# Biological Systems as Reactive Systems

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### 50 Years of <u>Molecular Cell Biology</u>

- Genes are made of DNA
  - Store digital information as sequences of 4 different nucleotides
  - Direct protein assembly through RNA and the Genetic Code
- Proteins (>10000) are made of amino acids
  - Process signals
  - Activate genes
  - Move materials
  - Catalyze reactions to produce substances
  - Control energy production and consumption
- Bootstrapping still a mystery
  - DNA, RNA, proteins, membranes are today interdependent. Not clear who came first
  - Separation of tasks happened a long time ago
  - Not understood, not essential



### Towards <u>Systems Biology</u>

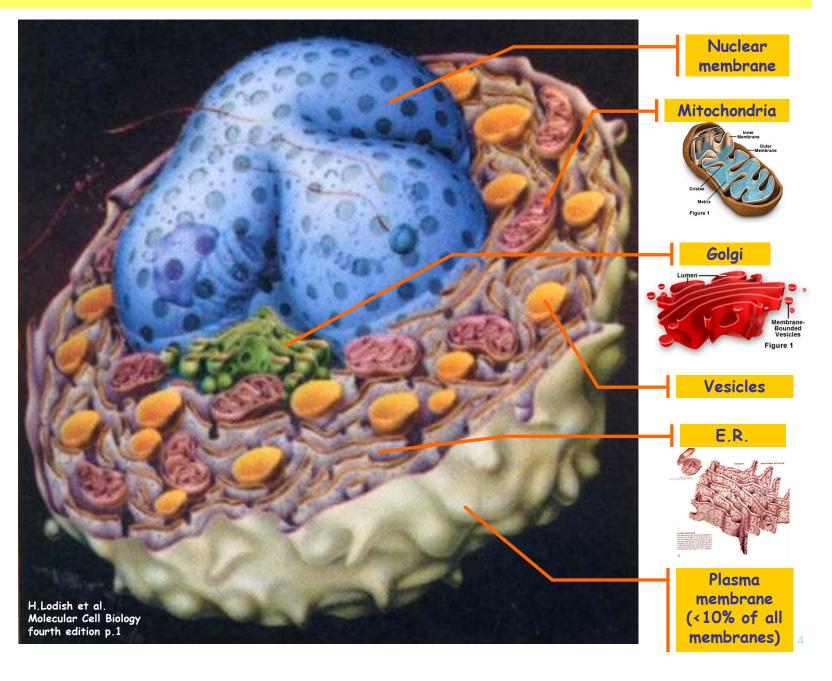
- Biologists now understand many of the cellular components
  - A whole team of biologists will typically study a single protein for years
  - Reductionism: understand the components in order to understand the system
- But this has not led to understand how "the system" works
  - Behavior comes from complex patterns of interactions between components
  - Predictive biology and pharmacology still rare
  - Synthetic biology still unreliable
- New approach: try to understand "the system"
  - Experimentally: massive data gathering and data mining (e.g. Genome projects)
  - Conceptually: modeling and analyzing networks (i.e. interactions) of components
- What kind of a system?
  - Just beyond the basic chemistry of energy and materials processing...
  - Built right out of digital information (DNA)
  - Based on information processing for both survival and evolution
  - Highly concurrent
- Can we fix it when it breaks?
  - Really becomes: How is information structured and processed?

#### Structural Architecture



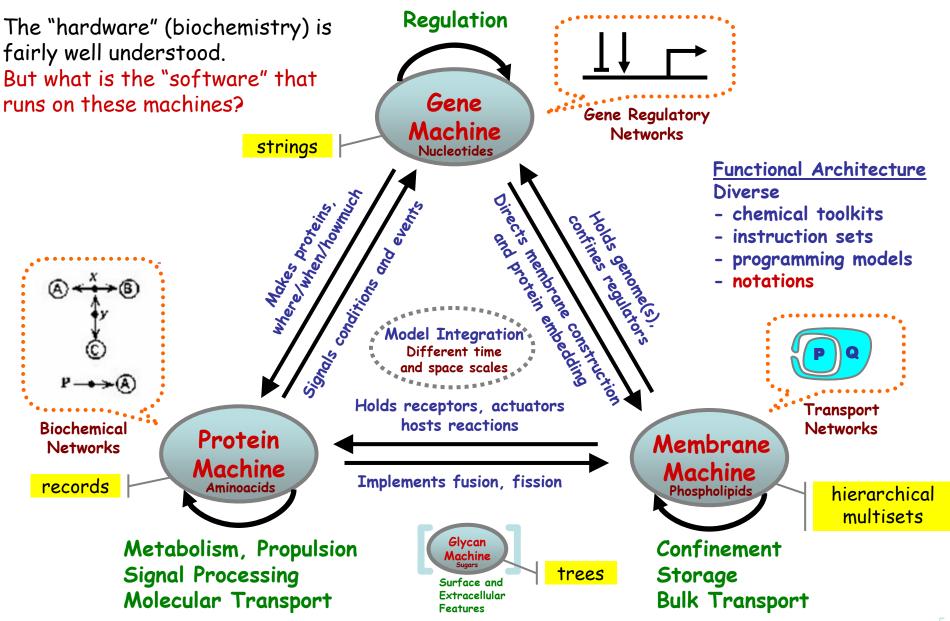
(10~100 trillion in human body)

Membranes everywhere

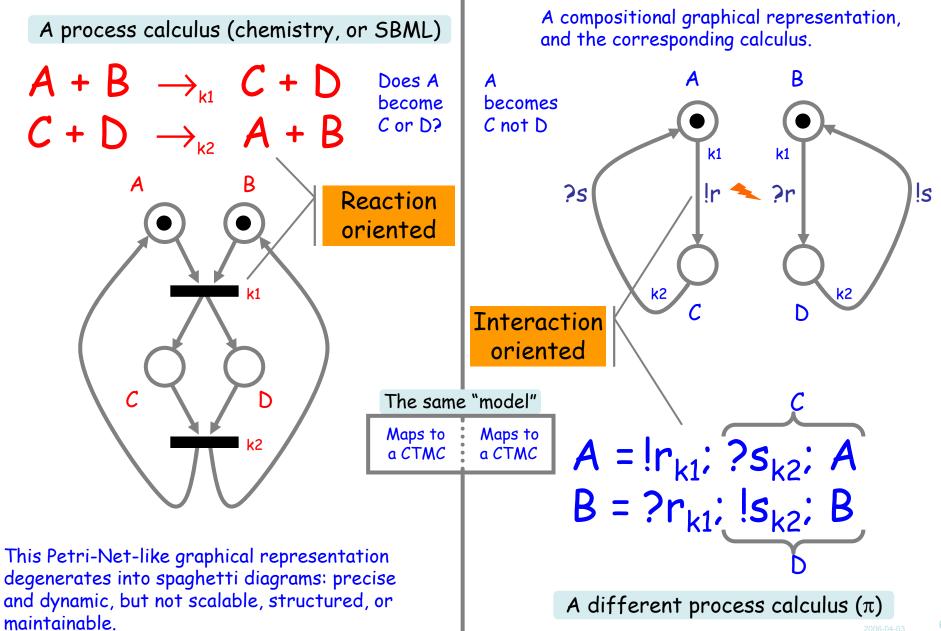




### Abstract Machines of Systems Biology

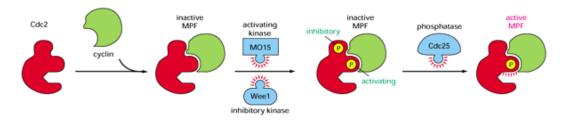


#### Chemistry vs. $\pi$ -calculus

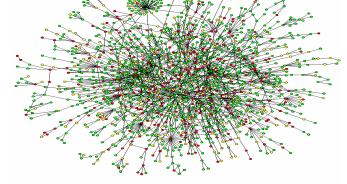


### 1. The Protein Machine

- Complex folded-up shapes that:
  - Fit together, dock, undock.
  - Excite/unexcite, warp each other.
  - Bring together, catalyze, transform materials.
  - Form complex aggregates and networks.



- Mapping out such networks:
  - In principle, it's "just" a very large set of chemical equations.
  - Notations have been developed to summarize and abstract.



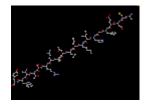
An actual molecular interaction network. (Nodes are distinct protein kinds, arcs mean that two kinds of proteins interact.)

Very close to

the atoms.

#### **Protein Structure**

Primary

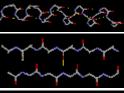


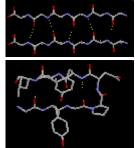
The 20 Aminoacids



Tryptophan

#### Secondary





Alpha Helix, Beta Sheet

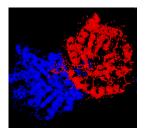
#### Tertiary



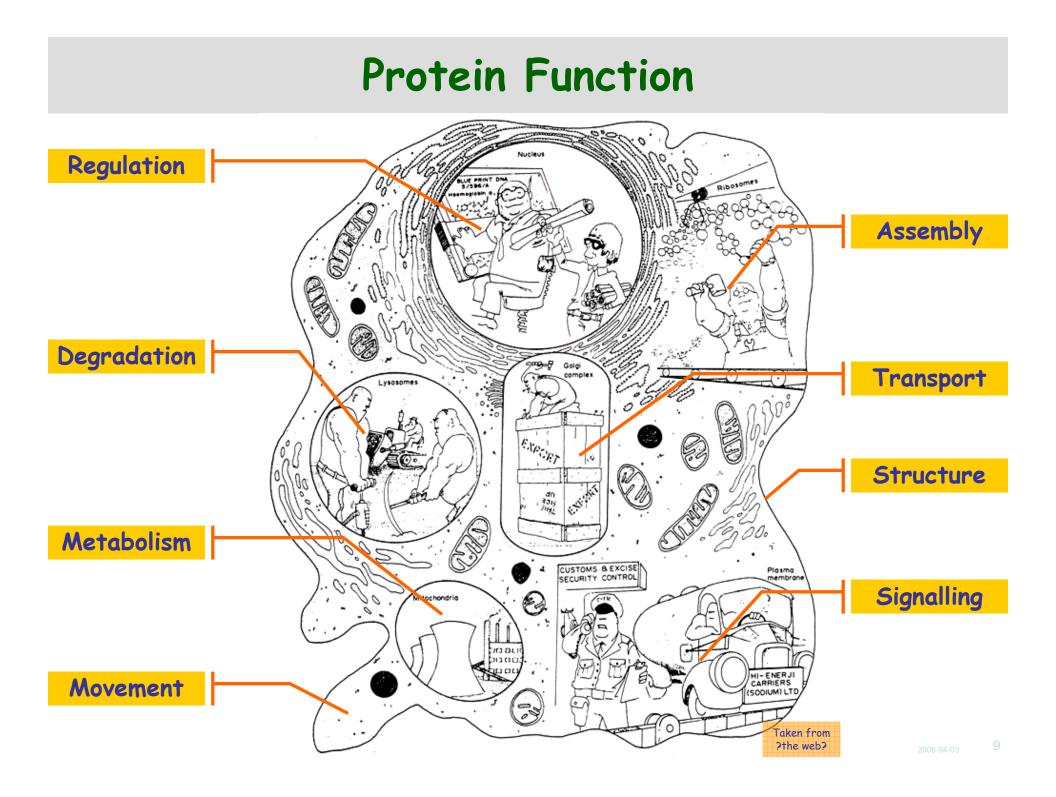


Green Fluorescent Protein

#### Quaternary



#### Triose Phosphate Isomerase



### MIM: Molecular Interaction Maps (Kohn)

| ৻৶৻৻       | <b>≜</b> ↔€    | The double-arrowed line indicates that proteins <b>A</b> and <b>B</b> can bind to each other. "The "node" placed on the line                                      | (A) <b>→</b> ®  | Stoichiometric conversion of A into B.  |  |  |
|------------|----------------|---|-----------------|---|--|--|
| €          | <del>~</del> ® | represents the A:B complex.<br>Asymmetric binding where protein A donates a peptide that<br>binds to a receptor site or pucket on protein B.                      | cytosol nucleus | Transport of A from cytosol to nucleus. The node represents A after it has been transported into the nucleus.   |  |  |
| <b>⊗</b> ≁ | x<br>→®        | Representation of multimolecular complexes: $x$ is A:B; y is (A:B):C. This notation is extensible to any number of components in a complex.                       | @               | Formation of a homodimer. Filled circle on the righ<br>represents another copy of <b>A</b> . The node on the line<br>represents the homodimer <b>A</b> : <b>A</b> . |  |  |
| ©<br>₽→→   | 0<br>⊷®        | Covalent modification of protein A. The single-arrowed line indicates that A can exist in a phosphorylated state. The node represents the phosphorylated species. | x z y           | z is the combination of states defined by $x$ and $y$ .<br>Enzymatic stimulation of a reaction.   |  |  |
| Phitase    | ┝              | Cleavage of a covalent bond: dephosphorylation of <b>A</b> by a phosphatase.  | ÅÅ<br>T         | General symbol for stimulation.<br>A bar behind the arrowhead signifies necessity.<br>General symbol for inhibition.  |  |  |
|            | $\geq$         | Proteolytic cleavage at a specific site within a protein.   | ^^<br>          | Shorthand symbol for transcriptional activation.<br>Shorthand symbol for transcriptional inhibition.  |  |  |
|            |                |   | Ø               | Degradation products  |  |  |

- ion of states defined by x and y.
- ation of a reaction.

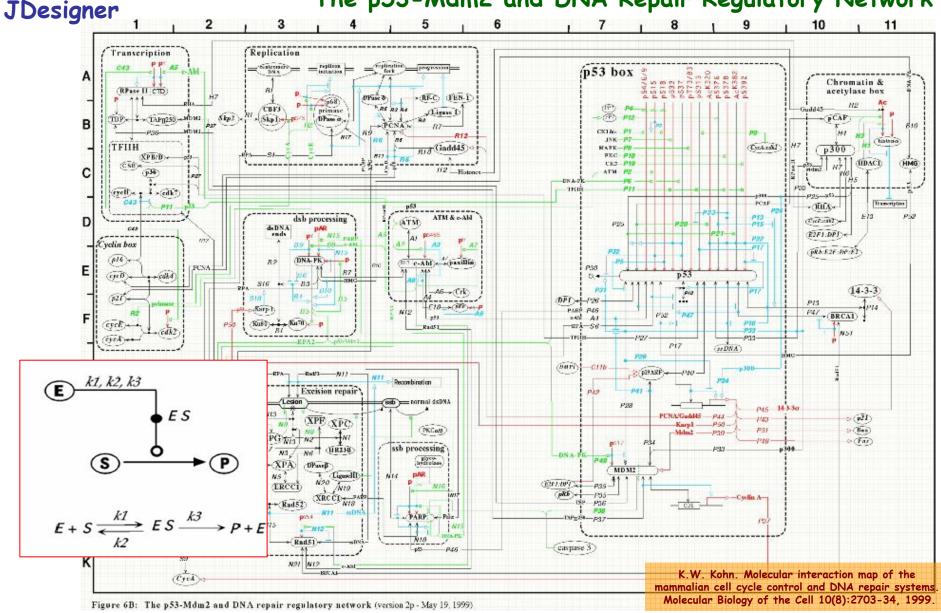
- or inhibition.
- for transcriptional activation.
  - for transcriptional inhibition.
    - ucts

Taken from Kurt W. Kohn

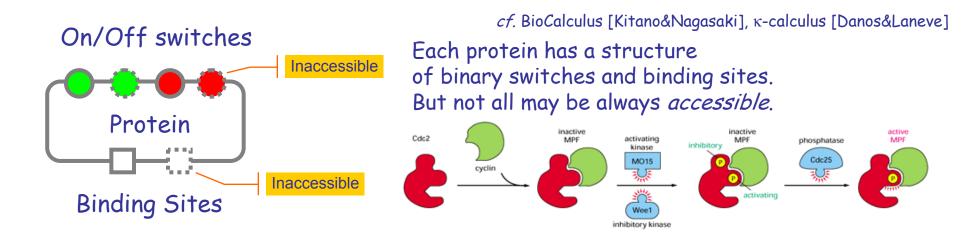
#### **Molecular Interaction Maps**

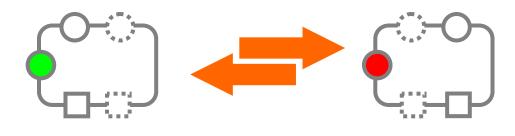
http://www.cds.caltech.edu/~hsauro/index.htm

#### The p53-Mdm2 and DNA Repair Regulatory Network



### The Protein Machine "Instruction Set"



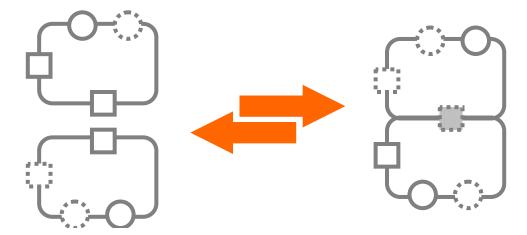


#### Switching of accessible switches.

- May cause other switches and

binding sites to become (in)accessible.

- May be triggered or inhibited by nearby specific proteins in specific states.



#### Binding on accessible sites.

- May cause other switches and

binding sites to become (in)accessible.

- May be triggered or inhibited by nearby specific proteins in specific states.

### Notations for the Protein Machine

- Stochastic  $\pi$ -Calculus
  - Priami (following Hillston's PEPA) formalizes a stochastic version of p-calculus where channels have communication *rates*.
- BioSPi
  - Regev-Shapiro-Silverman propose modeling chemical interactions (exchange of electrons and small molecules) as "communication".
  - Standard stochastic simulation algorithms (Gillespie) can be used to run in-silico experiments.
  - Complex formation is encoded via p-restriction.
- PEPA
  - Calder Gilmore and Hillston model the ERK pathway.
- k-calculus
  - Danos and Laneve (following Kitano's BioCalculus) define a calculus where complex formation is primitive.
- (Stochastic) Petri Nets
  - S.Reddy'94 modeling pathways.
  - Srivastava Perterson and Bentley analyze and simulate E.coli stress response circuit.

- Bio State Charts
  - Harel uses State Charts to model biological interactions via a semi-graphical FSM notation.
- Pathway Logic
  - Talcott-Eker-Knapp-Lincoln use term-rewriting.
- BioCham
  - ChabrierRivier-Fages-Soliman use term-rewriting and CLT modelchecking.
- Kohn Diagrams, Kitano Diagrams
- SBML (Systems Biology Markup Language)
  - XML dialect for MIM's:
    - Compartments (statically nested)
    - Reagents with concentrations
    - Reactions with various rate laws
  - Read and written by many tools via the Systems Biology Workbench protocol

#### MAPK Cascade

### <u>Ultrasensitivity in the mitogen-activated protein cascade</u>, Chi-Ying F. Huang and James E. Ferrell, Jr., 1996, <u>Proc. Natl. Acad. Sci. USA</u>, 93, 10078-10083.

| Biochemistry: Huang and Ferrel       | I  | Proc. Natl. Acad. Sci. USA 93 (1996) |                             |           |  |
|--------------------------------------|--|--------------------------------------|-----------------------------|-----------|--|
| Table 2. Predicted Hill coefficients | for MAP kinase cascade comp                                | onents: Varying the as               | sumed K <sub>m</sub> values |           |  |
|                                      | Range of effective Hill coefficients (nH)<br>predicted for |                                      |                             |           |  |
|                                      |  |                                      |                             |           |  |
| Reaction                             | Range of assumed K <sub>m</sub><br>values                  | MAPKKK                               | MAPKK                       | MAPK      |  |
| 1. MAPKKK $\rightarrow$ MAPKKK*      | 60-1500 nM   | 1.0                                  | 1.7                         | 4.9       |  |
| 2. MAPKKK $* \rightarrow$ MAPKKK     | 60 1500 nM   | 1.0                                  | 1.7                         | 4.9       |  |
| 3. MAPKK $\rightarrow$ MAPKK-P       | 60-1500 nM   | 1.0                                  | 1.3-2.3                     | 4.0 - 5.1 |  |
| 4. MAPKK-P → MAPKK                   | 60–1500 nM   | 1.0                                  | 1.5 - 1.9                   | 3.6-6.7   |  |
| 5. MAPKK-P $\rightarrow$ MAPKK-PP    | 60–1500 nM   | 1.0                                  | 1.3-2.4                     | 3.8-5.2   |  |
| 6. MAPKK-PP $\rightarrow$ MAPKK-P    | 60–1500 nM   | 1.0                                  | 1.7-1.8                     | 4.1-6.4   |  |
| 7. MAPK $\rightarrow$ MAPK-P         | 60–1500 nM (300 nM <sup>†</sup> )                          | 1.0                                  | 1.7                         | 3.7-6.2   |  |
| 8. MAPK-P $\rightarrow$ MAPK         | 60-1500 nM   | 1.0                                  | 1.7                         | 4.3-5.2   |  |
| 9. MAPK-P $\rightarrow$ MAPK-PP      | 60–1500 nM   | 1.0                                  | 1.7                         | 3.4 - 6.1 |  |
| 10. MAPK-PP $\rightarrow$ MAPK-P     | 60–1500 nM   | 1.0                                  | 1.7                         | 4.7-5.1   |  |

The assumed  $K_m$  values for each reaction were individually varied over the ranges shown, with the assumed  $K_m$  values for the other nine reactions held constant. The effective Hill coefficients were calculated from the steepness of the predicted stimulus/response curves, as described in the text.

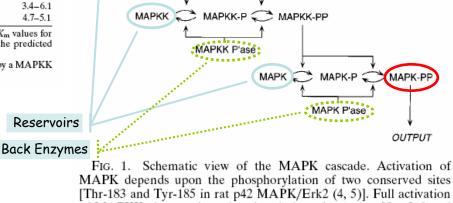
<sup>†</sup>The  $K_m$  value for reaction 7 has been measured to be 300 nM for the phosphorylation of a mammalian MAPK by a MAPKK (N. Ahn, personal communication). All of the other  $K_m$  values were initially assumed to be 300 nM as well.

d.

KK-P + KK P'ase

[6]

Calculations. Eqs. 1-10 represent the reactions of the MAPK cascade, which are shown schematically in Fig. 1. We have used Goldbeter and Koshland's nomenclature for the rate constants the letter a denotes association, d denotes dissociation without catalysis, and k denotes product formation (11). KKK denotes MAPKKK: KK denotes MAPKK: and K denotes MAPK.



10 chemical

reactions

MAPKKK\*

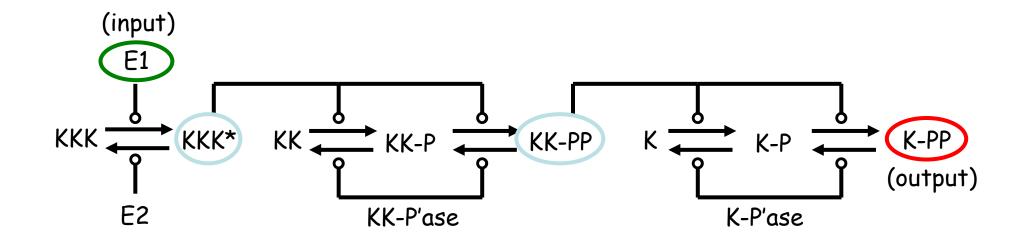
INPUT (E1)

E2

MAPKKK 🧲

MAPK depends upon the phosphorylation of two conserved sites [Thr-183 and Tyr-185 in rat p42 MAPK/Erk2 (4, 5)]. Full activation of MAPKK also requires phosphorylation of two sites [Ser-218 and Ser-222 in mouse Mek-1/MKK1 (6–10)]. Detailed mechanisms for the activation of various MAPKKKs (e.g., Raf-1, B-Raf, Mos) are not yet established; here we assume that MAPKKKs are activated and inactivated by enzymes we denote E1 and E2. MAPKKK\* denotes activated MAPKKK. MAPKK-P and MAPKK-PP denote singly and doubly phosphorylated MAPKK, respectively. MAPK-P and MAPK-PP denote singly and doubly phosphorylated MAPK. P'ase denotes phosphatase.

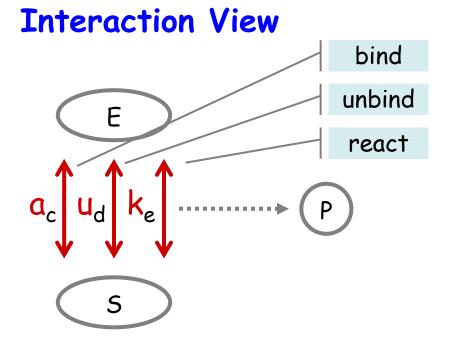
#### The Circuit



#### **Enzymatic Reactions**

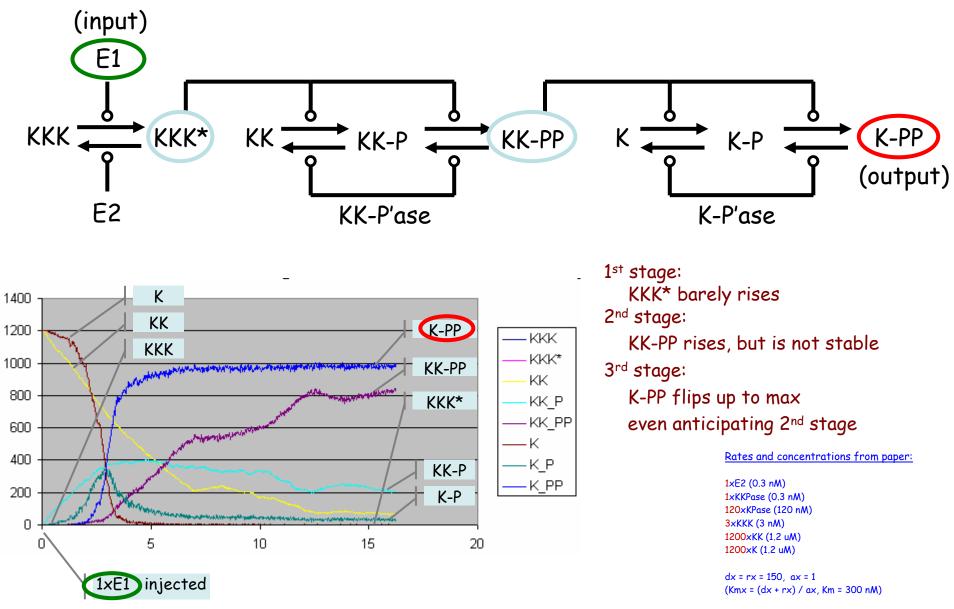
#### **Reaction View**





private bindings between one S and one E molecule  $S() \triangleq new u@d new k@e$  $|a_c(u,k); (!u_d; S() + !k_e; P())$ bind unbind react  $E() \triangleq ?a_c(u,k); (?u_d; E() + ?k_e; E())$  $P() \triangleq ...$ 

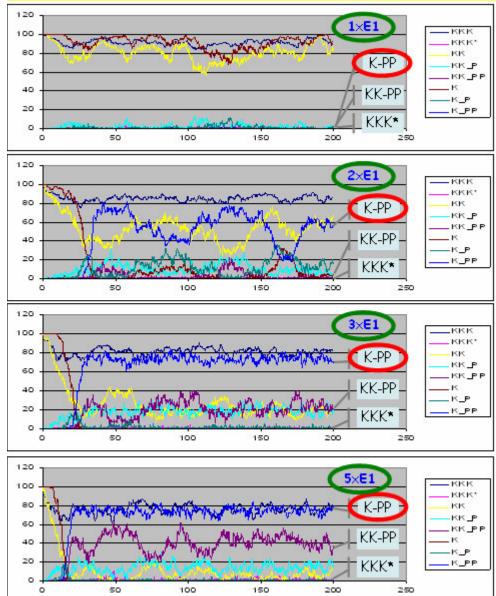
#### MAPK Cascade Simulation in SPiM

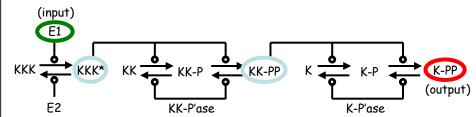


1×E1

06-04-03 1

#### **MAPK** Cascade Simulation in SPiM



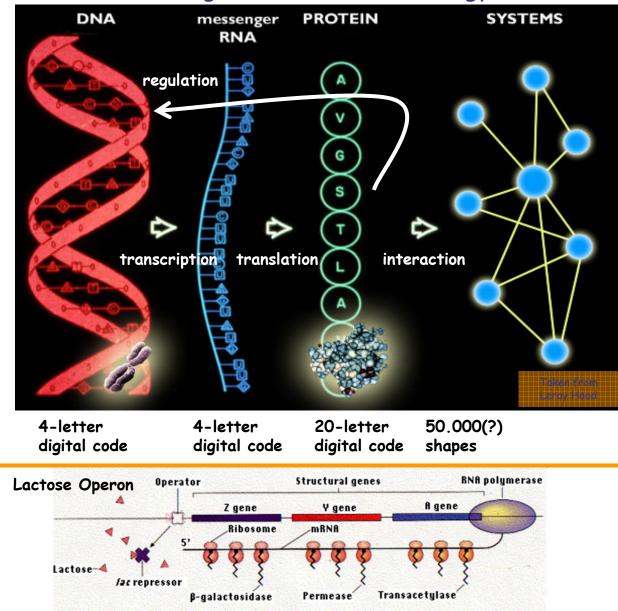


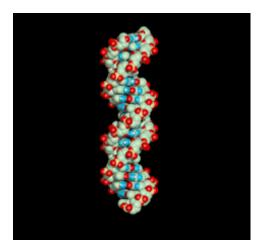
All coefficients 1.0 !!! 100×KKK, 100×KK, 100×K, 13×E2, 13×KKPse, 13×KPse. nxE1 as indicated (1×E1 is not sufficient to produce an output)

### 2. The Gene Machine

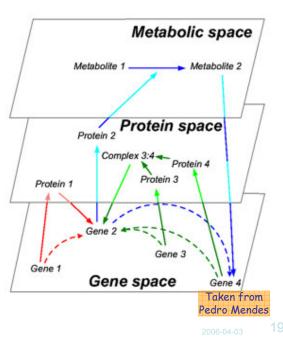
Pretty far from the atoms.

#### The "Central Dogma" of Molecular Biology



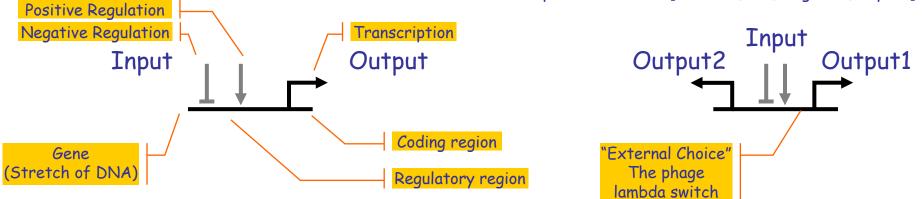


DNA Tutorial



### The Gene Machine "Instruction Set"

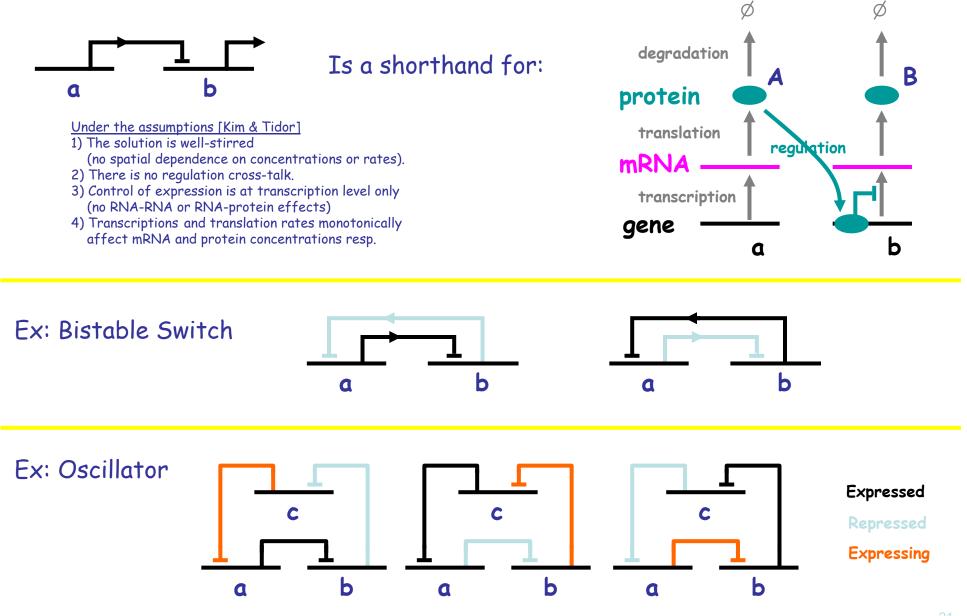
cf. Hybrid Petri Nets [Matsuno, Doi, Nagasaki, Miyano]



<u>Regulation</u> of a gene (positive and negative) influences transcription. The regulatory region has precise DNA sequences, but not meant for coding proteins: meant for binding regulators.

<u>Transcription</u> produces molecules (RNA or, through RNA, proteins) that bind to regulatory region of other genes (or that are endproducts). Human (and mammalian) Genome Size 3Gbp (Giga base pairs) 750MB @ 4bp/Byte (CD) Non-repetitive: 1Gbp 250MB In genes: 320Mbp 80MB Coding: 160Mbp 40MB Protein-coding genes: 30,000-40,000 <u>M.Genitalium</u> (smallest true organism) 580,073bp 145KB (eBook) <u>E.Coli</u> (bacteria): 4Mbp 1MB (floppy) <u>Yeast</u> (eukarya): 12Mbp 3MB (MP3 song) <u>Wheat</u> 17Gbp 4.25GB (DVD)

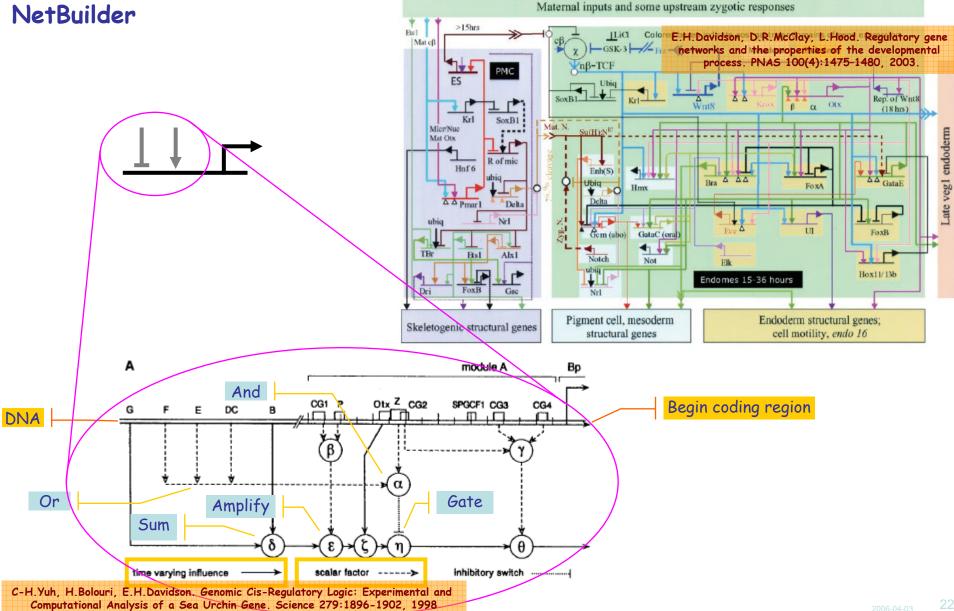
### Gene Composition



### Gene Regulatory Networks

http://strc.herts.ac.uk/bio/maria/NetBuilder/

#### NetBuilder



### The Programming Model

- Strange facts about genetic networks:
  - Not an operator algebra. The output of each gate is fixed and pre-determined; it is never a function of the input!
  - Not term-rewriting, nor Petri nets. Inhibition is widespread.
  - Not Communicating Sequential Processes. Feedback is widespread: asynchronous communication needed to avoid immediate self-deadlocks. Even the simplest gates cannot be modeled as a single synchronous automata.
  - Not Message-Passing between genes. Messages themselves have behavior (e.g., they stochastically decay and combine), hence messages are processes as well.
  - Not Data-Flow. Any attempt to use data-flow-style modeling seems doomed because of widespread loops that lead to deadlocks or unbounded queues. Data-flow tokens do not "decay" like proteins.
- How can it possibly work?
  - Stochastic broadcasting. The apparently crude idea of broadcasting a whole bunch of asynchronous decaying messages to activate a future gate, means there are never any "pipeline full" deadlocks, even in presence of abundant feedback loops.
  - Stochastic degradation. Degradation is fundamental for system stability, and at the same time can lead to sudden instability and detection of concentration levels.

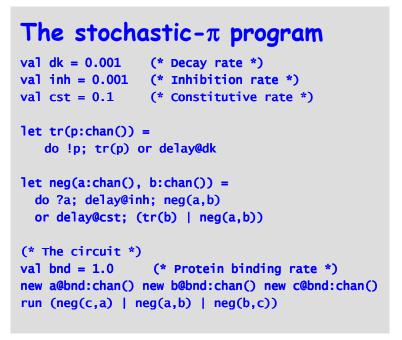
### Notations for the Gene Machine

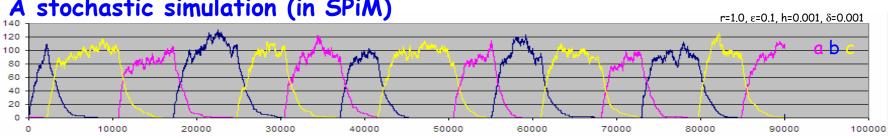
- Many of the same techniques as for the Protein Machine apply.
  - Process Calculi, Petri Nets, Term-Rewriting Systems...
- But the "programming model" is different.
  - Asynchronous stochastic control.
  - Biologically poorly understood.
  - Network "motifs" are being analyzed.

- Specific techniques:
  - Hybrid Petri Nets
    - [Matsuno, Doi, Nagasaki, Miyano] Gene Regulation
    - Genomic Object Net www.genomicobject.net
- Gene Regulation Diagrams
- Mixed Gene-Protein Diagrams

#### Gene Gates and Circuits

A gene gate neg(a,b) ≜ ?a<sub>r</sub>; τ<sub>η</sub>; neg(a,b) + τ<sub>ε</sub>; (tr(b) | neg(a,b)) ► b 0 neg  $tr(p) \triangleq (!p_r; tr(p)) + \tau_{\delta}$ A genetic circuit (engineered in E.Coli) neg(a,b) | neg(b,c) | neg Ь С neq(c,a)0



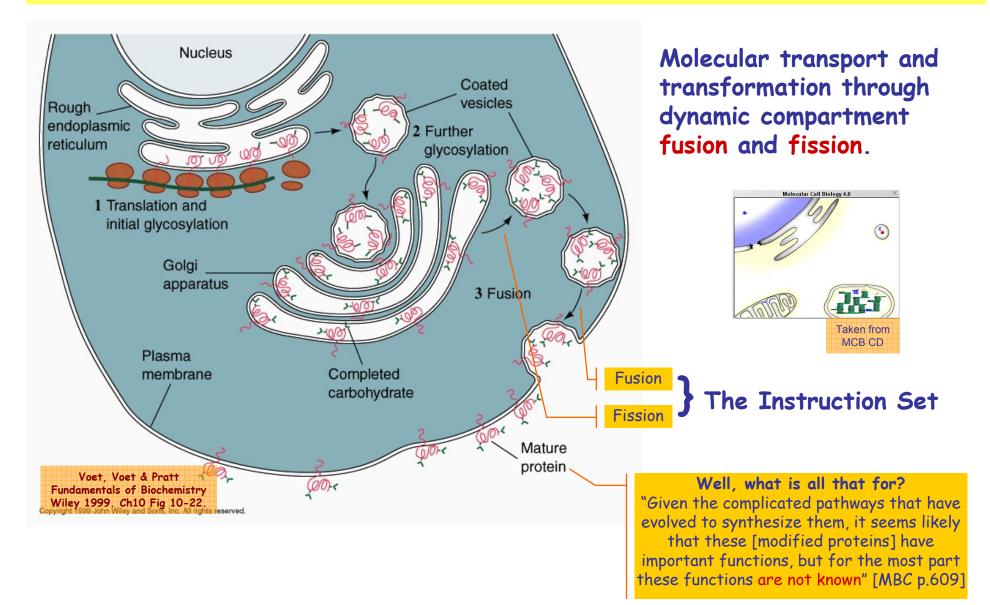


#### stochastic simulation (in SPiM)

neg

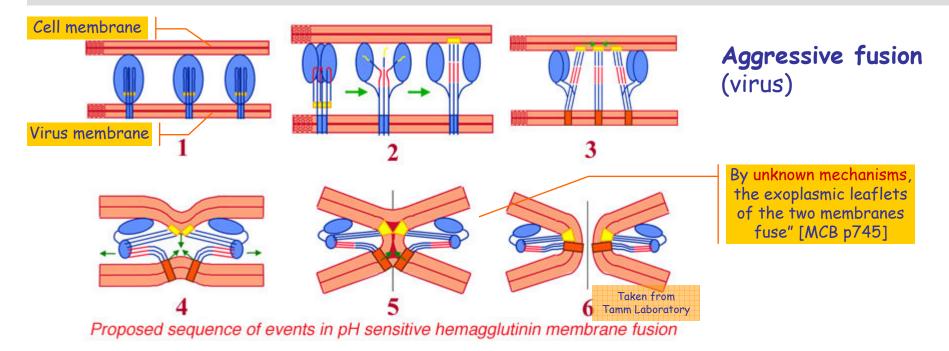
neg

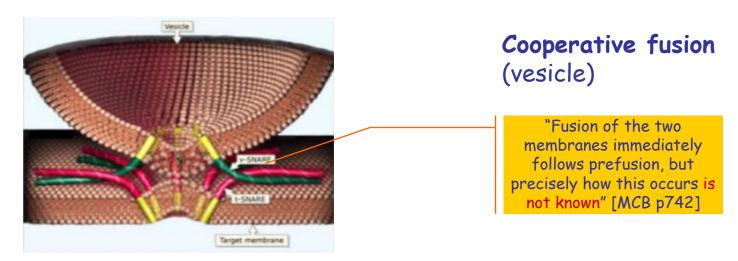
### 3. The Membrane Machine Very far from the atoms.



### Membrane Fusion

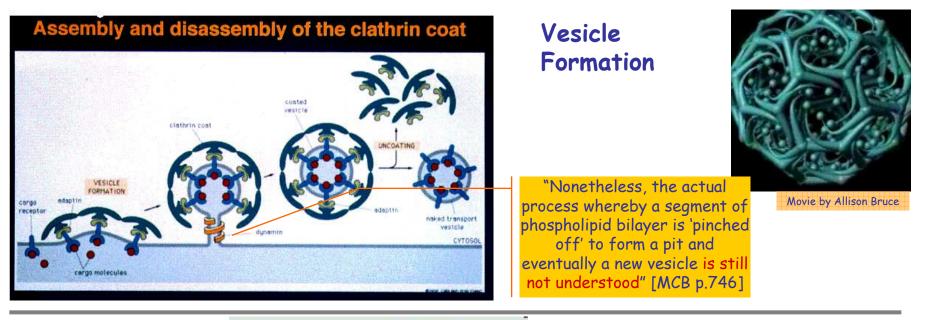
Positive curvature to Negative curvature transition in 3D

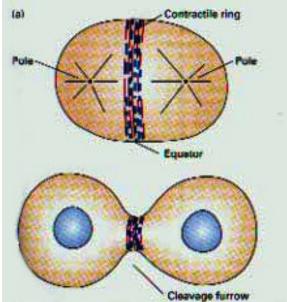




#### **Membrane Fission**

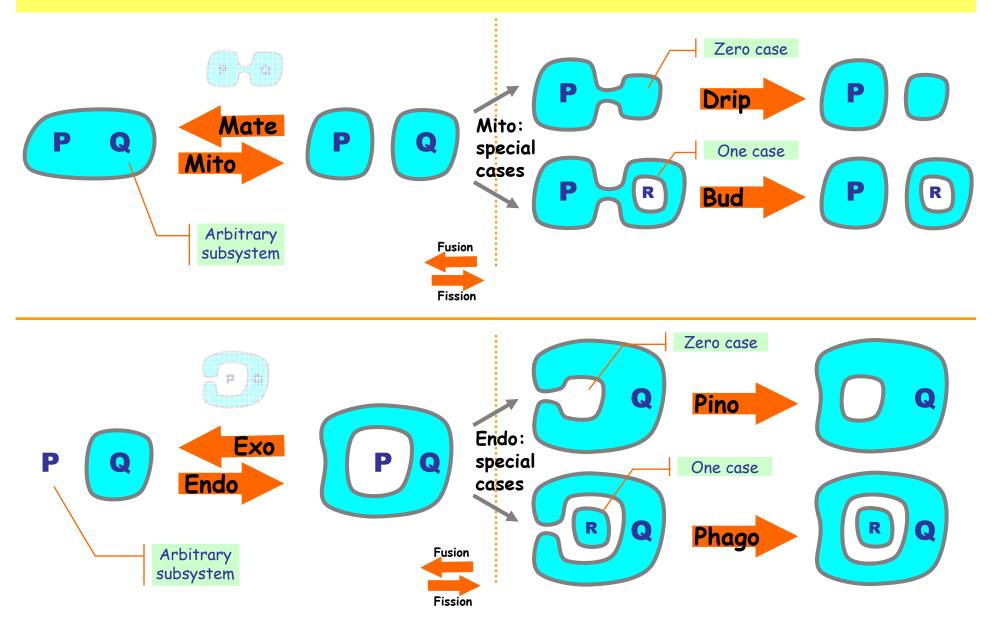
Negative curvature to Positive curvature transition in 3D



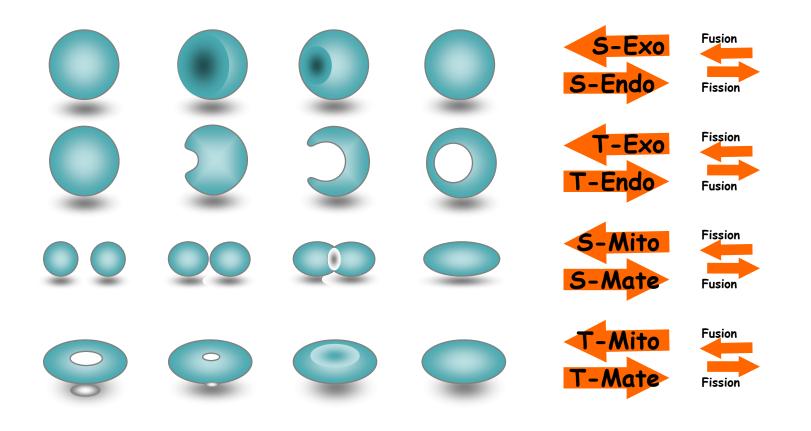


#### Cytokinesis (Mitosis)

### The Membrane Machine "Instruction Set"

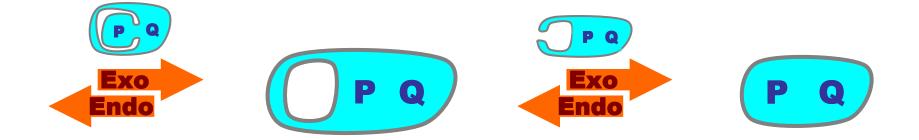


#### ... in 3D



#### Mito/Mate by 3 Endo/Exo





### Notations for the Membrane Machine

- "Snapshot" diagrams
  - In biology literature.
- P-Systems
  - G.Paun uses ideas from the theory of grammars and formal languages to model "Membrane Computing" (book 2002).

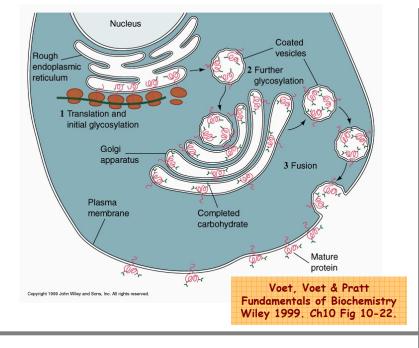
http://psystems.disco.unimib.it/.

#### • BioAmbients

- An extension of BioSPI along Ambient Calculus lines (with more bio-relevant mobility primitives) to model dynamic compartments.
- Brane Calculi
  - Computation on the membrane...

#### Membrane Algorithms

#### Protein Production and Secretion

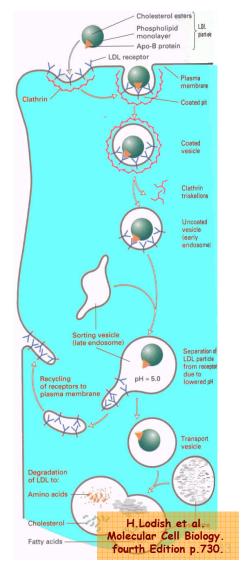


Viral Replication

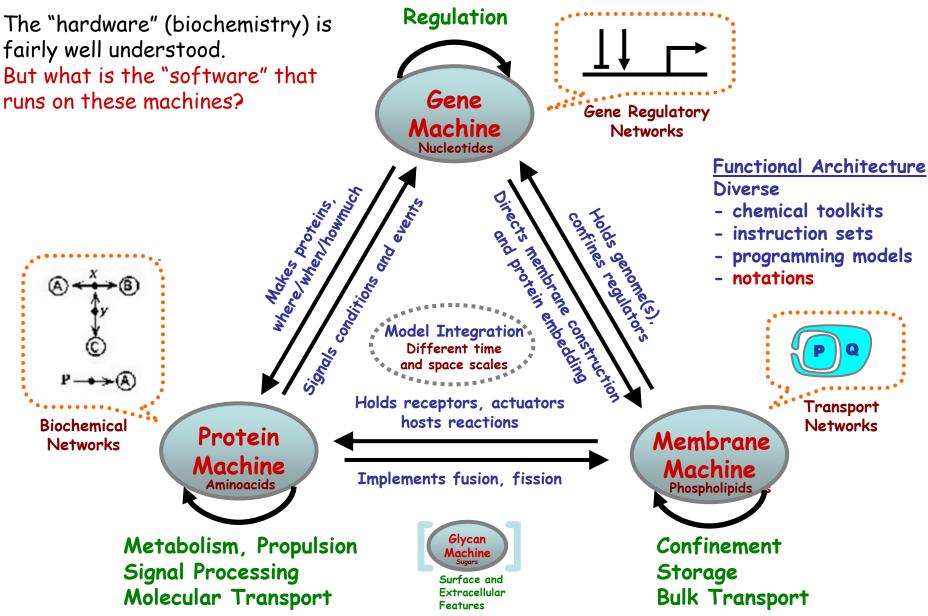
Virus Ray and Annukana Revelage gretain Finggo Cytosol Fin

Adapted from: B.Alberts et al. Molecular Biology of the Cell third edition p.279.





### Abstract Machines of Systems Biology



# Model Construction and Validation

### **Reactive Systems**

- Modeling biological systems
  - Not as continuous systems (often highly nonlinear)
  - But as discrete reactive systems; abstract machines with:
    - States represent situations
    - Event-driven transitions between states represent dynamics
  - The adequacy of describing (discrete) complex systems as reactive systems has been argued convincingly [Harel]
- Many biological systems exhibit feaures of reactive systems:
  - Deep layering of abstractions
  - Complex composition of simple components
  - Discrete transitions between states
  - Digital coding and processing of information
  - Reactive information-driven behavior
  - High degree of concurrency and nondeterminism
  - "Emergent behavior" not obvious from part list

### Model Validation: Simulation

- Basic stochastic algorithm: Gillespie
  - Exact (i.e. based on physics) stochastic simulation of chemical kinetics.
  - Can compute concentrations and reaction times for biochemical networks.
- Stochastic Process Calculi
  - BioSPi [Shapiro, Regev, Priami, et. al.]
    - Stochastic process calculus based on Gillespie.
  - BioAmbients [Regev, Panina, Silverma, Cardelli, Shapiro]
    - Extension of BioSpi for membranes.
  - Case study: Lymphocytes in Inflamed Blood Vessels [Lecaa, Priami, Quaglia]
    - Original analysis of lymphocyte rolling in blood vessels of different diameters.
  - Case study: Lambda Switch [Celine Kuttler, IRI Lille]
    - Model of phage lambda genome (well-studied system).
  - Case study: VICE [U. Pisa]
    - Minimal prokaryote genome (180 genes) and metabolism of *whole* VIrtual CEII, in stochastic  $\pi$ -calculus, simulated under stable conditions for 40K transitions.
- Hybrid approaches
  - Charon language [UPenn]
    - Hybrid systems: continuous differential equations + discrete/stochastic mode switching.
  - Etc.

### Model Validation: "Program" Analysis

#### • Causality Analysis

- *Biochemical pathways*, ("concurrent traces" such as the one here), are found in biology publications, summarizing known facts.
- This one, however, was automatically generated from a program written in BioSpi by comparing traces of all possible interactions. [Curti, Priami, Degano, Baldari]
- One can play with the program to investigate various hypotheses about the pathways.

#### • Control Flow Analysis

- Flow analysis techniques applied to process calculi.
- Overapproximation of behavior used to answer questions about what "cannot happen".
- Analysis of positive feedback transcription regulation in BioAmbients [Flemming Nielson].
- Probabilistic Abstract Interpretation



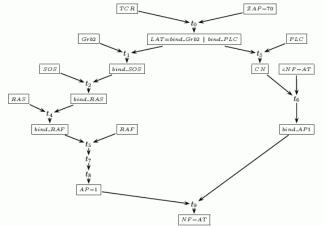
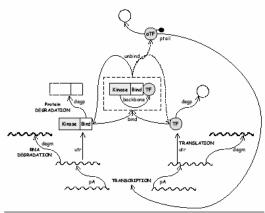
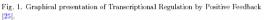


Fig.2. A computation of Sys. For readability, the processes, enclosed in boxes, have no address. Causality (both on transitions and processes) is represented by the (Hasse diagram resulting from the) arrows; their absence makes it explicit concurrent activities.

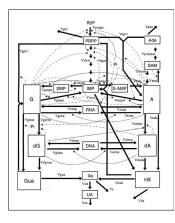




### Model Validation: Modelchecking

- Temporal
  - Software verification of biomolecular systems (NA pump) [Ciobanu]
  - Analysis of mammalian cell cycle (after Kohn) in CTL. [Chabrier-Rivier Chiaverini Danos Fages Schachter]
    - E.g. is state  $S_1$  a necessary checkpoint for reaching state  $S_2$ ?
- Quantitative: Simpathica/xssys [Antioniotti Park Policriti Ugel Mishra]
  - Quantitative temporal logic queries of human Purine metabolism model.

Eventually(Always (PRPP = 1.7 \* PRPP1) implies steady state() and Eventually(Always(IMP < 2 \* IMP1)) and Eventually(Always(hx\_pool < 10\*hx\_pool1)))



#### Stochastic: Spring [Parker Normal Kwiatkowska]

- Designed for stochastic (computer) network analysis
  - Discrete and Continuous Markov Processes.
  - Process input language.
  - Modelchecking of probabilistic queries.

### What Reactive Systems Do For Us

#### We can write things down precisely

 We can modularly describe high structural and combinatorial complexity ("do programming").

#### We can calculate and analyze

- Directly support simulation.
- Support analysis (e.g. control flow, causality, nondeterminism).
- Support state exploration (modelchecking).

#### We can visualize

- Automata-like presentations.
- Petri-Net-like presentations.
- State Charts, Live Sequence Charts [Harel]
  - Hierarchical automata.
  - Scenario composition.

#### We can reason

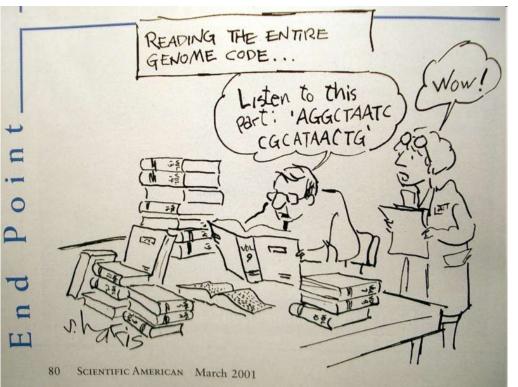
- Suitable equivalences on processes induce algebraic laws.
- We can relate different systems (e.g. equivalent behaviors).
- We can relate different abstraction levels.
- We can use equivalences for state minimization (symmetries).

#### Disclaimers

- Some of these technologies are basically ready (medium-scale stochastic simulation and analysis, medium-scale nondeterministic and stochastic modelchecking).
- Others need to scale up significantly to be really useful. This is (has been) the challenge for computer scientists.

Many approaches, same basic philosophy, tools being built:  $\Rightarrow$  Proc. Computational Methods in Systems Biology [2003-2005]

# Conclusions



- Q: "The data are accumulating and the computers are humming, what we are lacking are the words, the grammar and the syntax of a new language..." D. Bray (TIBS 22(9):325-326, 1997)
- A: "The most advanced tools for computer process description seem to be also the best tools for the description of biomolecular systems."

E.Shapiro (Lecture Notes)

#### References

[MCB] Molecular Cell Biology, Freeman. [MBC] Molecular Biology of the Cell, Garland. [Ptashne] A Genetic Switch. [Davidson] Genomic Regulatory Systems.

[Milner] Communicating and Mobile Systems: the Pi-Calculus. [Regev] Computational Systems Biology: A Calculus for Biomolecular Knowledge (Ph.D. Thesis).

Papers

**BioAmbients** 

a stochastic calculus with compartments.

Brane Calculi

process calculi with computation "on" the membranes, not inside them. *Bitonal Systems* 

membrane reactions and their connections to "local" patch reactions. *Abstract Machines of Systems Biology* 

the abstract machines implemented by biochemical toolkits.

www.luca.demon.co.uk/BioComputing.htm