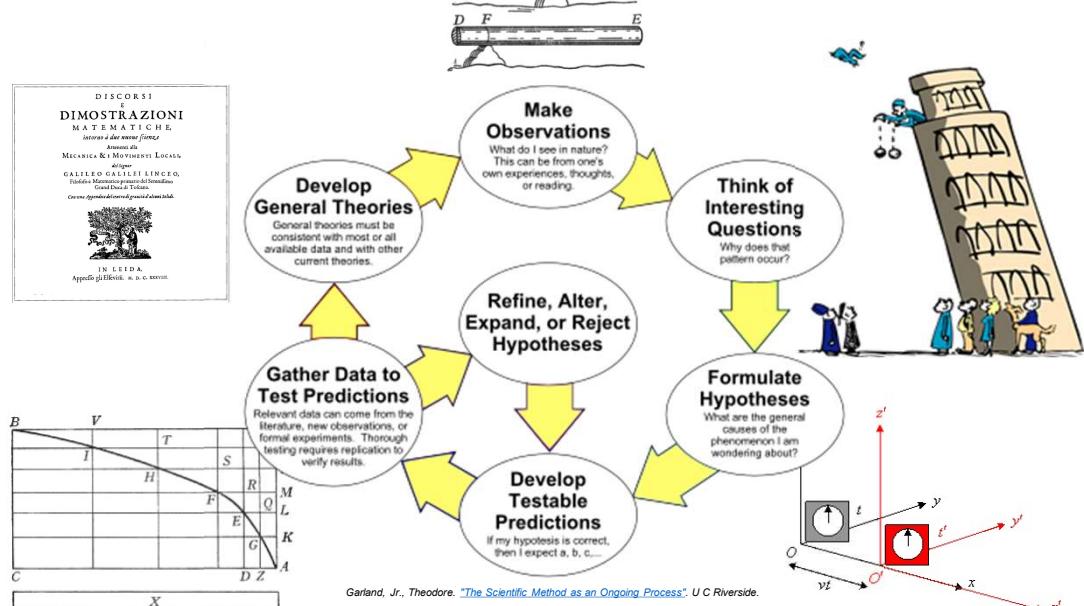
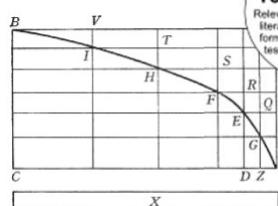


# Integrated Scientific Modeling and Lab Automation

Luca Cardelli, University of Oxford  
<http://www.biocompute.club/>, 2020-05-15

# Discovery through Observation

The Scientific Method ~ 1638



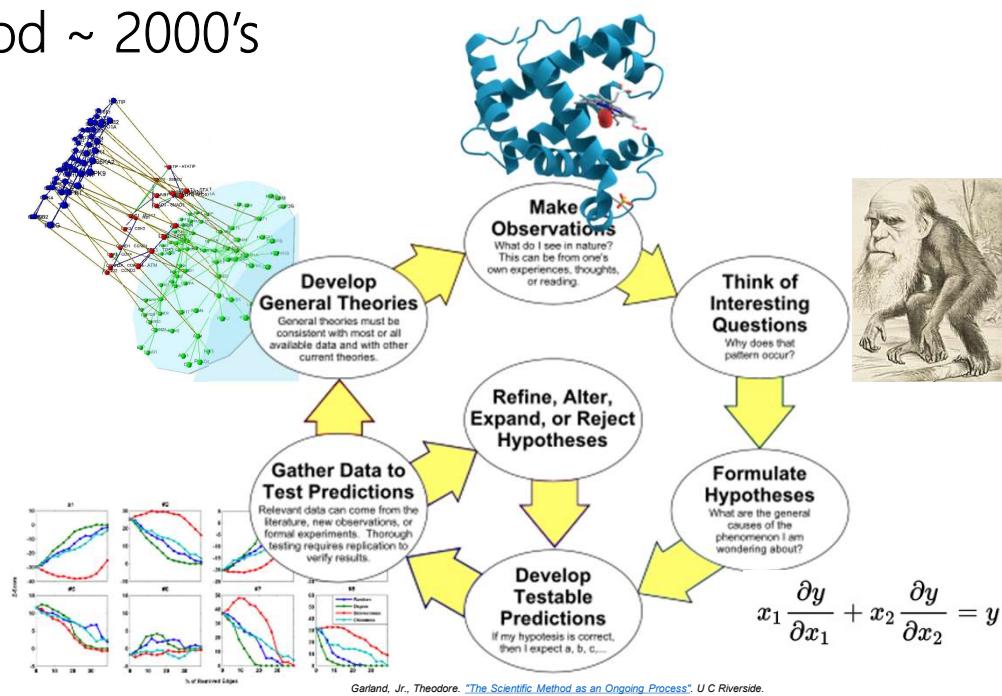
# Discovery through Collaboration

The Scientific Method ~ 2000's



1 protein = 30 people / 30 years

Humans have >250,000 proteins ☺



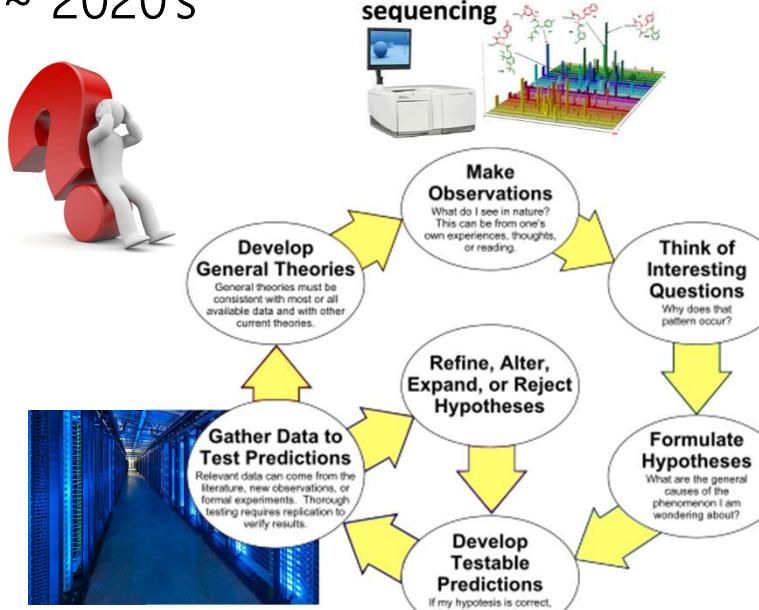
$$x_1 \frac{\partial y}{\partial x_1} + x_2 \frac{\partial y}{\partial x_2} = y$$

# Discovery through Automation

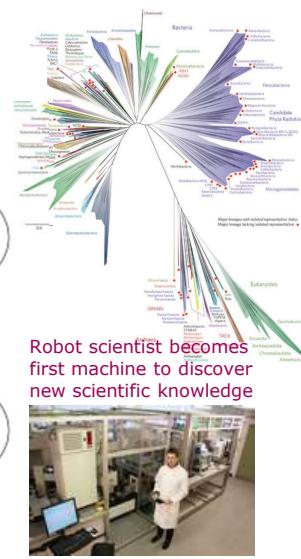
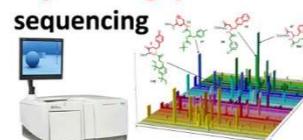
The Scientific Method ~ 2020's



```
while (true) {  
    predict();  
    falsify();  
}
```



High Throughput sequencing



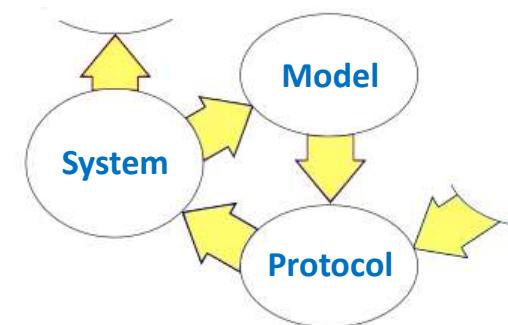
Robot scientist becomes  
first machine to discover  
new scientific knowledge

Ross King

Garland, Jr., Theodore. *"The Scientific Method as an Ongoing Process."* U C Riverside.

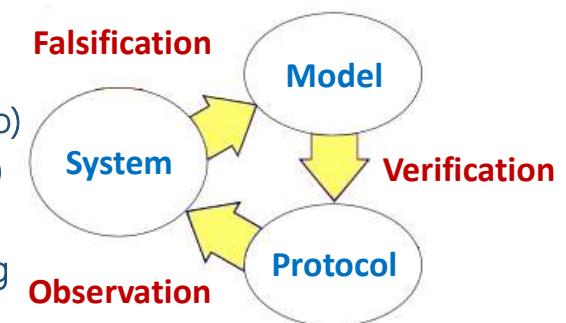
# The Inner Loop

- A *model* is refined by testing a (fixed) *protocols* against a *systems*
- A *protocol* is refined by testing a (fixed) *model* against a *systems*
- Today: publication does not accurately reflect execution
  - Model: poorly-maintained matlab script
  - Protocol: poorly-described manual steps in the lab
  - System: poorly-characterized and hardly "resettable"
  - ⇒ Crisis in biology: experiments are done once and are hard to reproduce  
<http://www.nature.com/news/reproducibility-1.17552>



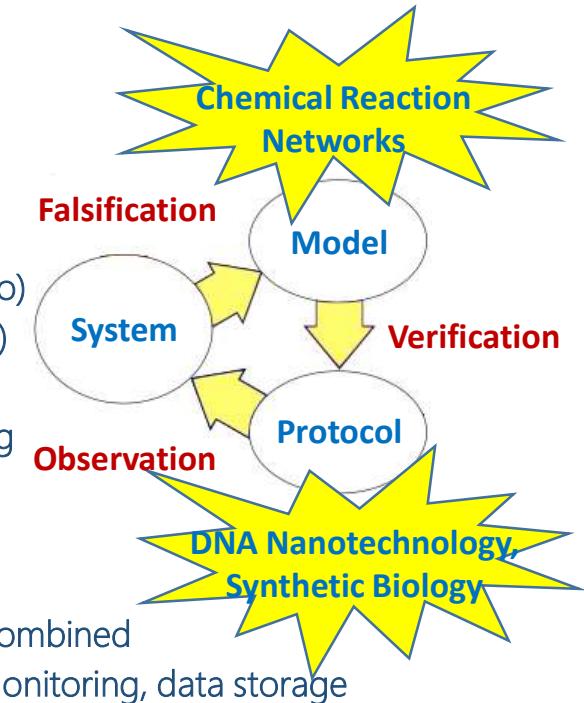
# The Inner Loop

- Tomorrow, automation
- |           |  |
|-----------|--|
| Nodes     | <ul style="list-style-type: none"><li>• Model: unambiguous (mathematical) description (CompBio)</li><li>• Protocol: standardized (engineered) parts and procedures (SynthBio)</li><li>• System: characterized (biological) organism and foundries (SysBio)</li></ul> |
| Arcs      | <ul style="list-style-type: none"><li>• Verification: simulation / analysis / model checking / theorem proving</li><li>• Observation: lab automation</li><li>• Falsification: statistical inference / model reduction</li></ul>                                      |
| Lifecycle | <ul style="list-style-type: none"><li>• Performance evaluation/optimization: of model+protocol+system combined</li><li>• Management: version control, equipment monitoring, data storage</li></ul>   |



# The Inner Loop

- Tomorrow, automation
  - Nodes • Model: unambiguous (mathematical) description (CompBio)
  - Protocol: standardized (engineered) parts and procedures (SynthBio)
  - System: characterized (biological) organism and foundries (SysBio)
- Arcs
  - Verification: simulation / analysis / model checking / theorem proving
  - Observation: lab automation
  - Falsification: statistical inference / model reduction
- Lifecycle
  - Performance evaluation/optimization: of model+protocol+system combined
  - Management: version control, equipment monitoring, data storage



# Why are *abstract* chemical reactions interesting?



- A fundamental model of kinetics in the natural sciences
- A fundamental mathematical structure, rediscovered in many forms
  - Vector Addition Systems, Petri Nets, Bounded Context-Free Languages, Population Protocols, ...
- A description of mechanism rather than just behavior
  - A way of describing and comparing biochemical algorithms
  - Enabling addition analysis techniques, e.g. evolution of mechanism through unchanging behavior
- A programming language (coded up in the genome) by which living things manage the processing of matter and information

# Also, a formal language we can implement with *real* (DNA) molecules

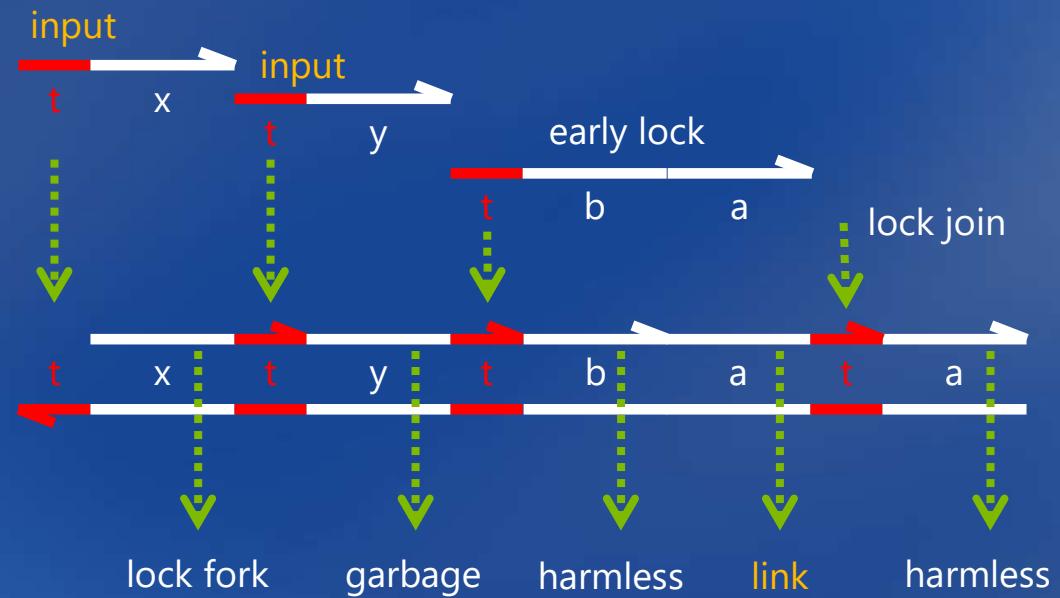
- ANY collection of abstract chemical reactions can be implemented with specially designed DNA molecules, with accurate kinetics (up to time scaling).
- A situation where we can "systematically compile" (synthesize) a model, run an (automated) protocol, and observe (sequence) the results in a closed loop.

## DNA as a universal substrate for chemical kinetics

David Soloveichik, Georg Seelig, and Erik Winfree  
PNAS March 23, 2010 107 (12) 5393-5398; <https://doi.org/10.1073/pnas.0909380107>

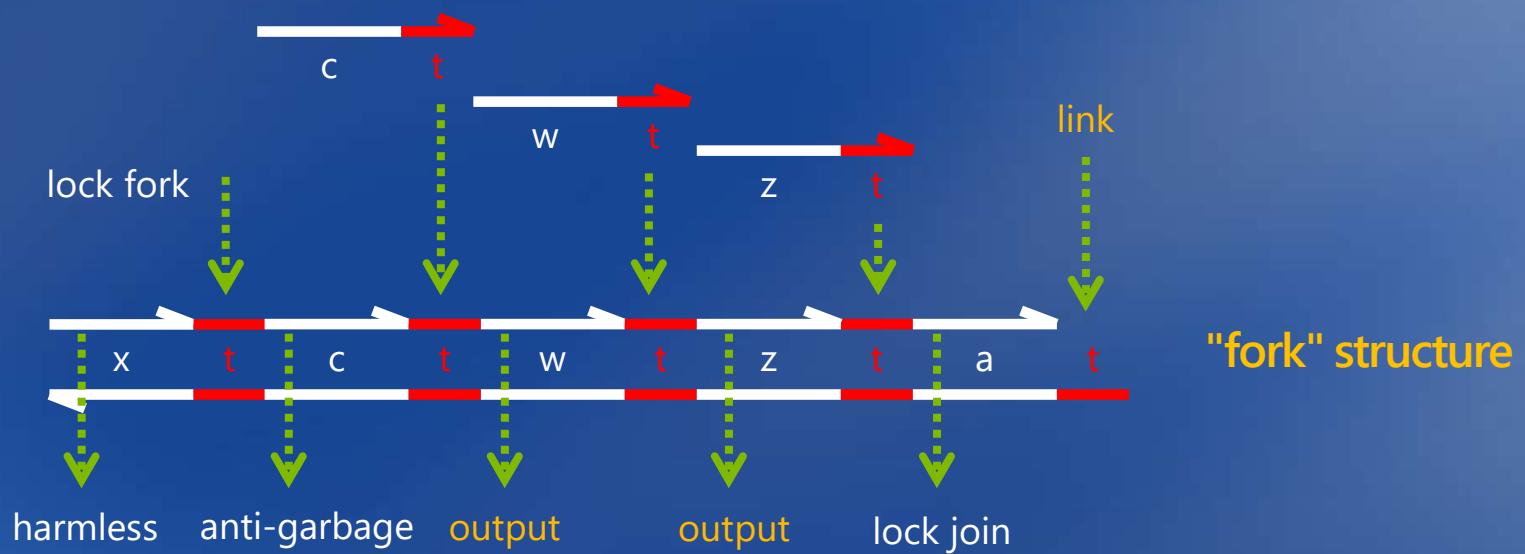
Reaction  $x + y \rightarrow z + w$

reactants  
half



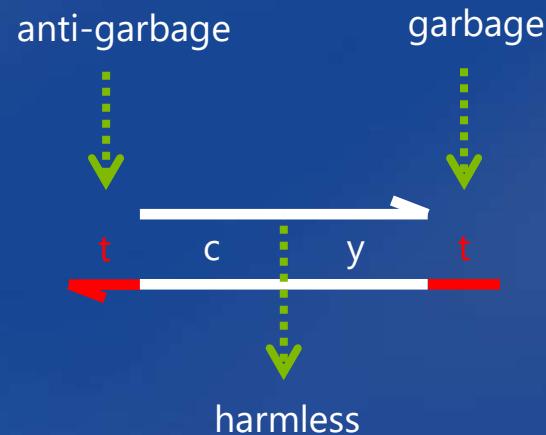
"join" structure

Reaction  $x + y \rightarrow z + w$  products half



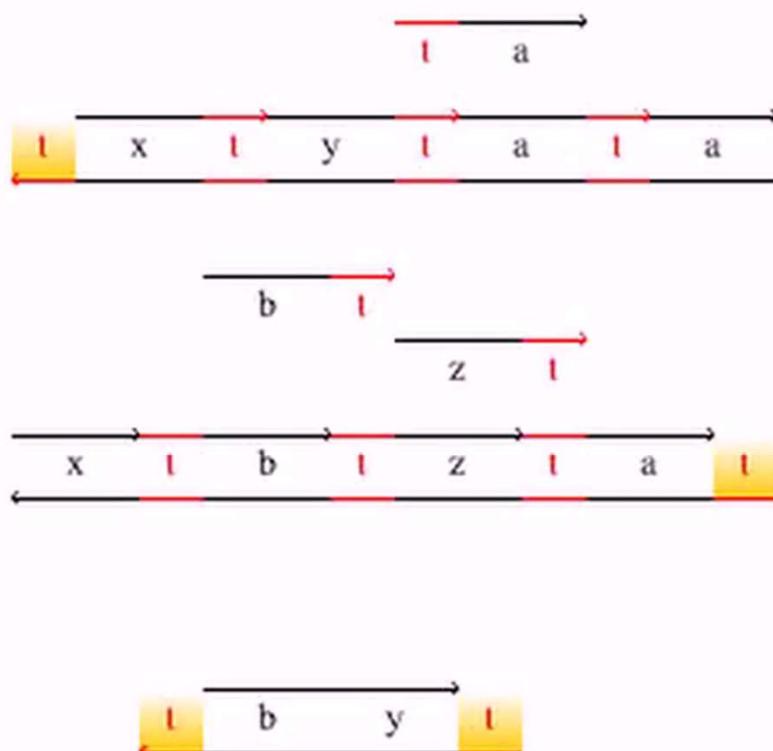
Reaction  $x + y \rightarrow z + w$

garbage  
collection

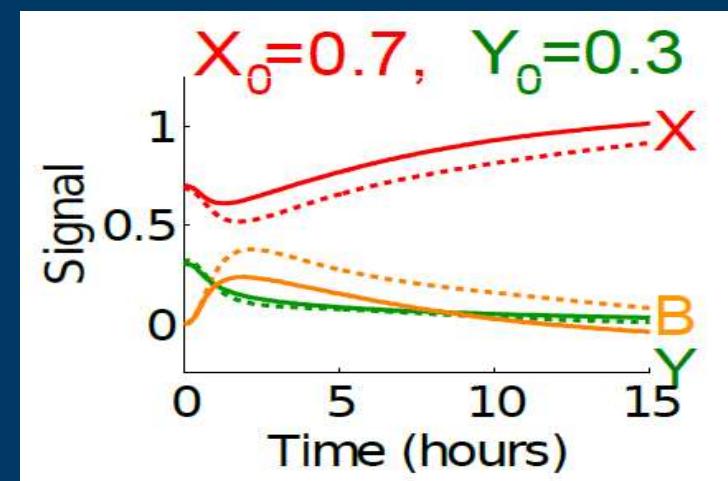
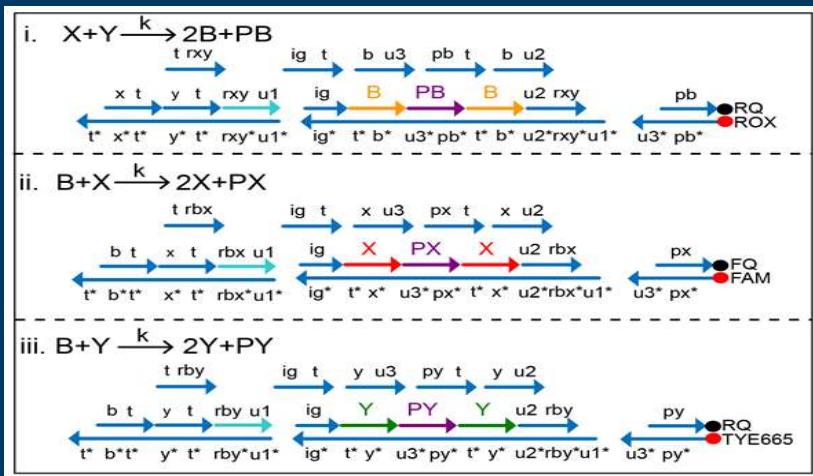


Powered by Sothink

Join  $x+y \rightarrow z$



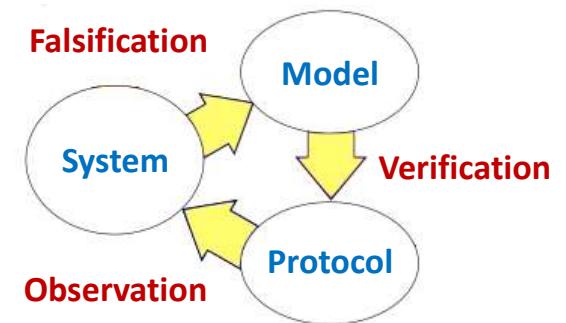
# DNA Implementation of the Approximate Majority Algoithm



# Experimental-Protocol Languages for Chemical Reaction Networks

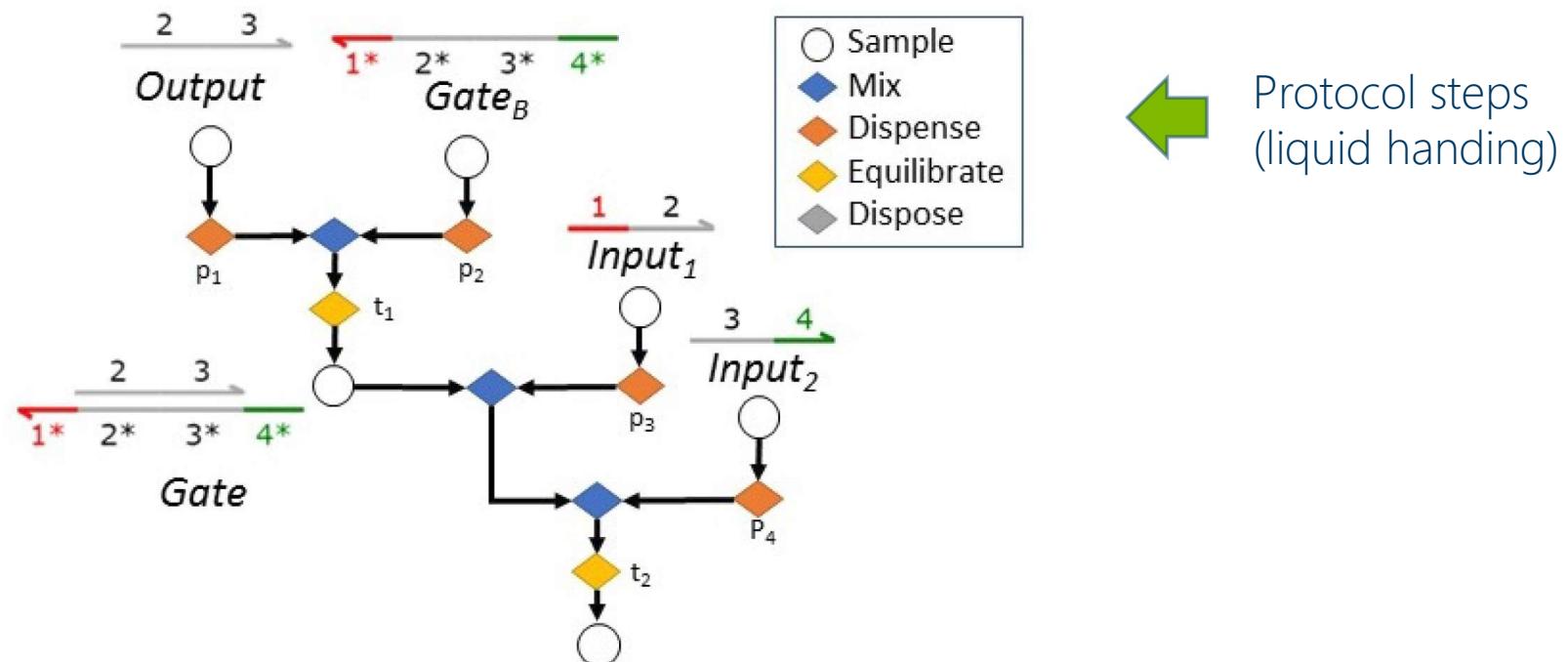
# Automating “the whole thing”

- Protocols: sets of steps to direct lab machinery (or people)
  - Published (possibly) in specialized journals. With varying accuracy.
- Models: sets of equations to predict the results of lab experiments
  - Published (possibly) in Auxiliary Online Materials. With lots of typos.
- Protocols know nothing about models
  - What hypothesis is the protocol trying to test? It is not written in the protocol.
- Models know nothing about protocols
  - What lab conditions are being used to test the model? It is not written in the model.
- While presumably talking about the same system
  - Through the experiment.
- Reproducibility crisis
  - Experiments are hard to reproduce.
  - Even models are hard to reproduce!
- Similar to a classical problem in C.S.
  - Documentation (model) gets out of step from code (protocol) if their integration is not automated.



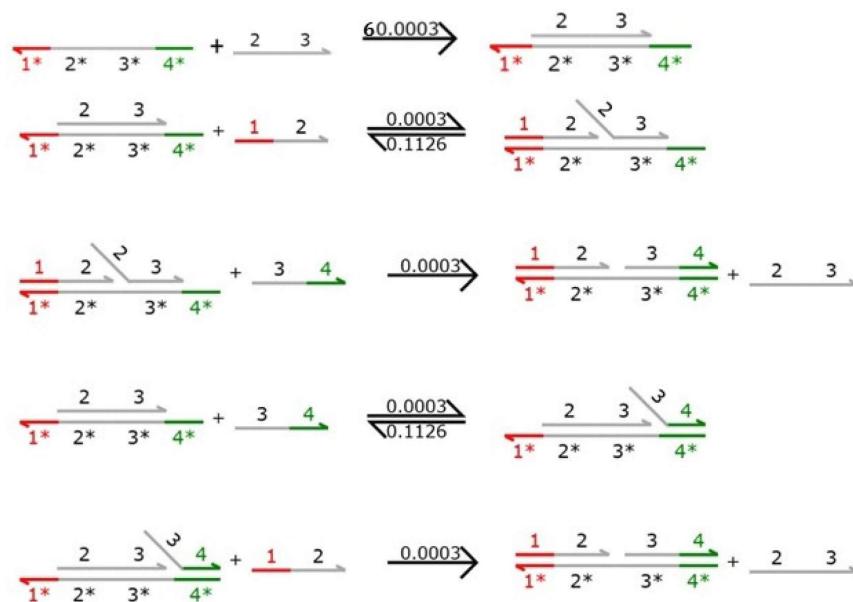
# A Protocol

For DNA gate assembly and activation in vitro



# A Model

A Chemical Reaction Network, provided explicitly or (in this case) generated from a higher-level description of the initial strands, according to the DNA strand displacement rules



# An Integrated Description

This requires a language

$$\mathcal{C} = (\mathcal{A}, \mathcal{R})$$

$$P =$$

$x$  (*sample variable*)

$(x_0, V, T)$  (*initial condition*)

$Mix(P_1, P_2)$  (*mix samples*)

$let x = P_1 in P_2$  (*define variable*)

$let x, y = Dispense(P_1, p) in P_2$  (*dispense samples*)

$Equilibrate(P, t)$  (*let time pass*)

$Dispose(P)$  (*discard P*)

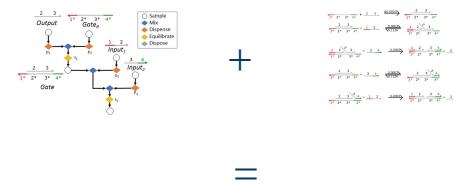
Experimental Biological Protocols with Formal Semantics

Alessandro Abate<sup>2</sup>, Luca Cardelli<sup>1,2</sup>, Marta Kwiatkowska<sup>2</sup>, Luca Laurenti<sup>2</sup>, and Boyan Yordanov<sup>1</sup>

<sup>1</sup> Microsoft Research Cambridge

<sup>2</sup> Department of Computer Science, University of Oxford

The CRN can be computed from  $\{Input_1, Input_2, Output, Gate\}$ , and its initial conditions and evolution are determined by the protocol steps.



$Input_1 = < 1^* 2 >$     $Output = < 2 3 >$

$Input_2 = < 3 4^* >$     $Gate = \{1^*\}[2 3]\{4^*\}$

$P_1 = let In1 = ((Input1, 100.0nM), 0.1mL, 25.0^\circ C) in$   
 $let In2 = ((Input2, 100.0nM), 0.1mL, 25.0^\circ C) in$   
 $let GA = ((Output, 100.0nM), 0.1mL, 25.0^\circ C) in$   
 $let GB = ((Gate_B, 100.0nM), 0.1mL, 25.0^\circ C) in$   
 $let sGA,_= Dispense(GA, p_1) in$   
 $let sGB,_= Dispense(GB, p_2) in$   
 $let sIn1,_= Dispense(In1, p_3) in$   
 $let sIn2,_= Dispense(In2, p_4) in$   
 $Observe(Equilibrate(Mix(Mix(Equilibrate($   
 $Mix(sGA, sGB), t_1), sIn1), sIn2), t_2), idn).$

# Language Semantics (deterministic)

The deterministic case is a warm-up exercise, but simple to explain

Each program denotes a final state <concentrations, volume, temperature>

$\llbracket P \rrbracket^\rho$  is the final state produced by a protocol  $P$  for a fixed CRN  $\mathcal{C} = (\mathcal{A}, \mathcal{R})$ :

$$\llbracket x \rrbracket^\rho = \rho(x)$$

$$\llbracket x_0, V, T \rrbracket^\rho = (x_0, V, T)$$

$$\llbracket Mix(P_1, P_2) \rrbracket^\rho =$$

$$\text{let } (x_0^1, V_1, T_1) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } (x_0^2, V_2, T_2) = \llbracket P_2 \rrbracket^\rho$$

$$\left( \frac{x_0^1 V_1 + x_0^2 V_2}{V_1 + V_2}, V_1 + V_2, \frac{T_1 V_1 + T_2 V_2}{V_1 + V_2} \right)$$

$$\llbracket let x = P_1 \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho\{x \leftarrow (x_0, V, T)\}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

$$\llbracket let x, y = Dispense(P_1, p) \text{ in } P_2 \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P_1 \rrbracket^\rho$$

$$\text{let } \rho_1 = \rho\{x \leftarrow (x_0, V \cdot p, T), y \leftarrow (x_0, V \cdot (1 - p), T)\}$$

$$\llbracket P_2 \rrbracket^{\rho_1}$$

$$\llbracket Equilibrate(P, t) \rrbracket^\rho =$$

$$\text{let } (x_0, V, T) = \llbracket P \rrbracket^\rho$$

$$\llbracket (\mathcal{A}, \mathcal{R}, x_0), V, T \rrbracket (H)(t)$$

$$\llbracket Dispose(P) \rrbracket^\rho = (0^{|\mathcal{A}|}, 0, 0),$$

State produced by CRN  $\mathcal{C} = (\mathcal{A}, \mathcal{R})$  at time t:

$$\llbracket ((\mathcal{A}, \mathcal{R}, x_0), V, T) \rrbracket (H)(t) =$$

$$\text{let } G : [0 \dots H] \rightarrow \mathbb{R}^{|\mathcal{A}|} \text{ be the solution of } G(t') = x_0 + \int_0^{t'} F(V, T)(G(s))ds \\ (G(t), V, T)$$

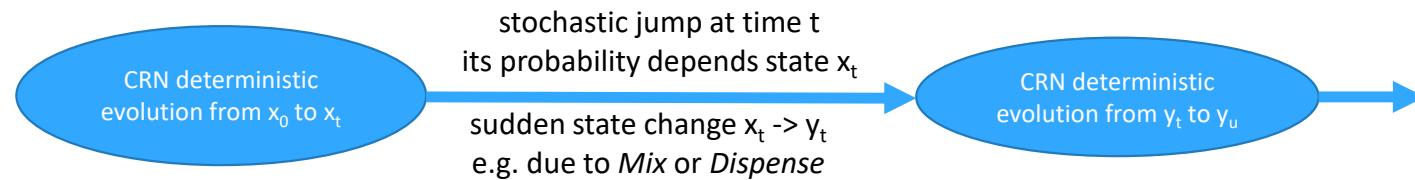
# Language Semantics (stochastic)

*Dispense* has a volume uncertainty.

*Equilibrate* has a time uncertainty.

Reactions have rate uncertainty and/or intrinsic molecular noise.

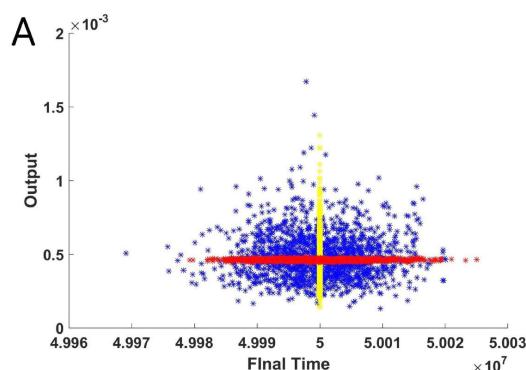
**Each program now represents a Hybrid System with stochastic jumps between deterministic evolutions:**



Which in turn denotes a **Piecewise Deterministic Markov Process (PDMP)**

# Stochastic Analysis

- We can ask: what is the probability of a certain outcome given uncertainties in *both the protocol and the model*?
- Conversely: which parameters of *both the protocol and the model* best fit the observed result?



1500 executions including protocol uncertainty due timing and pipetting errors (red).

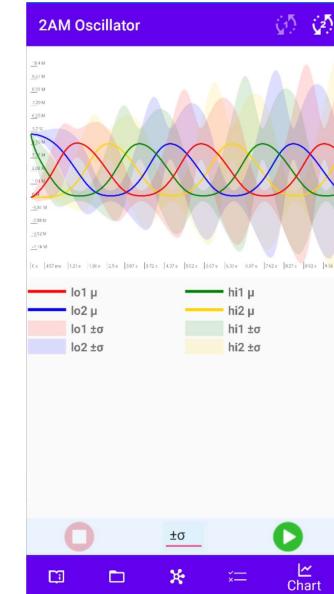
1500 executions including only model uncertainty about rates of the CRN (yellow).

1500 executions including both sources of uncertainty (blue).

We may estimate by Statistic Model Checking, e.g. the probability that Output will fall in a certain range, given distributions over uncertain model and protocol parameters.

# Kaemika

- A prototype language for chemical models & protocols
- <http://lucacardelli.name/kaemika.html>
- Search "Kaemika" in the App stores



- CRN simulation
- Microfluidics simulation
- Reaction graphs
- ODE equations
- Stochastic noise (LNA)

# Describing a Model

- *Species and reactions*
  - Characterized by initial values and rates
- *Kinetics*
  - Deterministic (ODE) or stochastic (LNA)
- “*Samples*” (*compartments*) and *Protocols*
  - Isolate species and reactions in a compartment, and mix compartments
- *Programming abstractions*
  - Assemble models as compositions of modules

# Species and Reactions

```
//=====
// Lotka 1920, Volterra 1926
// (simplified with all rates = 1)
//=====

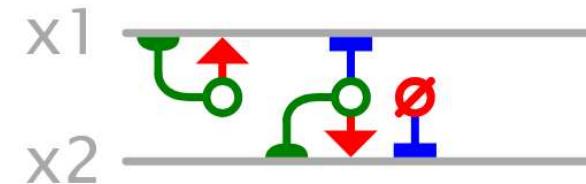
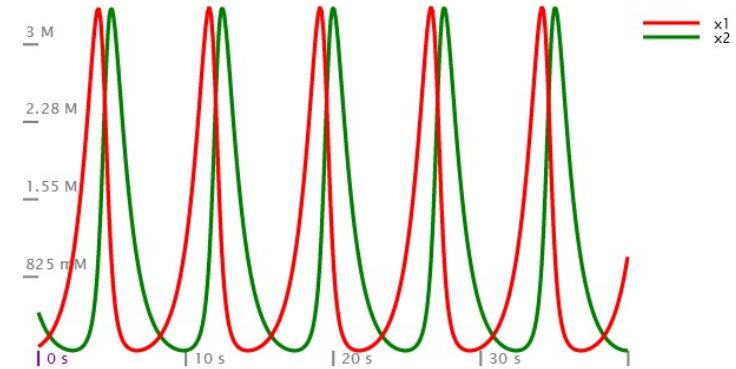
number x1_0 <- uniform(0,1) // random x1_0
number x2_0 <- uniform(0,1) // random x2_0

species x1 @ x1_0 M      // prey
species x2 @ x2_0 M      // predator

x1 -> x1 + x1    {1} // prey reproduces
x1 + x2 -> x2 + x2    {1} // predator eats prey
x2 -> Ø           {1} // predator dies

equilibrate for 40
```

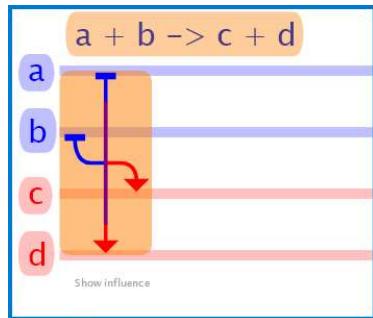
UNDAMPED OSCILLATIONS, ETC. 1595  
UNDAMPED OSCILLATIONS DERIVED FROM THE LAW OF MASS ACTION.  
BY ALFRED J. LOTKA.  
Received June 2, 1920.



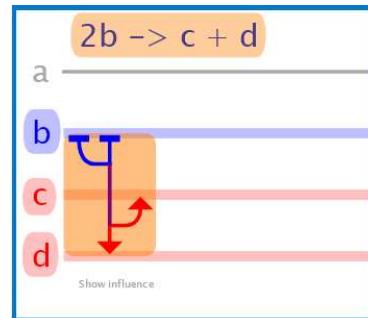
# Reaction scores (graphical representation of reaction networks)

Horizontal lines: *species*. Vertical stripes: *reactions*.      Blue: reagents. Red: products. Green: catalysts.

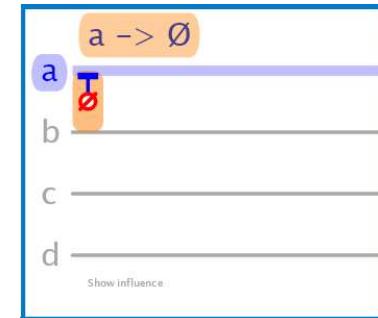
Reactants and products



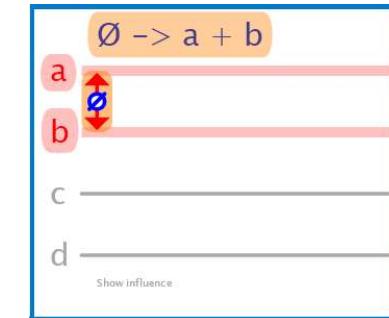
Repeated species



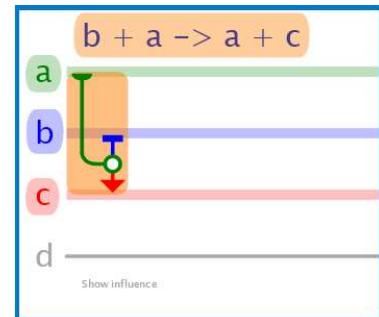
Reactants but no products



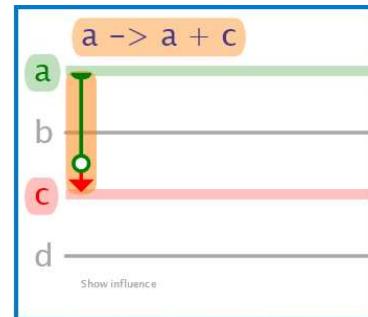
Products but no reactants



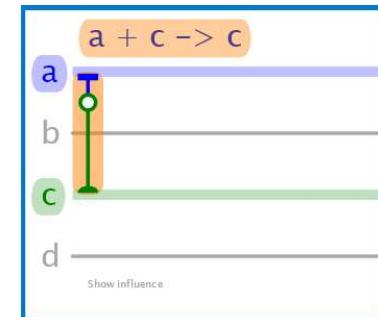
Catalyst



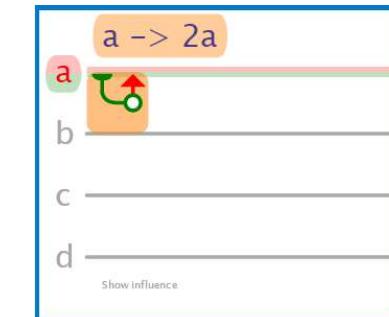
Catalyst but no reactants



Catalyst but no products



Autocatalyst



# Writing Models Compositionally

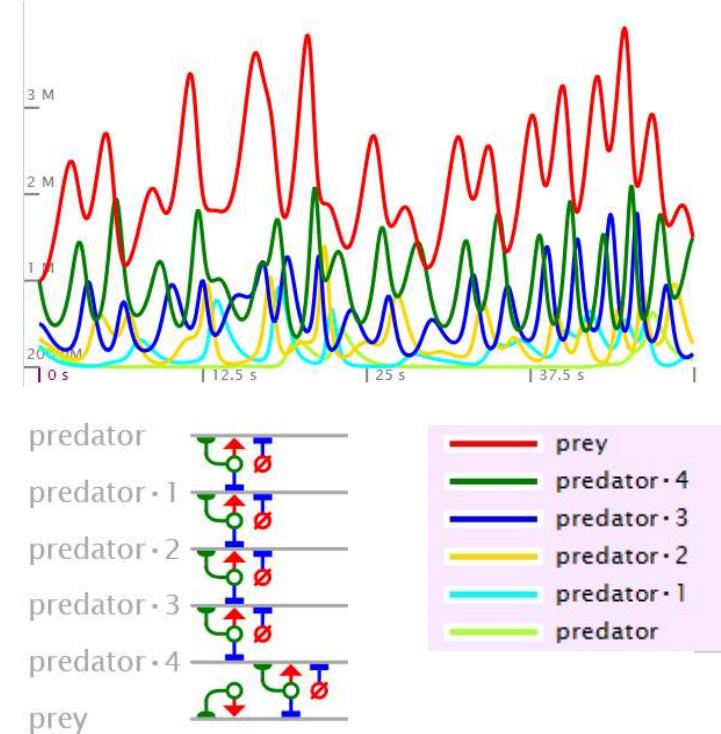
- Functional-monadic approach
  - *Functions* take *data* as parameters and produce *data* as results
  - *Networks* take *data* as parameters and produce *effects* as results
  - *Data* is *numbers*, *species*, *functions*, *networks*, *flows*, etc.
  - *Effects* are *species creation*, *reaction definitions*, and *sample handling*
  - A program execution produces both a final *result* and a sequence of *effects*
- (Temporal) Flows
  - Flows are functions of time (mostly real-valued)
  - Can be assembled programmatically (as a data structure)
  - Can be used as *rates* (leading to programmable kinetics)
  - Can be *observed* at specific times (leading to protocol observations)
  - Can be *plotted* over time (leading to chart series and legends)

# Ex: Predatorial

```
function Predatorial(number n) {
    if n = 0 then
        define species prey @ 1 M
        prey -> 2 prey // prey reproduces
        report prey
        yield prey
    else
        define species predator @ 1/n M
        species prey = Predatorial(n-1)
        prey + predator ->{n} 2 predator // predator eats
        predator -> Ø // predator dies
        report predator
        yield predator
    end
}

species apexPredator = Predatorial(5)
equilibrate for 50
```

```
=====
// Creates a stack of predator-prey
// relationships in Lotka-Volterra style,
// and returns the apex predator.
=====
```



# Describing a Protocol

- *Samples* (e.g. test tubes)
  - Are characterized by a volume and a temperature
  - Contain a specified set of species
  - Evolve according to reactions that operates on those species
- *Protocol Operations* (e.g. liquid handling)
  - Accept and produce samples
  - Accepted samples are *used up* (they can only be operated-on once)

# Samples

- Samples contain concentrations of species, acted over by reactions.
- Each sample has a fixed volume and a fixed temperature through its evolution.
- Sample concentrations are in units of molarity M = mol/L.
- The default implicit sample is called the vessel {1 mL, 20 C}

```
species {c} // a species for multiple samples

sample A {1µL, 20C}      // volume and temperature
species a @ 10mM in A    // species local to A
amount c @ 1mM in A      // amount of c in A
a + c -> a + a

sample B {1µL, 20C}
species b @ 10mM in B    // species local to B
amount c @ 1mM in B      // amount of c in B
b + c -> c + c
```

An amount can also be given in grams (if molar mass is specified). The resulting concentration is then relative to sample volume.

```
species {NaCl#58.44}
```

```
sample C {1mL, 20C}
amount NaCl @ 8g in C
```

Reactions can be specified with Arrhenius parameters {collision frequency, activation energy}. The reaction kinetics is then relative to sample temperature T.

```
a + c ->{2, 5} a + a
// rate is 2*e^(-5/(R*T))
```

# Liquid Handling

Mix two samples into one

```
mix A = B, C
```

Split a sample into two

```
split B,C = A by 0.5
```

Let a sample evolve by its reactions

```
equilibrate A = B for 3
```

Throw away a sample

```
dispose C
```

Change sample temperature (heat or cool)

```
regulate A = B to 37C
```

Change sample volume (concentrate or dilute)

```
concentrate A = B to 1mL
```

Experimental Biological Protocols with Formal Semantics

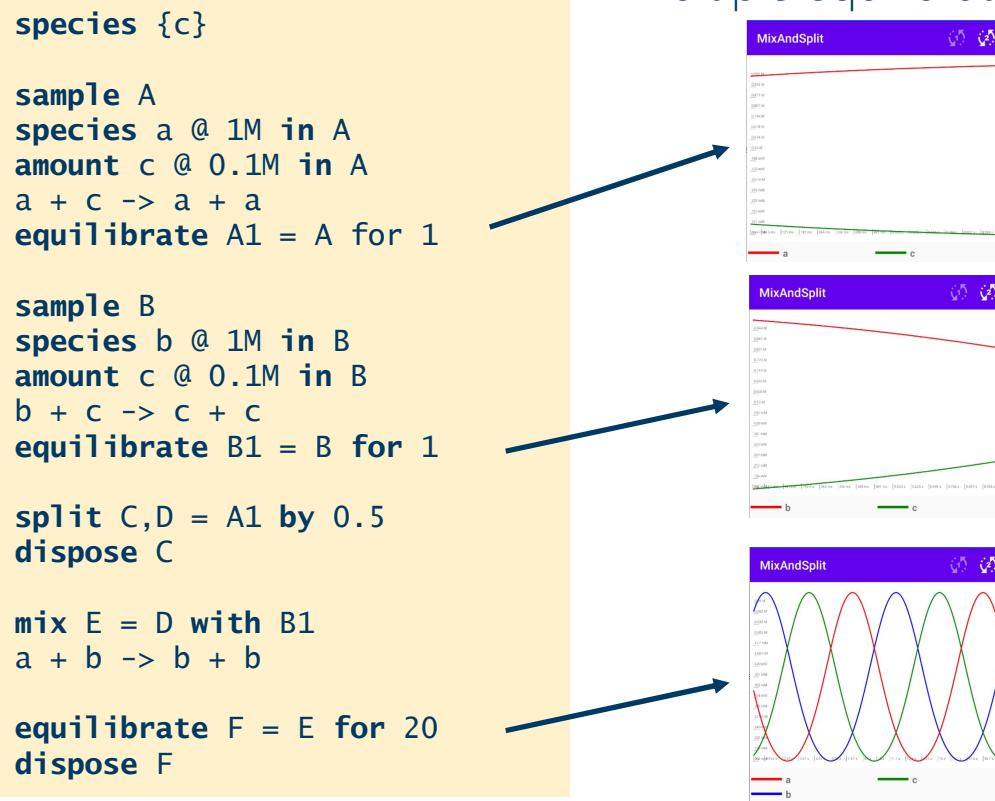
Alessandro Abate<sup>2</sup>, Luca Cardelli<sup>1,2</sup>, Marta Kwiatkowska<sup>2</sup>, Luca Laurenti<sup>2</sup>, and Boyan Yordanov<sup>1</sup>

<sup>1</sup> Microsoft Research Cambridge

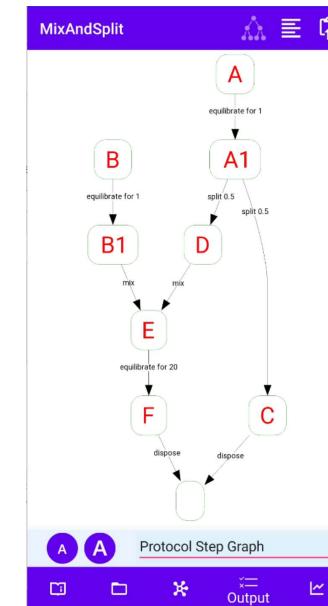
<sup>2</sup> Department of Computer Science, University of Oxford

# Ex: Sample Manipulation

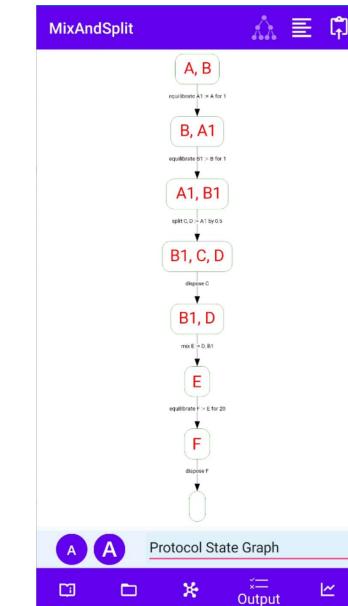
Multiple equilibration steps



"Protocol step graph"



"Protocol state graph"



PDMP ("System Equations")

# Ex: Phosphate-buffered saline (PBS)

```
species {NaCl#58.44, KCl#74.5513, NA2HP04#141.96, KH2P04#136.086}
report NaCl, KCl, NA2HP04, KH2P04

function Autoclave(sample PBS, number t) {
    define
        // increase temperature, preserve volume:
        regulate hot = PBS to 121C
        // bake
        equilibrate hot for t
        // decrease temperature, preserve volume:
        regulate PBS = hot to 20C
    yield PBS
}

function MakePBS() {
    define
        sample PBS {800mL, 20C}
        amount NaCl @ 8g in PBS
        amount KCl @ 0.2g in PBS
        amount NA2HP04 @ 1.44g in PBS
        amount KH2P04 @ 0.24g in PBS

        sample topup {200mL, 20C}
        mix PBS = PBS,topup
    yield Autoclave(PBS, 20*60)
}

sample PBS = MakePBS()
```

 Cold Spring Harbor Protocols

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 Recipe

**Phosphate-buffered saline (PBS)**

Reagent	Amount to add (for concentration solution)	Final (1×)	Amount to add (for 10× stock)	Final concentration (10×)
NaCl	8 g	137 mM	80 g	1.37 M
KCl	0.2 g	2.7 mM	2 g	27 mM
Na <sub>2</sub> HPO <sub>4</sub>	1.44 g	10 mM	14.4 g	100 mM
KH <sub>2</sub> PO <sub>4</sub>	0.24 g	1.8 mM	2.4 g	18 mM

If necessary, PBS may be supplemented with the following:

CaCl <sub>2</sub> ·2H <sub>2</sub> O	0.133 g	1 mM	1.33 g	10 mM
MgCl <sub>2</sub> ·6H <sub>2</sub> O	0.10 g	0.5 mM	1.0 g	5 mM

PBS can be made as a 1× solution or as a 10× stock. To prepare 1 L of either 1× or 10× PBS, dissolve the reagents listed above in 800 mL of H<sub>2</sub>O. Adjust the pH to 7.4 (or 7.2, if required) with HCl, and then add H<sub>2</sub>O to 1 L. Dispense the solution into aliquots and sterilize them by autoclaving for 20 min at 15 psi (1.05 kg/cm<sup>2</sup>) on liquid cycle or by filter sterilization. Store PBS at room temperature.

<http://cshprotocols.cshlp.org/content/2006/1/pdb.rec8247>

# Ex: Serial Dilution

```
network SerialDilution(number count, sample s, network f) {
    if count > 0 then
        sample solvent {9*observe(volume,s) L, observe(kelvin,s) K}
        mix s = s, solvent
        split s, dilution = s by 0.1, 0.9
        f(dilution)
        SerialDilution(count-1, s, f)
    end
}

initial sample to be diluted:

sample init {1mL, 25C}
species A @ 1M in init
species B @ 1M in init
A + B ->{20} A
A -> Ø

apply this network to each dilution;
note that this invokes a simulation
each time in each solution

network test(sample s) {
    equilibrate s for 10
    dispose s
}

dilute 4 times

SerialDilution(4, init, test)
```

Prepare a series of increasingly diluted solutions and apply a network  $f$  to each ( $f$  can add species and reactions to the solutions)

## RESULT:

```
sample init {1mL, 298.2K} {A = 1M, B = 1M}
sample s2 {1mL, 298.2K} {A = 100mM, B = 100mM}
sample s4 {1mL, 298.2K} {A = 10mM, B = 10mM}
sample s7 {1mL, 298.2K} {A = 1mM, B = 1mM}
sample s10 {1mL, 298.2K} {A = 100uM, B = 100uM}
```

# Extracting the Model and the Protocol

From the script

```
species {c}

sample A
species a @ 1M in A
amount c @ 0.1M in A
a + c -> a + a
equilibrate A1 = A for 1

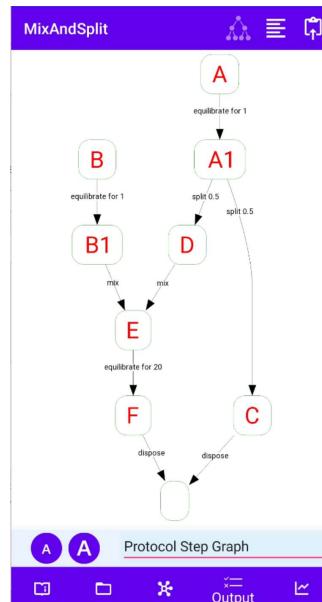
sample B
species b @ 1M in B
amount c @ 0.1M in B
b + c -> c + c
equilibrate B1 = B for 1

split C,D = A1 by 0.5
dispose C

mix E = D with B1
a + b -> b + b

equilibrate F = E for 20
dispose F
```

The protocol



The (final) model (sample E)

```
STATE_5
sample E {1.5mL, 293.2K} {
    a = 354.5mM
    c = 178mM
    b = 0.5674M
    consumed
    a + c -> a + a
    b + c -> c + c
    a + b -> b + b
}

KINETICS for STATE_5 (sample E) for 20 time units:
da = a * c - a * b
dc = c * b - a * c
db = a * b - c * b
```

# Extracting the Hybrid Transition System

## From the script

```

species {c}
sample A
species a @ 1M in A
amount c @ 0.1M in A
a + c -> a + a
equilibrate A1 = A for 1

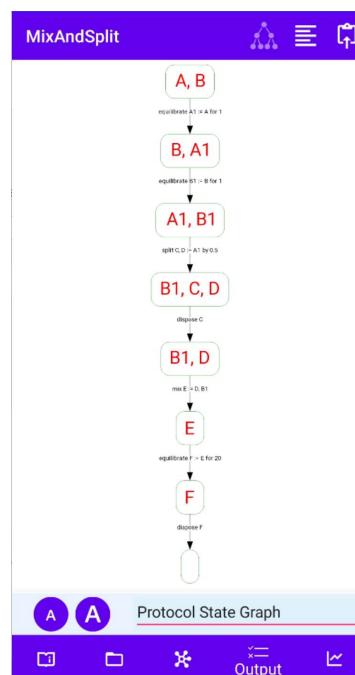
sample B
species b @ 1M in B
amount c @ 0.1M in B
b + c -> c + c
equilibrate B1 = B for 1

split C,D = A1 by 0.5
dispose C

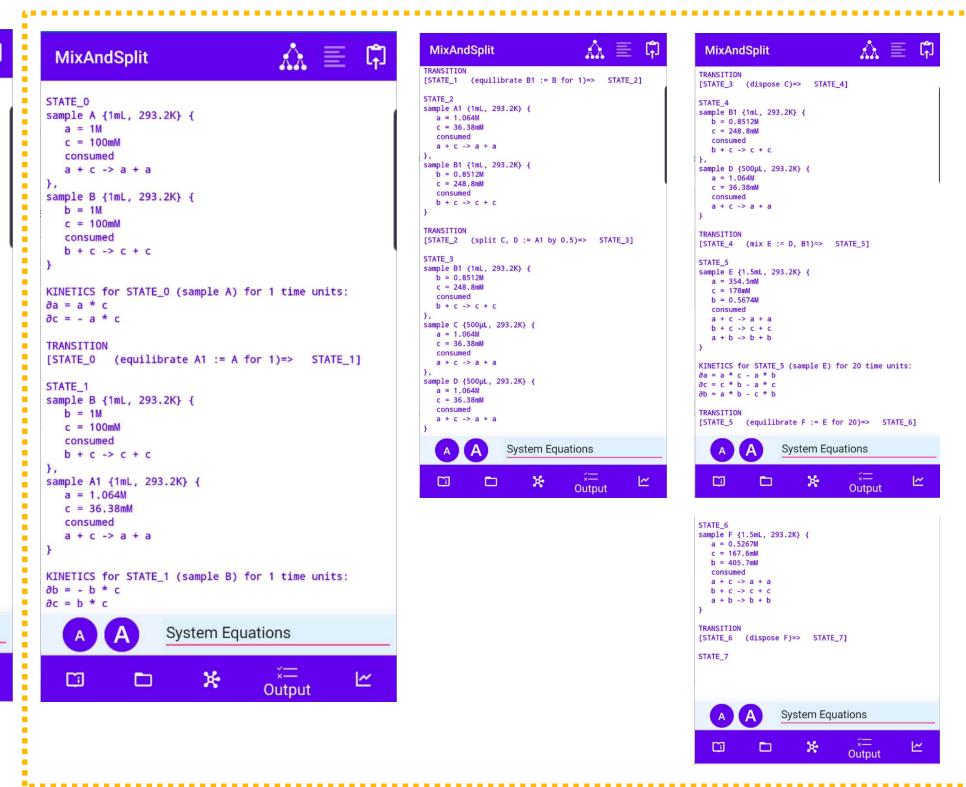
mix E = D with B1
a + b -> b + b

equilibrate F = E for 20
dispose F

```



## The full story (Hybrid system)



## Executing the protocols

- We have seen that *reactions can be executed* by DNA
- But how can we *execute the protocols*, so that we can execute the whole thing together?
- -> Digital Microfluidics Compiler

# Digital Microfluidics

- <https://www.youtube.com/watch?v=ncfZWqPm7-4>



Speed test

[https://www.youtube.com/watch?v=pSl9L\\_h3Q0](https://www.youtube.com/watch?v=pSl9L_h3Q0)



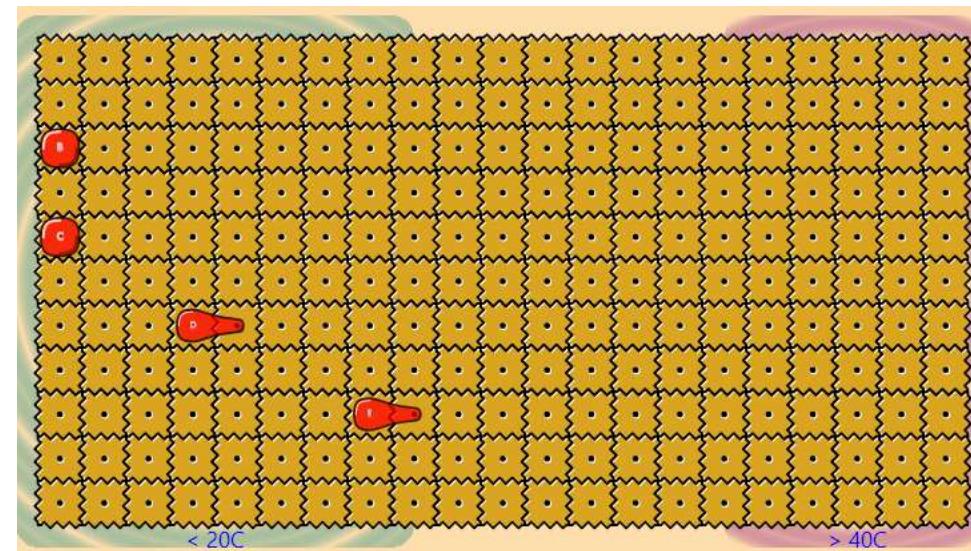
# Digital Microfluidics

- A general, *programmable*, platform to execute the main liquid-handling operations
- To close the cycle, it can support many automated observation techniques on-board or off-board via peripheral pumps (sequencing, mass spec, ...) although these are all very hardware-dependent.

# Digital Microfluidics Compiler

- Mix, split, equilibrate, dispose
- Automatic routing – no geometrical information
- Hot/cold zones

```
sample A {3µL, 20C}  
split B,C,D,E = A  
mix F = E,C,B,D  
dispose F
```



# Other features

- Timeflows
  - General kinetic rates (fractions, rational powers, exponentials, trigonometry) work with both deterministic and stochastic simulation and equation-extraction
  - Programmable plot reports (e.g.  $\text{var}(2*a - 3*b)$ )
  - Capture timeflow outputs to combine (e.g. avg) and re-plot/export them later
- Mass action compiler
  - Turn *any* elementary ODE system (with fractions, rational powers, exponentials, trigonometry) into an equivalent system of pure mass action reactions.
- Programmable random numbers and distributions
  - As in the Omega probabilistic language, with rejection sampling.

# Conclusions

## Bridging culture gaps

We can have more sophisticated modeling languages than chemical reactions  
And we can have more sophisticated protocols than liquid handling  
But it is good to find an intersection where we can get them into an automated loop

## Chemical reaction networks

An interface between engineering (algorithms, programming, verification)  
and science (dynamical and stochastic systems in nature, laboratory protocols)

## Closed-loop models and protocols

Unified description of the scientific cycle

## Automation (programmability)

Generating networks of parametric size and complexity  
Scripting protocols