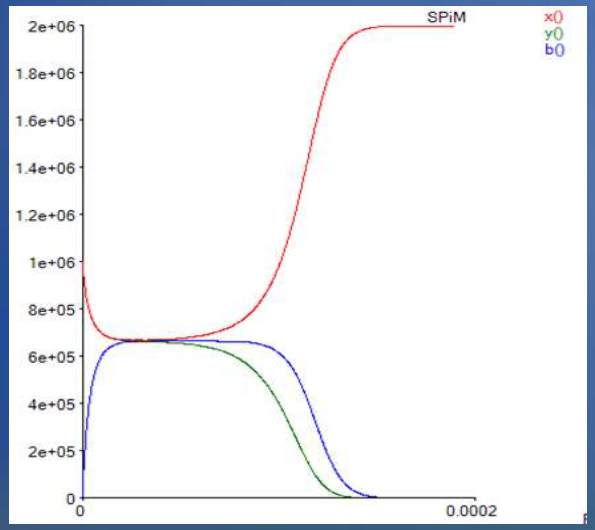
"our program" →



Optimal Consensus Algorithm

- Fast: reaches agreement in O(log n) time w.h.p.
  - O(n log n) communications/collisions
  - Even when initially #X = #Y! (stochastic symmetry breaking)

- Robust: true majority wins w.h.p.
  - If initial majority exceeds minority by $\omega(\sqrt{n} \log n)$
  - Hence the agreement state is stable



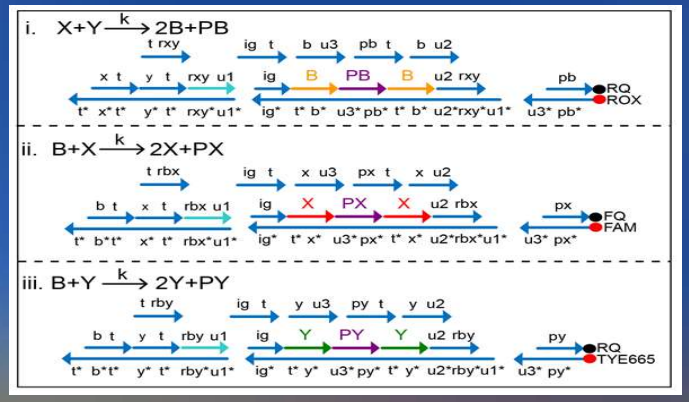
Stochastic simulation of worst-case scenario with initially #X = #Y

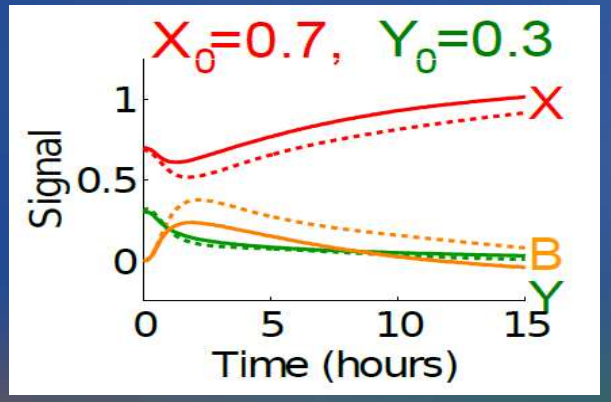
DNA Implementation of the Approximate Majority algorithm

nature nanotechnology

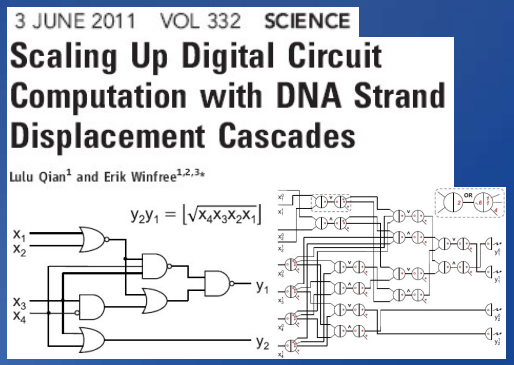
Programmable chemical controllers made from DNA

Yuan-Jyue Chen, Neil Dalchau, Niranjan Srinivas, Andrew Phillips, Luca Cardelli, David Soloveichik & Georg Seelig

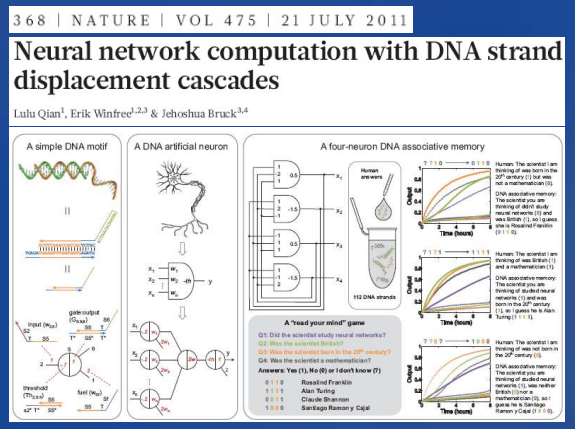




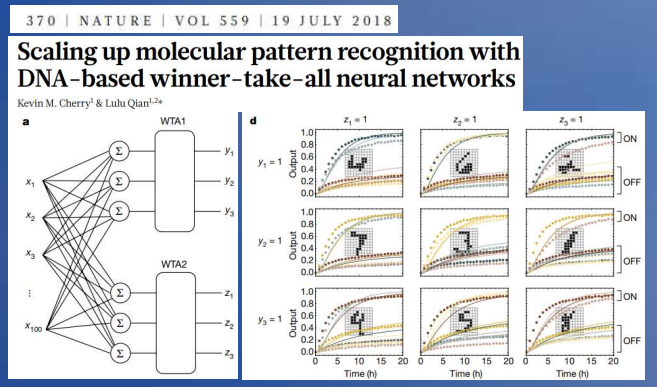
Some Large-scale Circuits (so far…)



Computing the square root of a 4-bit number



Classifying 4 distinct 4-bit patterns via 4 neurons



Classifying 9 distinct 100-bit patterns via WTA networks

Scaling up: DNA Circuit Boards

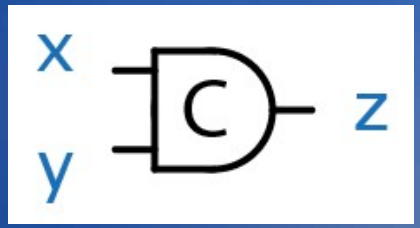
ARTICLES
PUBLISHED ONLINE: 24 JULY 2017 | DOI: 10.1038/NNANO.2017.127
nature nanotechnology

A spatially localized architecture for fast and modular DNA computing

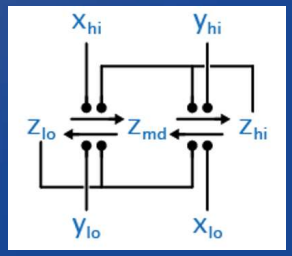
Gourab Chatterjee[1], Neil Dalchau[2], Richard A. Muscat[3], Andrew Phillips[2]* and Georg Seelig[3,4]*

The first computational circuit boards made of DNA
https://www.microsoft.com/en-us/research/blog/researchers-build-nanoscale-computational-circuit-boards-dna

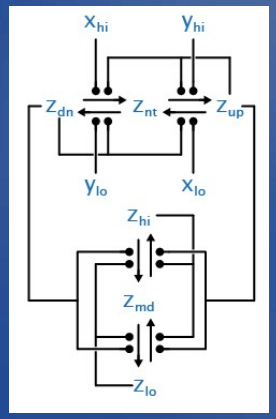
Avoiding Clocks



- Muller C-Element
  - A Boolean gate
  - When x = y then z = x = y, otherwise z remembers its *last* state.



Core C-Element
(AM with external inputs)



Full C-Element with output rectified by another AM

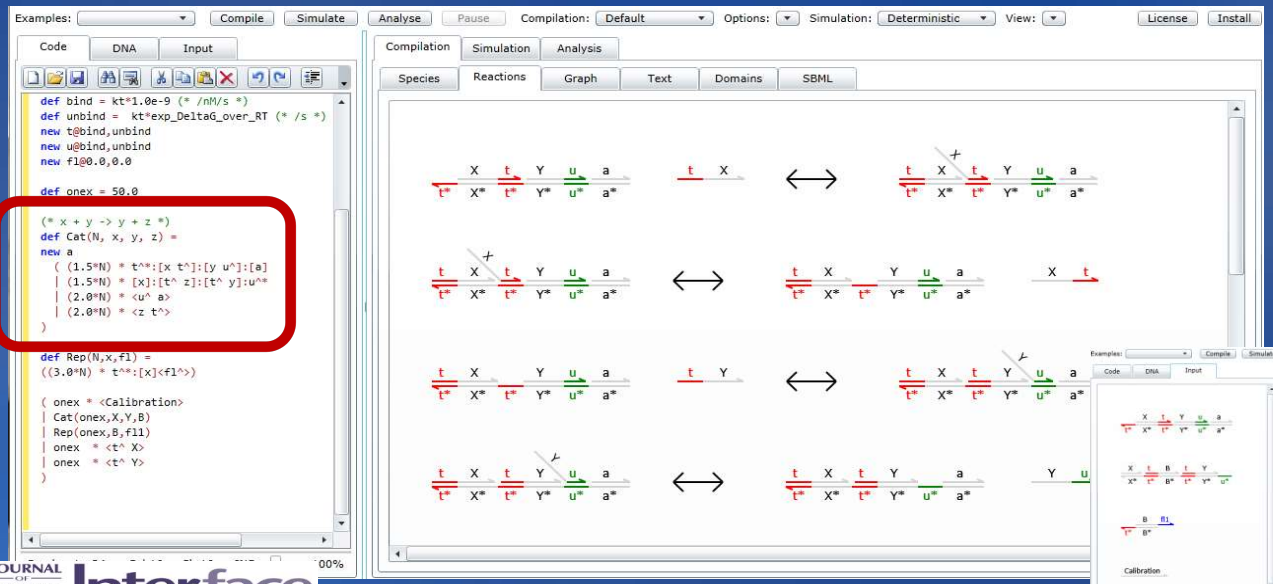
Chemical Reaction Network Designs for Asynchronous Logic Circuits.
Luca Cardelli, Marta Kwiatkowska, Max Whitby.
Natural Computing Journal.

Algorithm Design

A software pipeline for Molecular Programming

Development Tools

MSRC Biological Computation Group



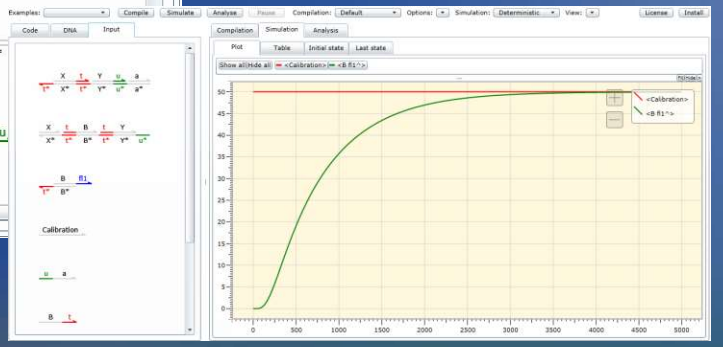
JOURNAL OF THE ROYAL SOCIETY Interface

A programming language for composable DNA circuits

Andrew Phillips and Luca Cardelli

Visual DSD

A Development Environment for DNA Strand Displacement



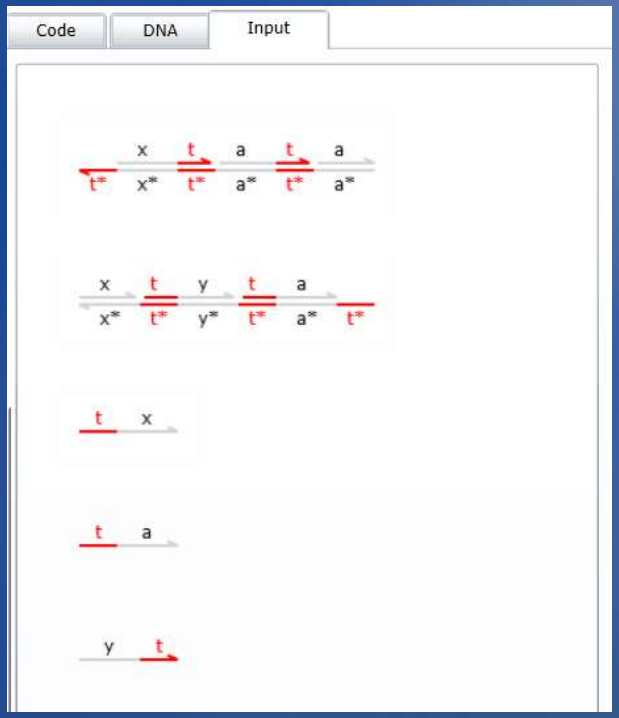
A Language for DNA Structures

- Describe the initial *structures* (not behavior)

Code | DNA | Input

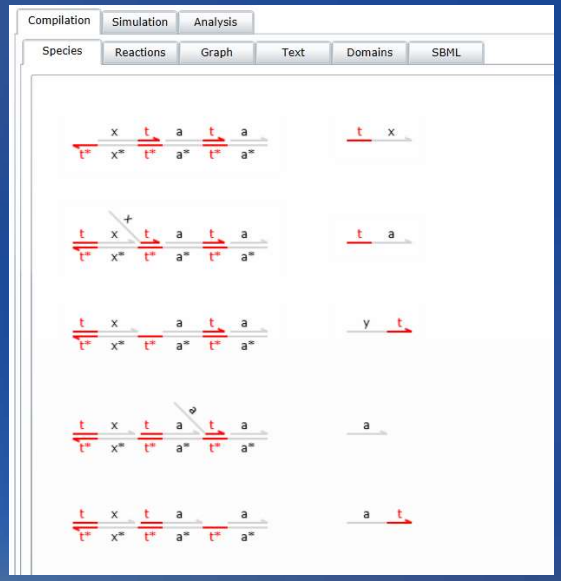
```
directive duration 10000.0 points 1000
directive plot <t^ x>; <t^ y>; <t^ z>
new t

def T(N,x,y) =
  new a
  ( N * <t^ a>
  | N * <y t^>
  | N * t^*:[x t^]:[a t^]:[a] (* Input gate *)
  | N * [x]:[t^ y]:[t^ a]:t^* (* Output gate *)
  )

( <t^ x> | T(1,x,y) )
```

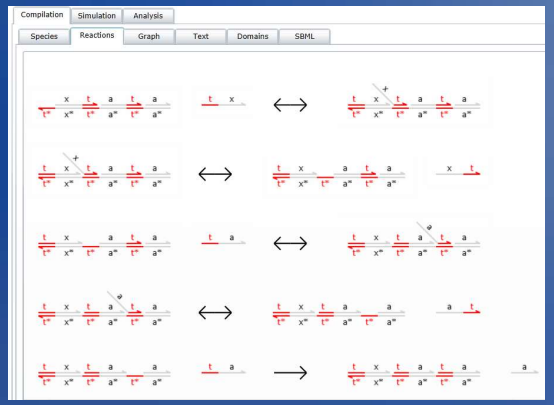
=

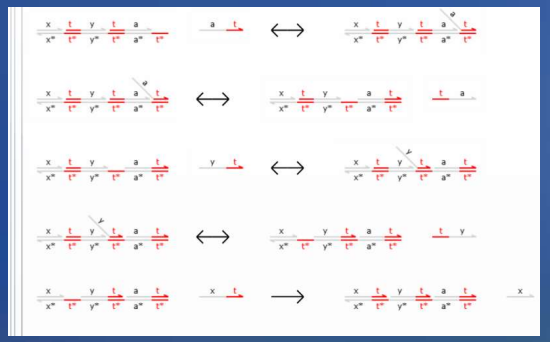


Compute Species and Reactions

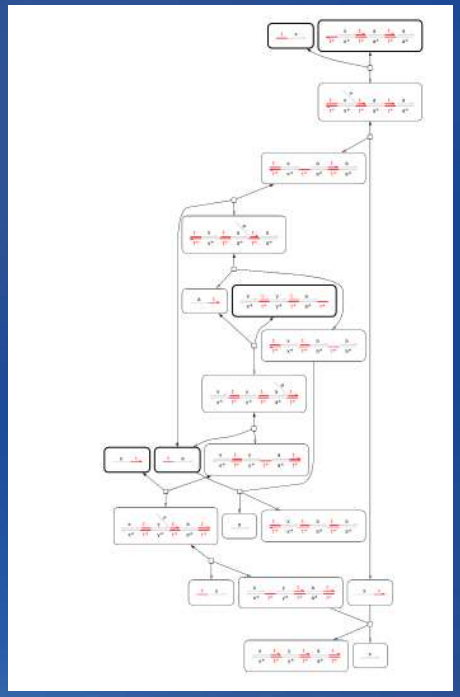
- Recursively computed from the initial structures







Reaction Graph and Export



Compilation | Simulation | Analysis

Species | Reactions | Graph | Text | Domains | SBML

Save as XML

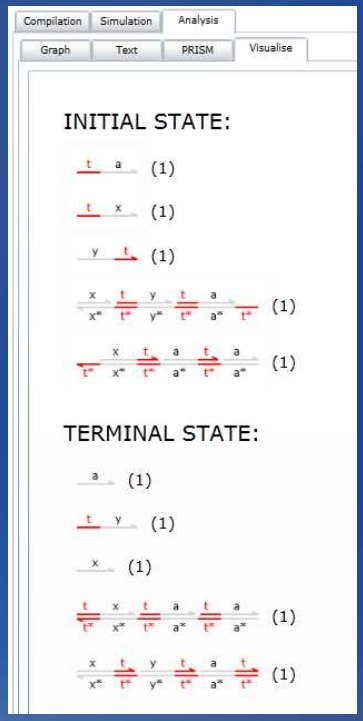
```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version1" level="2" version="1">
  <model>
    <listOfCompartments>
      <compartment id="c" size="1"/>
    </listOfCompartments>
    <listOfSpecies>
      <species id="s_id0" name="&lt;t^ x&gt;" compartment="c" initialAmount="1" constant="false"/>
      <species id="s_id1" name="&lt;t^ a&gt;" compartment="c" initialAmount="1" constant="false"/>
      <species id="s_id2" name="&lt;y t^&gt;" compartment="c" initialAmount="1" constant="false"/>
      <species id="s_id3" name="{t^*}[x t^]:[a t^]:[a]" compartment="c" initialAmount="1" constant="false"/>
      <species id="s_id4" name="[t^ x]:&lt;x&gt;[t^]:[a t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id5" name="[t^ x]{t^*}:[a t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id6" name="[t^ x]:[t^ a]:&lt;a&gt;[t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id7" name="[t^ x]:[t^ a]{t^*}:[a]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id8" name="[t^ x]:[t^ a]:[t^ a]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id9" name="&lt;a&gt;" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id10" name="&lt;a t^&gt;" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id11" name="&lt;x t^&gt;" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id12" name="[x]:[t^ y]:[t^ a]{t^*}" compartment="c" initialAmount="1" constant="false"/>
      <species id="s_id13" name="[x]:[t^ y]:[t^ a]:&lt;a&gt;[t^]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id14" name="[x]:[t^ y]{t^*}:[a t^]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id15" name="[x]:[t^ y]:&lt;y&gt;[t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id16" name="[x]{t^*}:[y t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id17" name="[x t^]:[y t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id18" name="&lt;x&gt;" compartment="c" initialAmount="0" constant="false"/>
      <species id="s_id19" name="&lt;t^ y&gt;" compartment="c" initialAmount="0" constant="false"/>
    </listOfSpecies>
    <listOfReactions>
      <reaction id="r_id20" reversible="false">
        <listOfReactants>
          <speciesReference species="s_id3"/>
          <speciesReference species="s_id0"/>
```

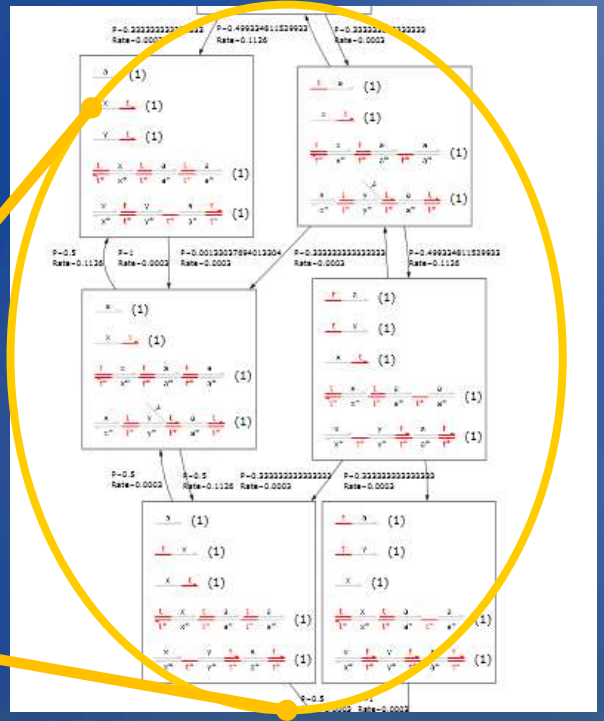
Simulation

- Deterministic
- Stochastic (Gillespie)
- Probabilistic (CME)
- Linear Noise Approximation
- "JIT"

State Space Analysis

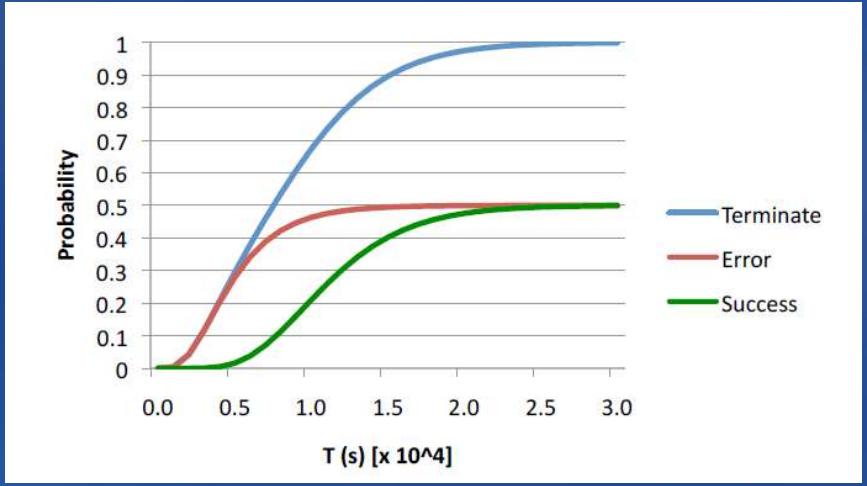
CTMC





Modelchecking

- Export to PRISM probabilistic modelchecker



JOURNAL OF THE ROYAL SOCIETY Interface

Design and analysis of DNA strand displacement devices using probabilistic model checking

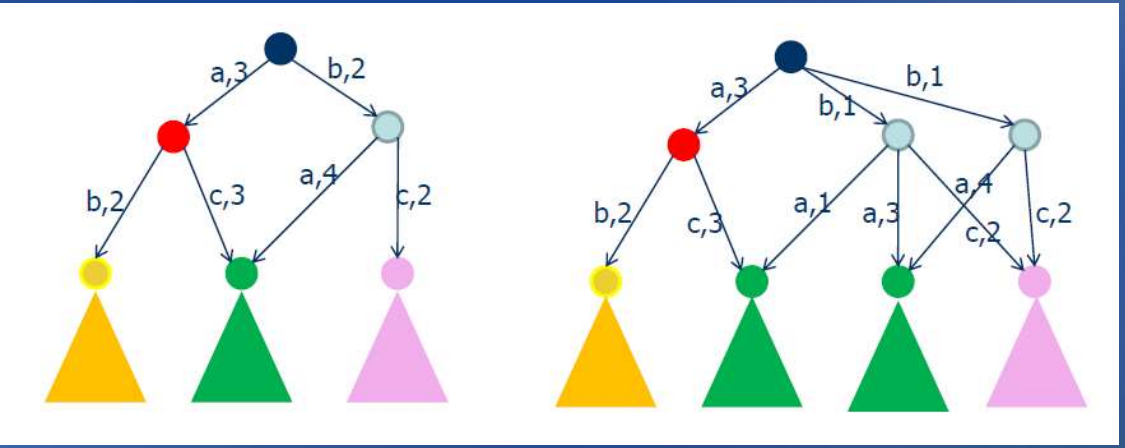
Matthew R. Lakin[1,3,†], David Parker[2,†], Luca Cardelli[1], Marta Kwiatkowska[2] and Andrew Phillips[1,*]

Verification

- Quantitative theories of system equivalence and approximation.

CONTINUOUS MARKOVIAN LOGICS
AXIOMATIZATION AND QUANTIFIED METATHEORY

RADU MARDARE, LUCA CARDELLI, AND KIM G. LARSEN

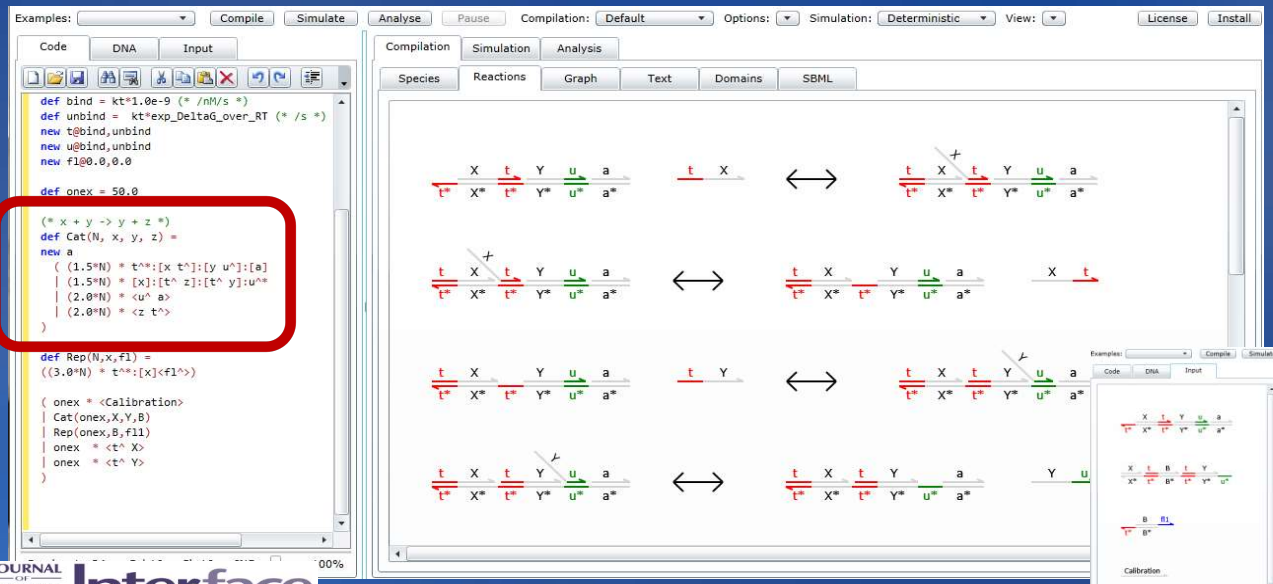


Physical Execution

A wetlab pipeline for Molecular Programming

Computer Aided Design

MSRC Biological Computation Group



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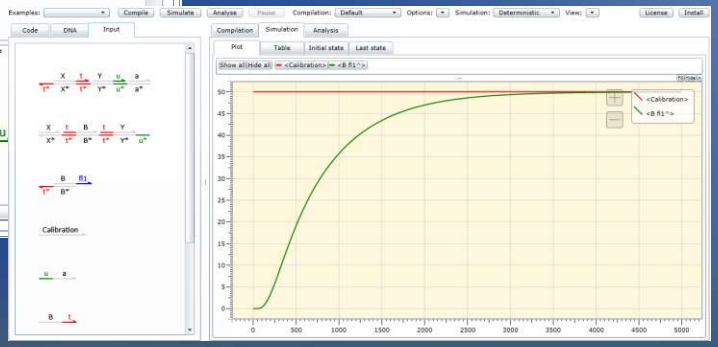
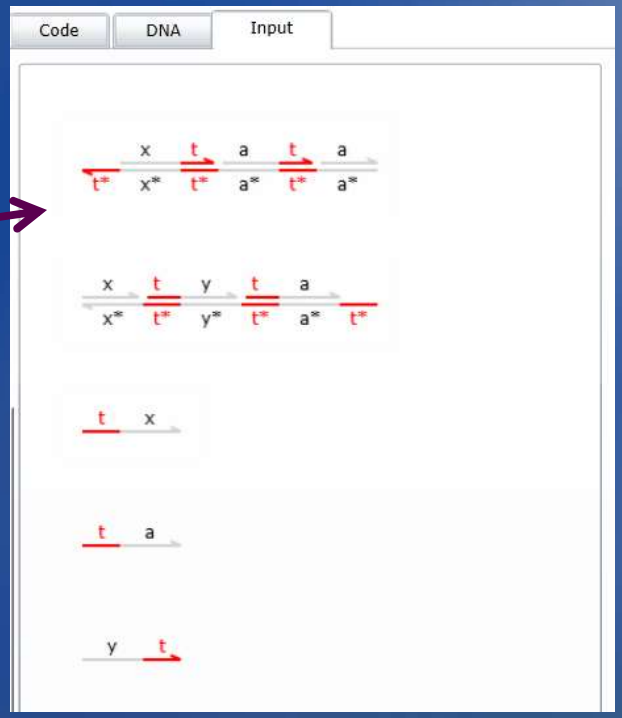


Output of Design Process

- Domain structures
  - (DNA sequences to be determined)

"Ok, how do I run this for real?"

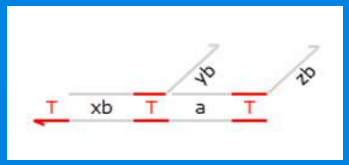
"What are the actual DNA sequences?"

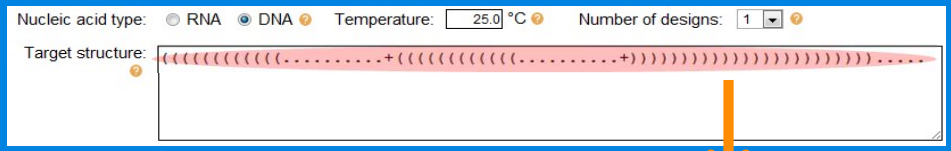


From Structures to Sequences

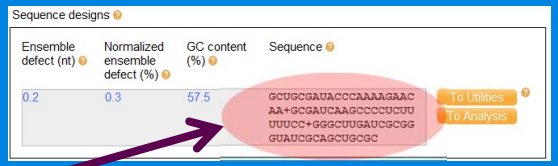
www.nupack.org

DSD Structure → "Dot-Paren" representation

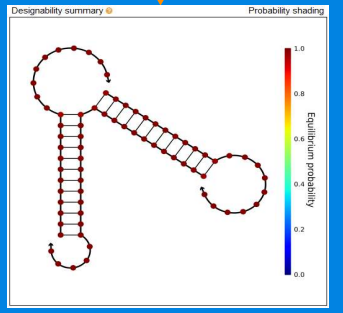




Output Sequences

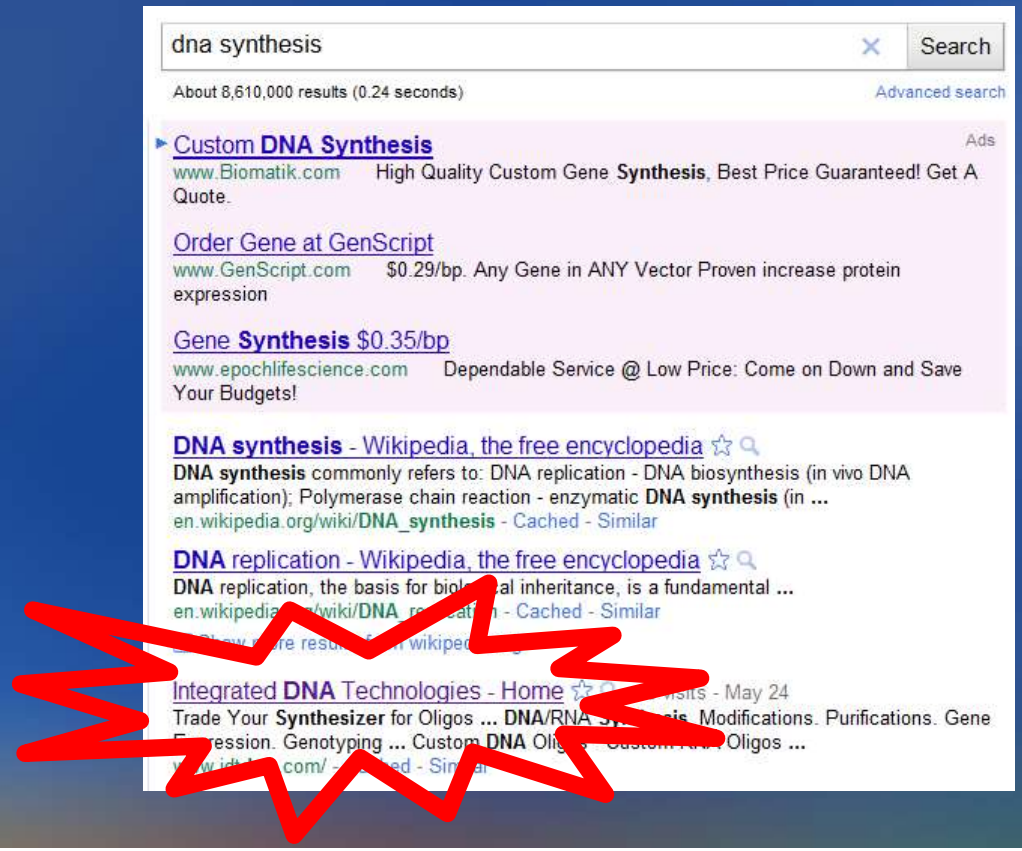


Thermodynamic Synthesis



"Ok, where do I buy these?"

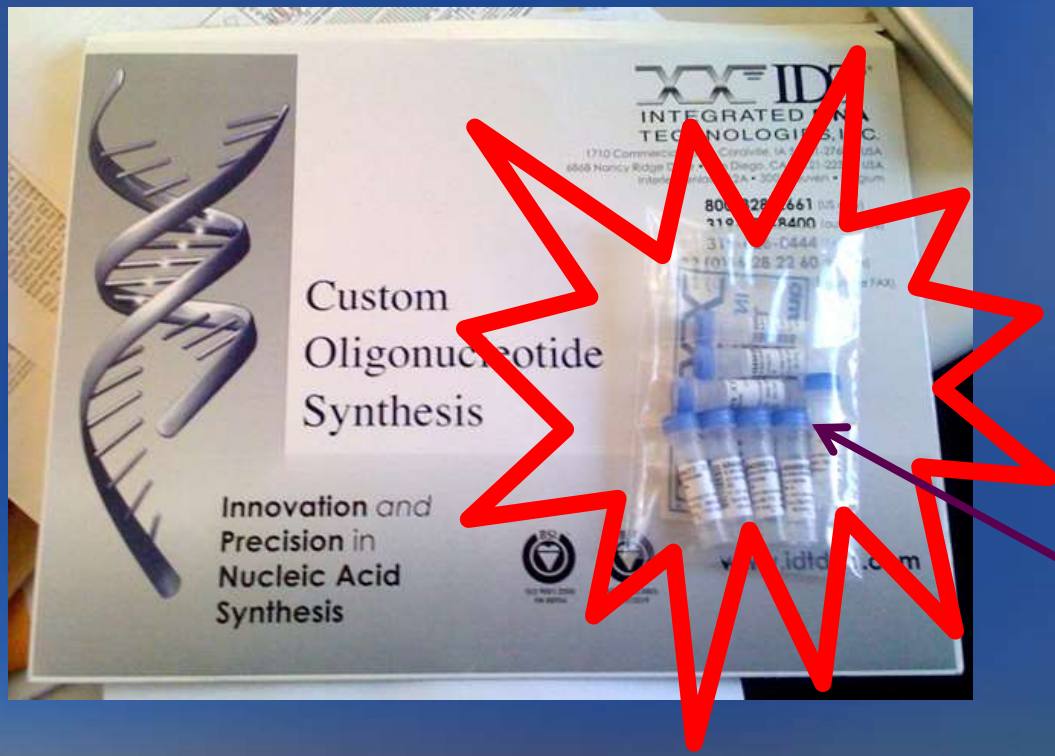
"DNA Synthesis"



From Sequences to Molecules

- Copy&Paste from nupack

Molecules by FedEx

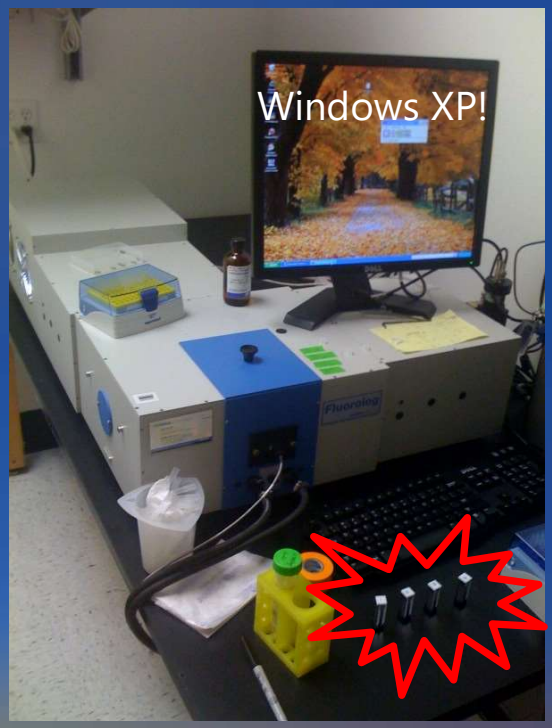


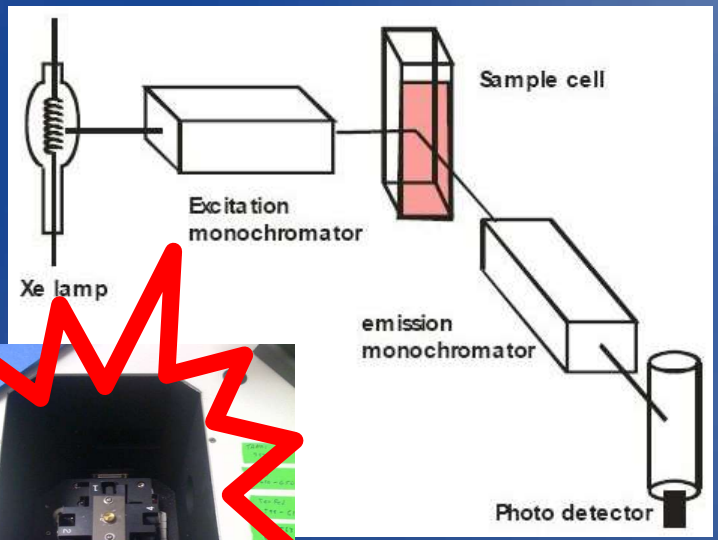
"Ok, how do I run these?"

Add Water

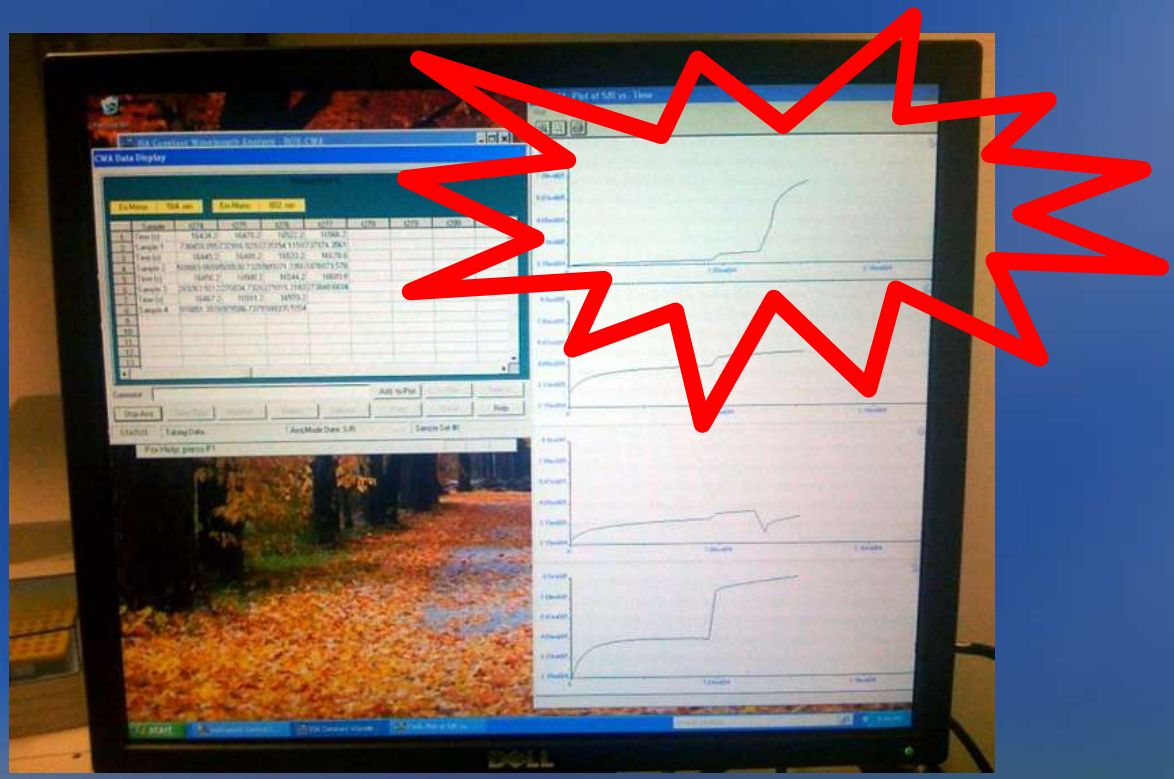
Execute (finally!)

- Fluorescence is your one-bit ‘print’ statement





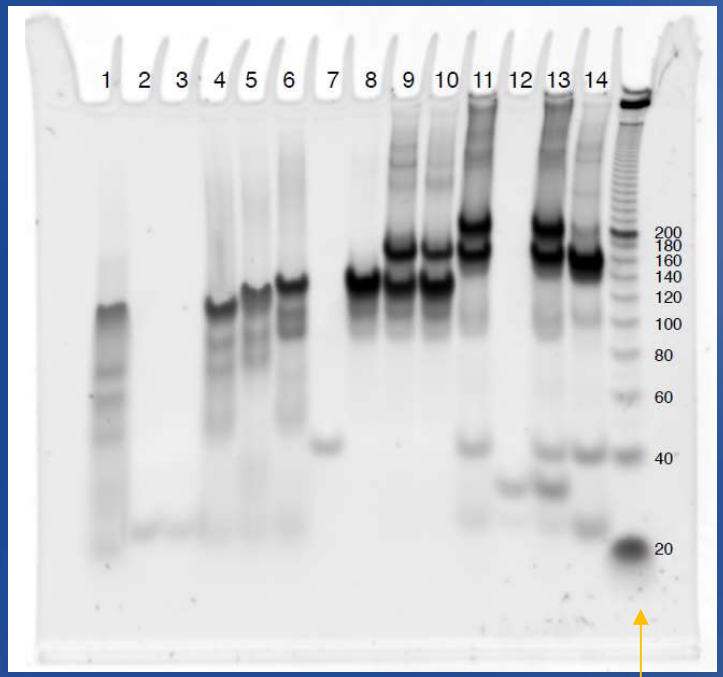
Output



Debugging

- A core dump

polyacrylamide gel electrophoresis



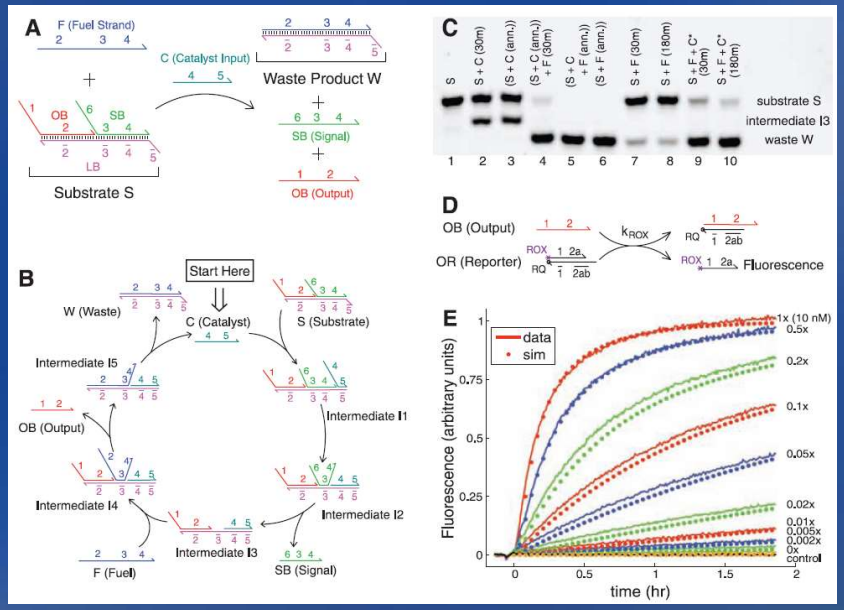
DNA strand length

Various processing stages

Calibration scale

Delivery!

Engineering Entropy-Driven Reactions and Networks Catalyzed by DNA
David Yu Zhang, *et al.*
Science **318**, 1121 (2007);
DOI: 10.1126/science.1148532



Final Remarks

"Modern" DNA Computing

- Non-goals
  - Not to solve NP-complete problems with large vats of DNA
  - Not to replace silicon
- Bootstrapping a carbon-based technology
  - To precisely control the organization and dynamics of matter and information at the molecular level
  - DNA is our engineering material
    - Its biological origin is "accidental" (but convenient)
    - It is an information-bearing programmable material
    - Other such materials will be (are being) developed

State of the art

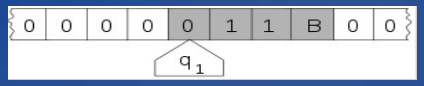
- Building a full software/hardware pipeline for a new fundamental technology
  - Mathematical Foundations [~ concurrency theory in the 80's]
  - Programming Languages [~ software engineering in the 70's]
  - Analytical Methods and Tools [~ formal methods in the 90's]
  - Device Architecture and Manufacturing [~ electronics in the 60's]
- To realize the potential of Molecular Programming
- "With *no alien technology*" [David Soloveichik]
- We have some good strategies. Device design is now largely a 'software problem' but with a significant 'engineering scaleup and integration' problem

Ongoing Challenges

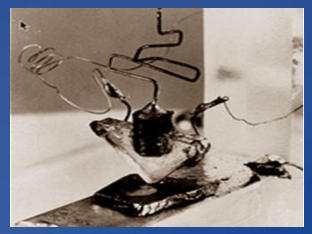
- In-vivo DNA survivability
- Complexity (and crosstalk)
- Manufacturing
- Speed
- Energy

A Brief History of DNA

Turing Machine, 1936

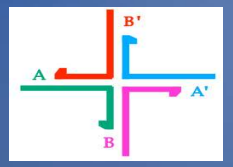


Transistor, 1947

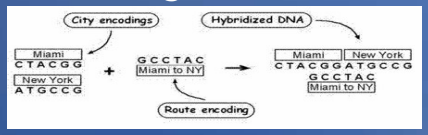


DNA, -3,800,000,000

Structural DNA Nonotech, 1982



DNA Algorithm, 1994



Computer programming

Systematic manipulation of information

Systematic manipulation of matter

Molecular programming

20th century

21th century

Resources

- DNA Computing and Molecular Programming Conference - incarnations since 1995
  http://www.dna-computing.org/
- Molecular Programming Project (Caltech - U.W. - Harvard - UCSF)
  http://molecular-programming.org/ (2008-2018 NSF Expeditions in Computing)
- Georg Seelig's DNA Nanotech Lab at U.W. CS&E
  http://homes.cs.washington.edu/~seelig/
- Biological Computation Group at Microsoft
  https://www.microsoft.com/en-us/research/group/biological-computation/