How the Cell Cycle Computes

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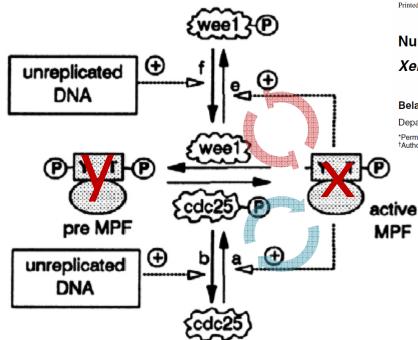
Outline

Analyzing molecular networks

- Various biochemical/bioinformatic techniques can tell us something about network structures.
- We try do discover the function of the network, or to verify hypotheses about its function.
- We try to understand how the structure is dictated by the function and other natural constraints.
- The Cell-Cycle Switches and Oscillators
 - Some of the best studied molecular networks.
 - Important because of their fundamental function (cell division) and preservation across evolution.

The Cell Cycle Switch

At the core of the cell-cycled oscillator.
 This network is universal in all Eukaryotes [P. Nurse].



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Numerical analysis of a comprehensive model of M-phase control in *Xenopus* oocyte extracts and intact embryos

Bela Novak* and John J. Tyson[†]

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- Double positive feedback on x
- Double negative feedback on x
- No feedback on y
- What on earth ... ???

• Well studied. But *why this structure?*

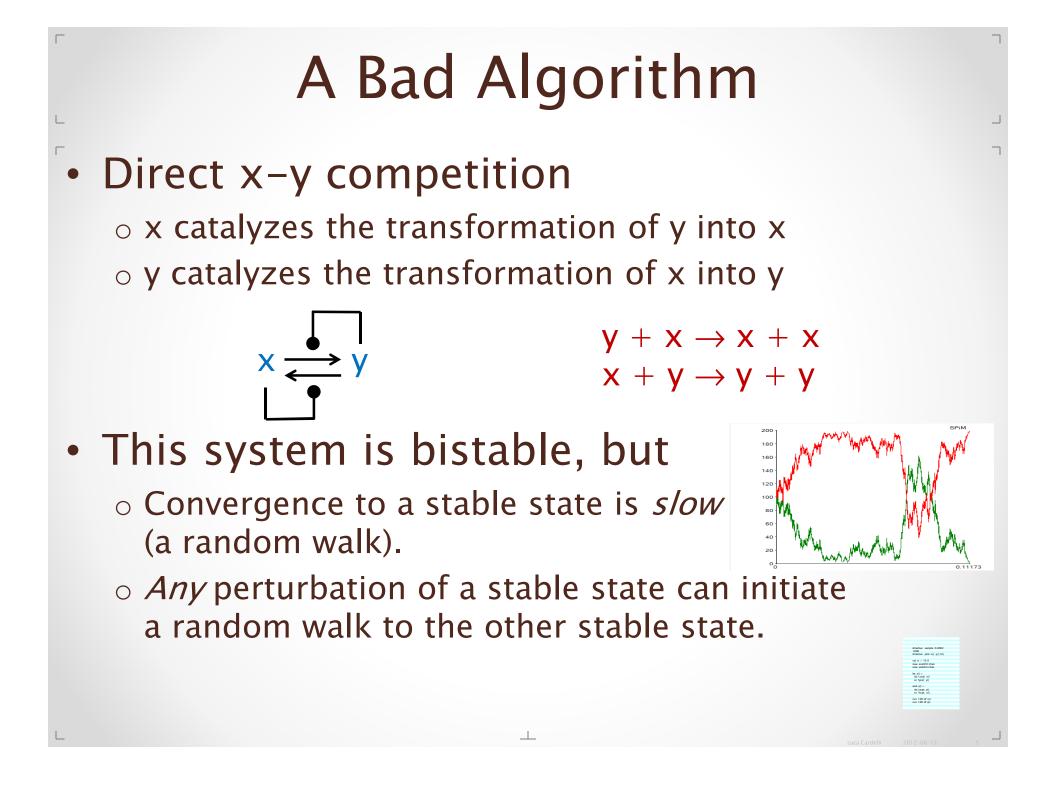
How to Build a Switch

• What is a "good" switch?

- We need first a *bistable* system: one that has two *distinct* and *stable* states. I.e., given *any* initial state the system must *settle* into one of two states.
- The settling must be *fast* (not get stuck in the middle for too long) and *robust* (must not spontaneously switch back).
- Finally, we need to be able to *flip* the switch: drive the transitions by external inputs.

"Population" Switches

- Populations of identical agents (molecules) that switch from one state to another *as a whole*.
- Highly concurrent (stochastic).



A Very Good Algorithm

Approximate Majority

Decide which of two populations is in majority

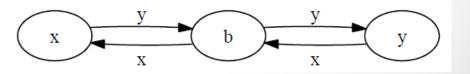
A fundamental 'population protocol'

- Agents in a population start in state x or state y.
- A pair of agents is chosen randomly at each step, they interact ("collide") and change state.
- The whole population must eventually agree on a majority value (all x or all y) with probability 1.

Dana Angluin · James Aspnes · David Eisenstat

A Simple Population Protocol for Fast Robust Approximate Majority

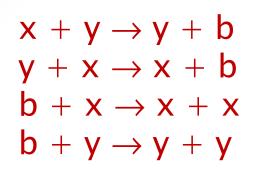
We analyze the behavior of the following population protocol with states $Q = \{b, x, y\}$. The state b is the **blank** state. Row labels give the initiator's state and column labels the responder's state.

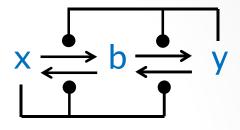


Third 'undecided' state.

Chemical Implementation

A programming language for population algorithms!





Worse case test: start with x=y.

Bistable

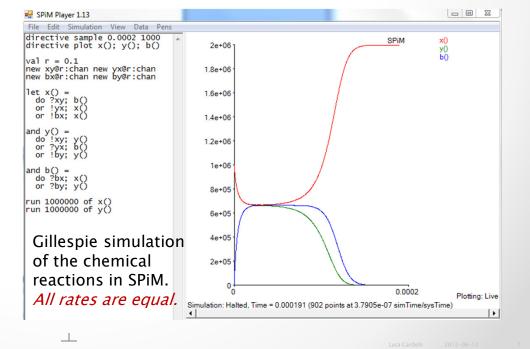
Even when x=y! (stochastically)

Fast

O(log n) convergence time

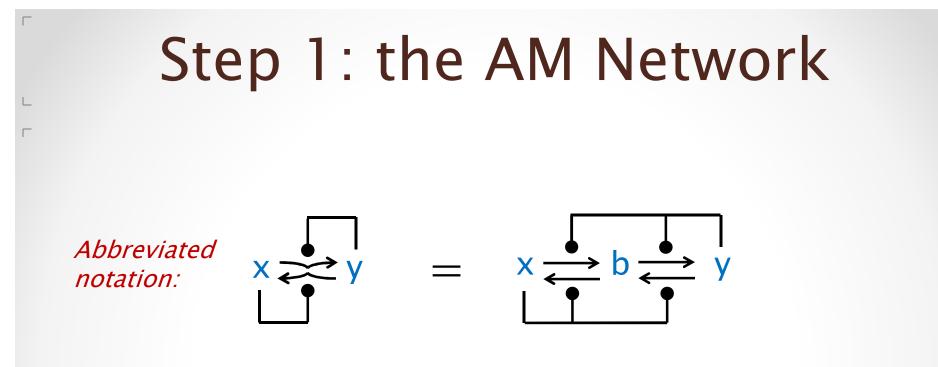
Robust

 $\omega(\sqrt{n \log n})$ majority wins whp



Back to the Cell Cycle

- The AM algorithm has great properties for settling a population into one of two states.
- But that is not what the cell cycle uses to switch its populations of molecules.
- Or is it?



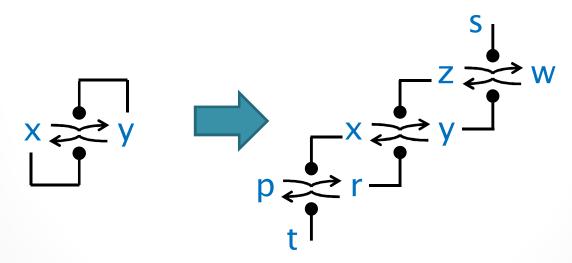
• CONSTRAINT: Autocatalysis, and especially intricate autocatalysis, is not commonly seen in nature.

$$b + x \rightarrow x + x$$

 $b + y \rightarrow y + y$

Step 2: remove auto-catalysis

- Replace autocatalysis by mutual (simple) catalysis, introducing intermediate species z, r.
 - Here z breaks the y auto-catalysis, and r breaks the x autocatalysis, while preserving the feedbacks.
 - z and r need to 'relax back' (to w and p) when they are not catalyzed: s and t provide the back pressure.

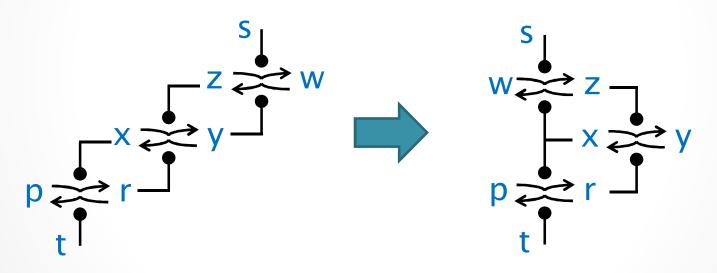


 CONSTRAINT: x and y (two states of the same molecule) are distinct active catalysts: that is not common in nature.

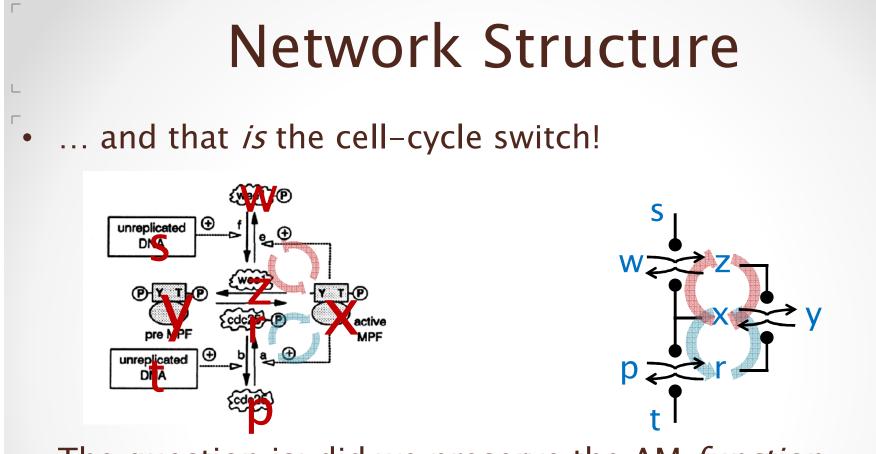
Step 3: only one active state

Remove the catalytic activity of y.

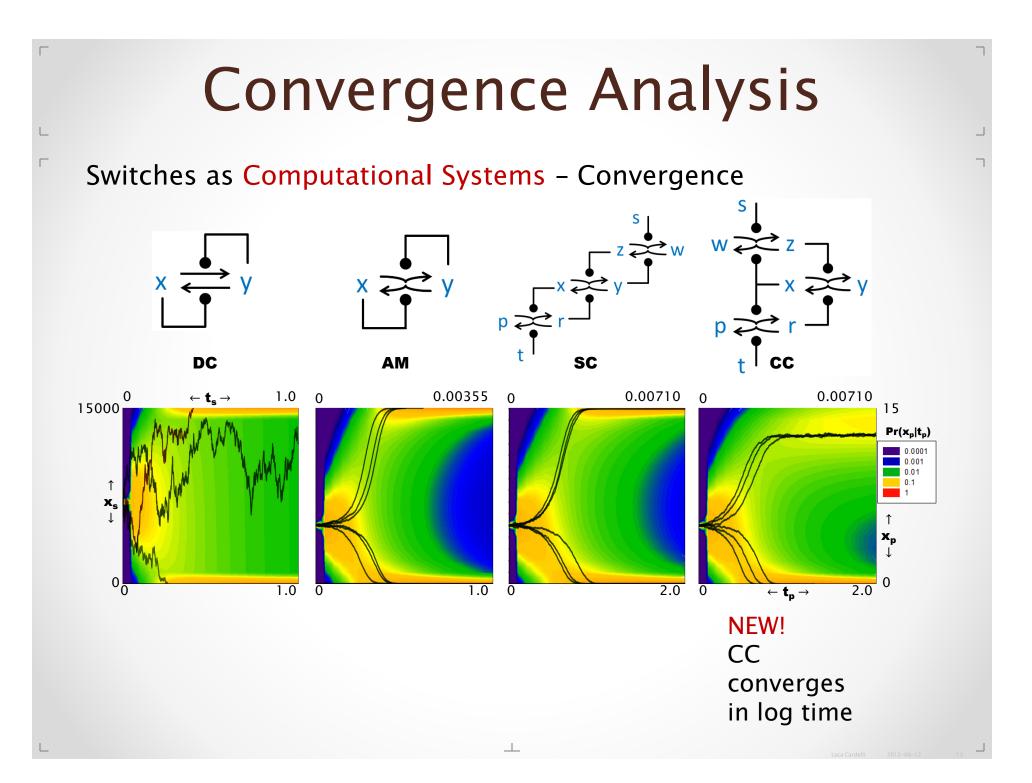
 Instead of y activating itself through z, we are left with z activating y (which remains passive). Hence, to deactivate y we now need to deactivate z. Since x 'wants' to deactivate y, we make x deactivate z.



 All species now have one active (x,z,r) and one inactive (y,w,p) form. This is 'normal'.

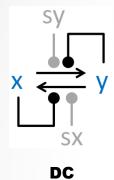


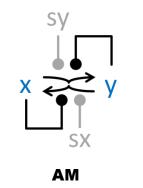
- The question is: did we preserve the AM *function* through our *network transformations*?
 - Ideally: prove either that the networks are 'contextually equivalent' or that the transformations are 'correct'.
 - Practically: compare their 'typical' behavior.

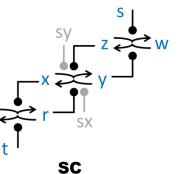


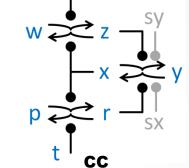
Steady State Analysis

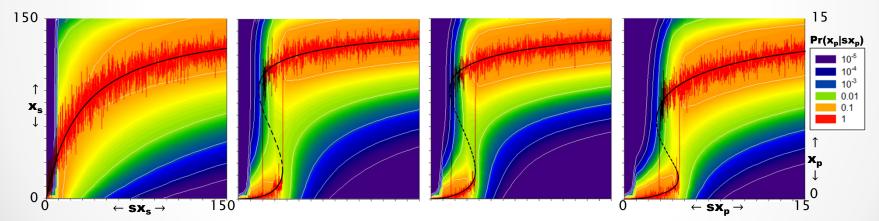
Switches as Dynamical Systems – Steady State Response









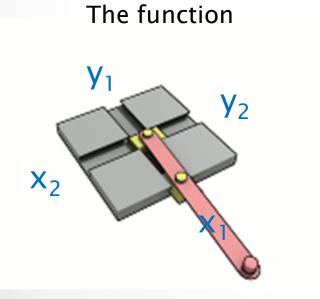


NEW! AM shows hysteresis

The Trammel of Archimedes

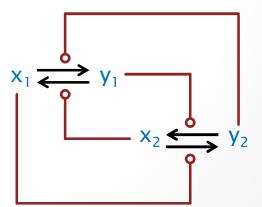
A device to draw ellipses

- Two interconnected switches.
- When one switch is on (off) it flips the other switch on (off).
 When the other switch is on (off) it flips the first switch off (on).
- The amplitude is kept constant by mechanical constraints.



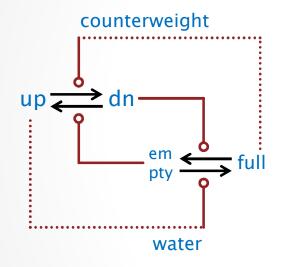
en.wikipedia.org/wiki/Trammel_of_Archimedes

The network

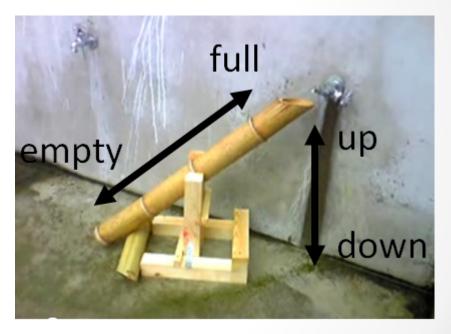


The Shishi Odoshi

A Japanese scarecrow (*lit.* scare-deer)
 O Used by Bela Novak to illustrate the cell cycle switch.



empty + up \rightarrow up + full up + full \rightarrow full + dn full + dn \rightarrow dn + empty dn + empty \rightarrow empty + up

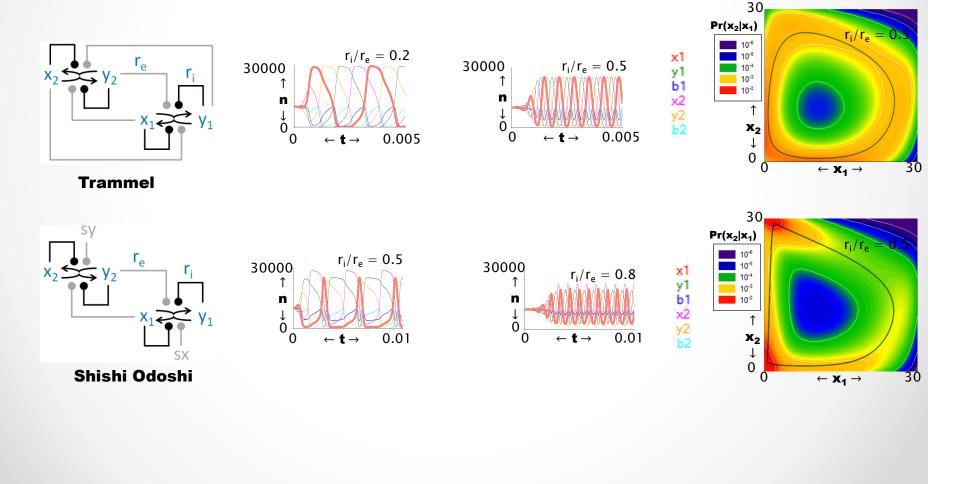


http://www.youtube.com/watch?v=VbvecTIftcE&NR=1&feature=fvwp

Outer switched connections replaced by constant influxes: tap water and gravity.

Contextual Analysis

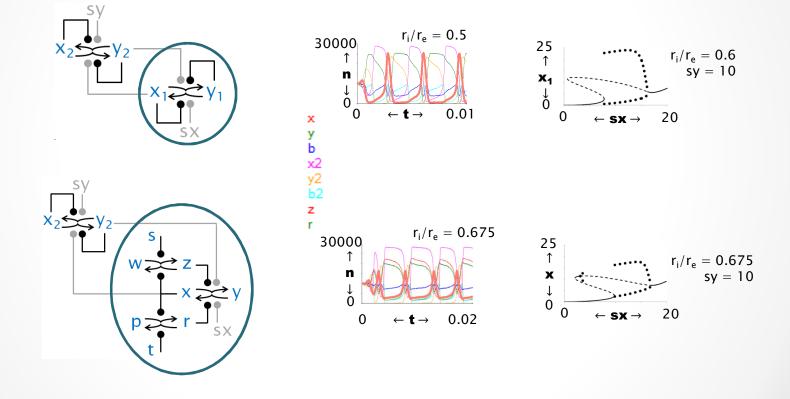
Switches in the context of larger networks (oscillators).



Modularity Analysis

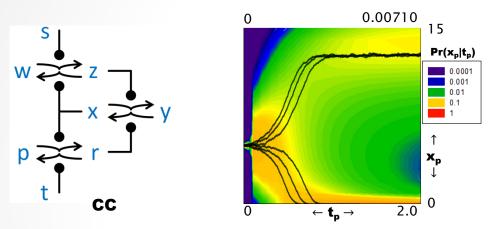
CC can be swapped in for AM.

 \square



CC does not "fully switch"

We have seen that the output of CC does not go 'fully on' like AM:

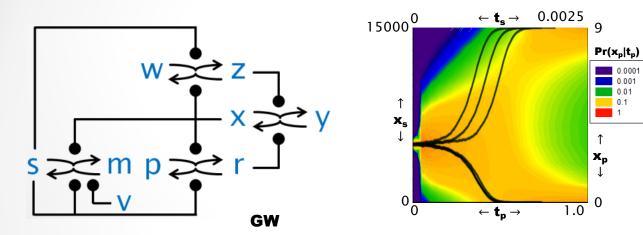


because s continuously inhibits s so that x cannot fully express. This could be solved if x would inhibit s in retaliation.

Q: How would *you* fix this problem?

Nature fixed it!

There is another known feedback loop in real cell cycle switches by which x suppresses s:

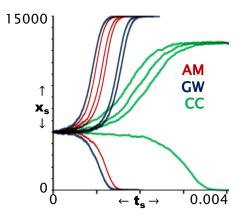


Full activation!

(Also, s and t happen to be the same molecule)

And made it fast too!

More surprising: the extra feedback also speeds up the decision time of the switch, making it about as good as the 'optimal' AM switch:



Conclusion: Nature is trying as hard as it can to implement an AM-class algorithm!

Conclusions

Summary

- The structure of AM implements an input-driven switching function (in addition to the known majority function).
 - The structure of CC implements a input-less majority function (in addition to the known switching function).
- The structures of AM and CC are related, and an intermediate network shares the properties of both.
- The behaviors of AM and CC in isolation are related.
- The behaviors of AM and CC in oscillator contexts are related.
- A refinement of the core CC network, known to occur in nature, improves switching performance and brings it in line with AM performance.

Reverse Engineering

- Q (traditional): What kind of dynamical system is the cell-cycle switch?
- A (traditional): Bistability ultrasensitivity hysteresis … Focused on how unstructured sub–populations change over time.
- Q: What kind of algorithmic system is the cell-cylce switch?
- A: Interaction complexity convergence … Focused on individual molecules as programmable, structured, algorithmic entities.
- Leading to a better understanding of not just the *function* but also the *network* (algorithm).

Direct Engineering

- AM was not learned from nature

 CC was invented ~2.7 billions years ago.
 AM was invented ~6 years ago (but independently).
- But nature may have more tricks
 - If there is some clever population algorithm out there, how will we recognize it?
 - We need to understand how nature operates.