Abstract Machines of Systems Biology

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50 Years of Molecular Cell Biology

Genes are made of DNA

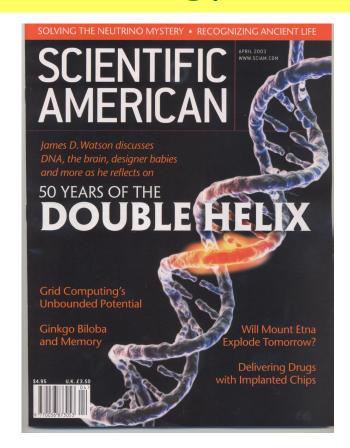
- Store digital information as sequences of 4 different nucleotides
- Direct protein assembly through RNA and the Genetic Code

Proteins (>10000) are made of amino acids

- Process signals
- Activate genes
- Move materials
- Catalyze reactions to produce substances
- Control energy production and consumption

Bootstrapping still a mystery

- DNA, RNA, proteines, membranes are today interdependent. Not clear who came first
- Separation of tasks happened a long time ago
- Not understood, not essential



Towards Systems Biology

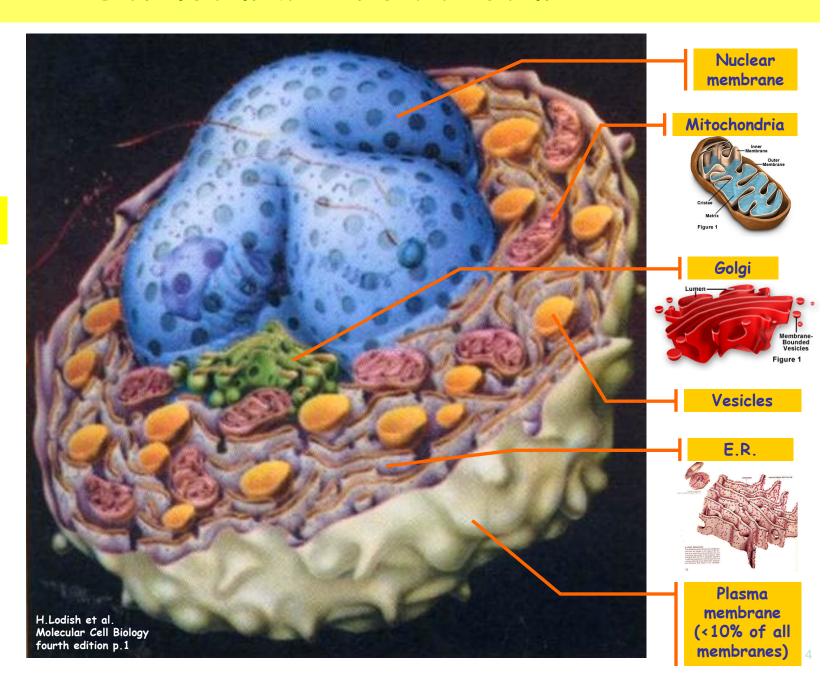
- Biologists now understand many of the cellular components
 - A whole team of biologists will typically study a single protein for years
 - When each component and each reaction is understood, the system is understood (?)
- But this has not led to understand how "the system" works
 - Behavior comes from complex chains of interactions between components
 - Predictive biology and pharmacology still rare
 - Synthetic biology still unreliable
- New approach: try to understand "the system"
 - Experimentally: massive data gathering and data mining (e.g. Genome projects)
 - Conceptually: modeling and analyzing networks (i.e. interactions) of components
- What kind of a system?
 - Just beyond the basic chemistry of energy and materials processing...
 - Built right out of digital information (DNA)
 - Based on information processing for both survival and evolution
- Can we fix it when it breaks?
 - The question really becomes: How is information structured and processed?

Structural Architecture

Eukaryotic Cell

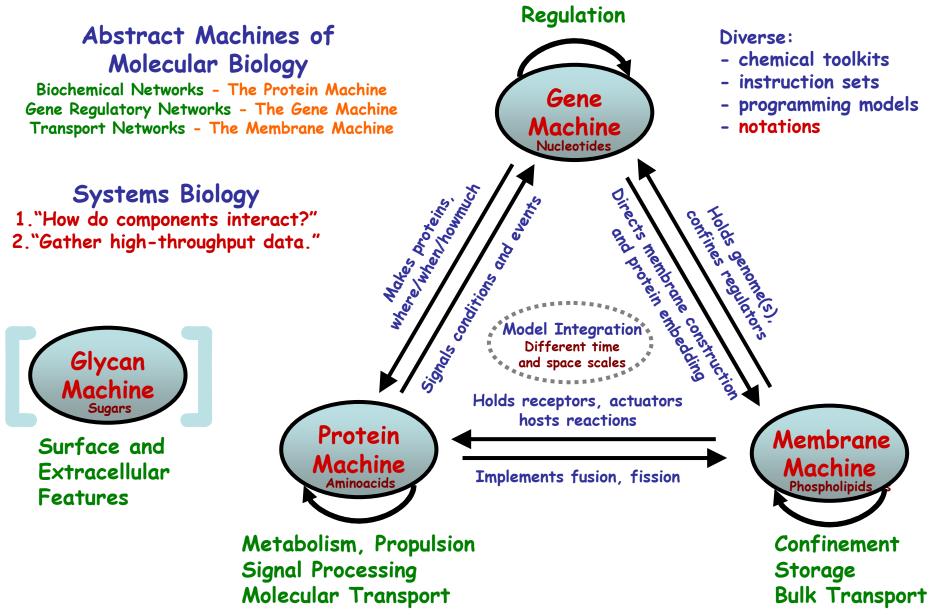
(10~100 trillion in human body)

Membranes everywhere





Functional Architecture

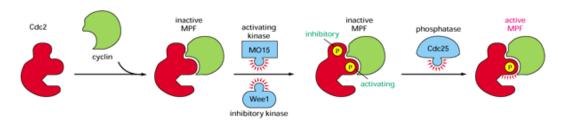


Very close to the atoms

1. The Protein Machine

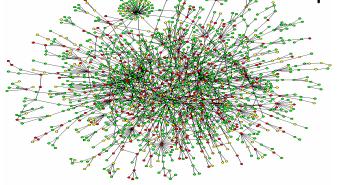
Complex folded-up shapes that:

- Fit together, dock, undock.
- Excite/unexcite, warp each other.
- Bring together, catalyze, transform materials.
- Form complex aggregates and networks.



• Mapping out such networks:

- In principle, it's "just" a very large set of chemical equations.
- Notations have been developed to summarize and abstract.

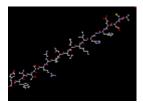


An actual molecular interaction network.

(Nodes are distinct protein kinds, arcs mean that two kinds of proteins interact.)

Protein Structure

Primary

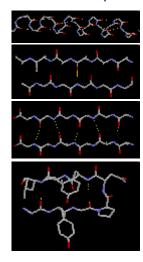


The 20 Aminoacids



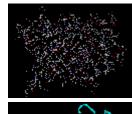
Tryptophan

Secondary



Alpha Helix, Beta Sheet

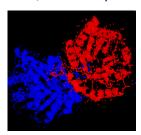
Tertiary





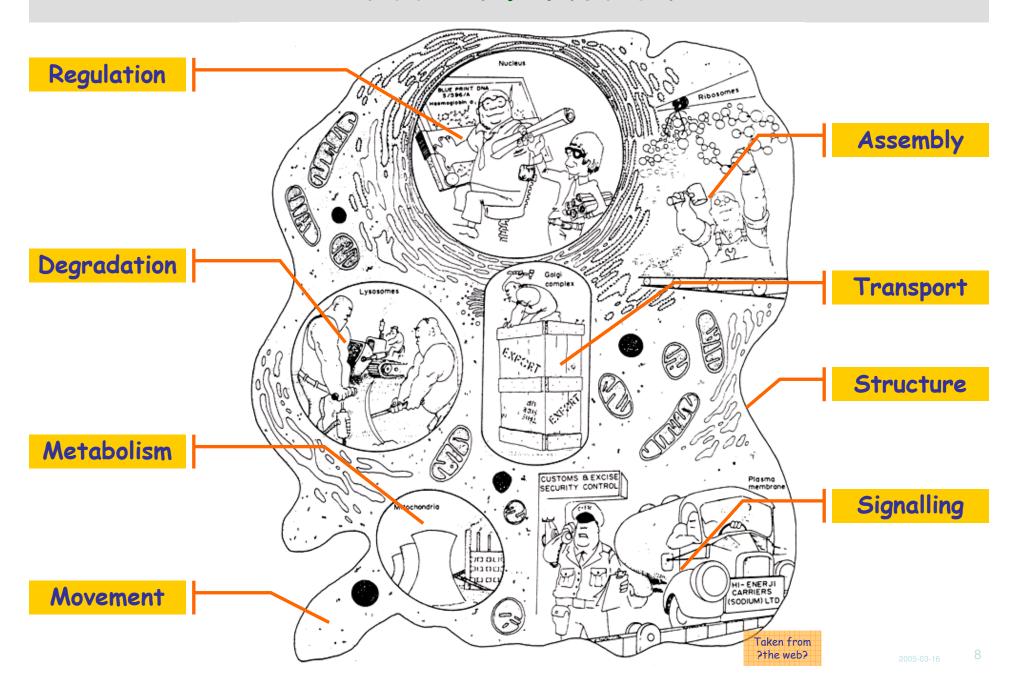
Green Fluorescent Protein

Quaternary

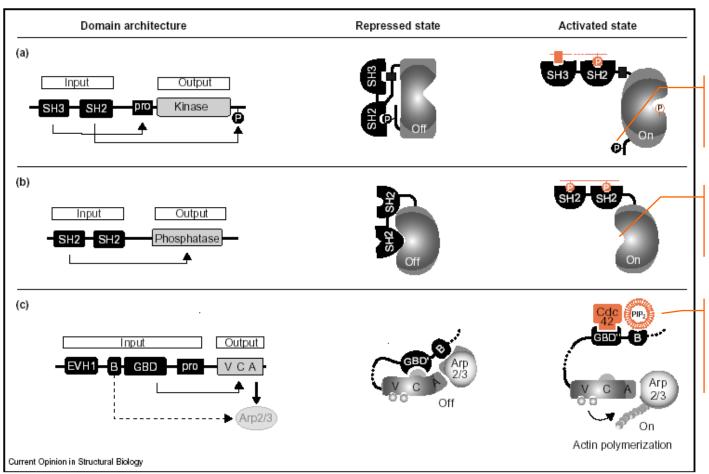


Triose Phosphate Isomerase

Protein Function



Some Allosteric Switches



Domain architecture and autoinhibitory interactions in modular switch proteins. (a) Src family kinases contain N-terminal SH3 and SH2 domains, and a kinase domain flanked by intramolecular SH3-binding and SH2-binding sites (when the C-terminal motif tyrosine is phosphorylated by Csk). The crystal structures of several family members show that both intramolecular domain interactions function in concert to lock the kinase in an inactive conformation. Activating stimuli (red) include external SH2 or SH3 ligands. After initial activation, the kinase is maintained in an active state by autophosphorylation of its activation loop. (b) SHP-2 phosphatase contains two SH2 domains and a phosphatase domain. The crystal structure of the phosphatase

shows that the N-terminal SH2 domain participates in an autoinhibitory interaction that directly blocks the phosphatase active site. Binding of external SH2 ligands activates by disrupting the autoinhibitory interaction. (c) N-WASP contains an Enabled VASP homology 1 (EVH1) domain, a B motif, a GBD, a proline-rich segment (pro) and an output region (VCA) that alone binds the Arp2/3 complex and stimulates its actin nucleation activity. The B and GBD motifs are required to repress activity and, by current models, are thought to participate in intracomplex interactions (only the structure of the GBD intramolecular complex for WASP is known). GTP-bound Cdc42 and PIP2 synergistically activate N-WASP.

Allosteric ("other shape") reactions modify accessibility.

Kinase

= donates phosphate P = phosphorilates other proteins

Phosphatase

= accepts phosphate P = dephosphorilates other proteins

Logical AND

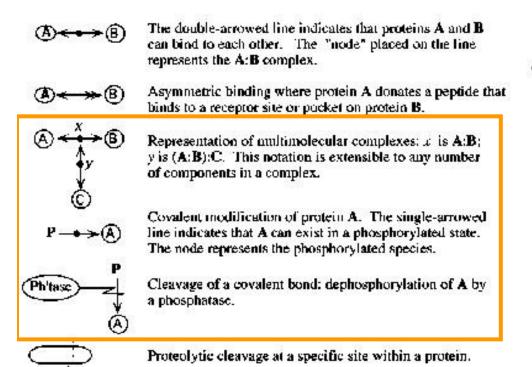
at equal concentrations of the individual input stimuli, activation is much higher if both stimuli are present

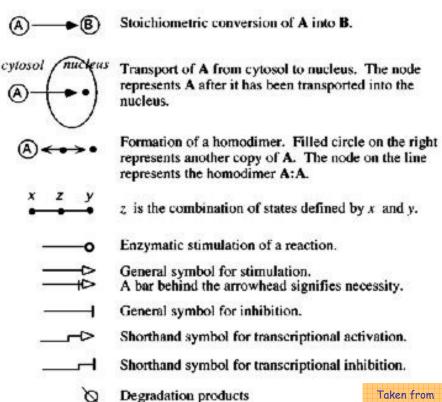
"Phosphatase Kinase Kinase" = a kinase that activates a kinase that activates a phosphatase that deactivates a protein.

Humans have the same number of modular protein domains (building blocks) as worms, but twice the number of multi-domain proteins.

Taken from Wendell Lim

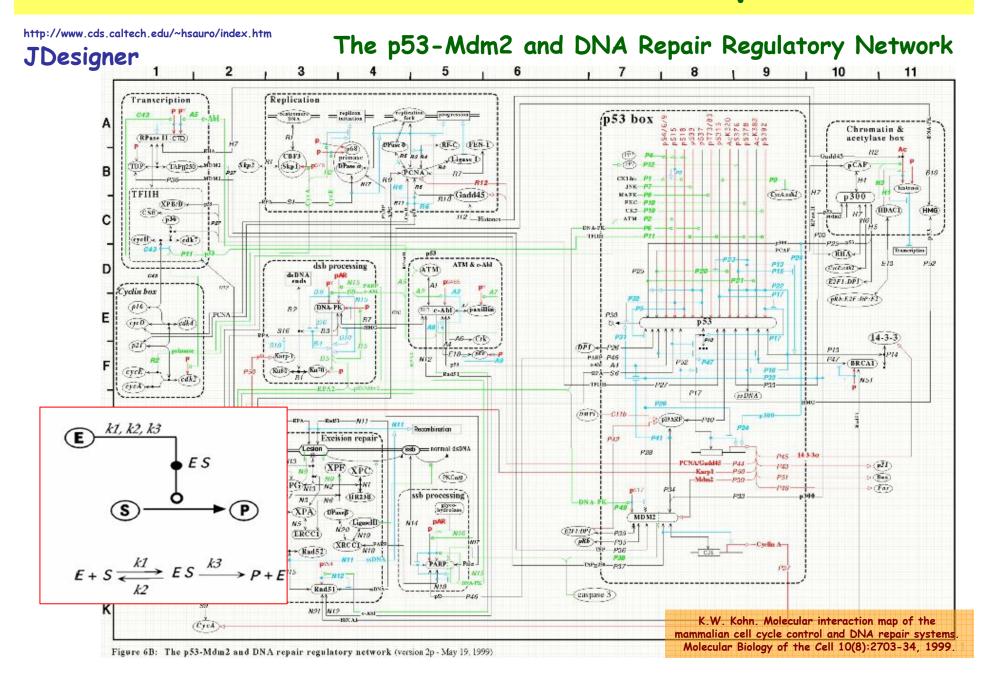
MIM: Molecular Interaction Maps (Kohn)





Kurt W. Kohn

Molecular Interaction Maps



The Protein Machine "Instruction Set"

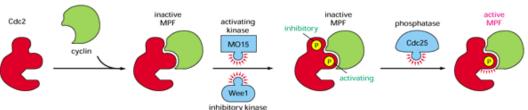
On/Off switches

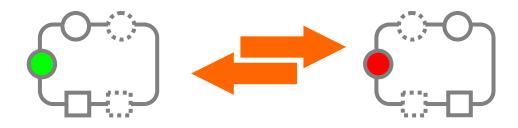
| Inaccessible | In

Binding Sites

cf. BioCalculus [Kitano&Nagasaki], κ-calculus [Danos&Laneve]

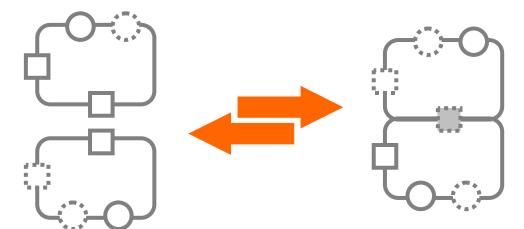
Each protein has a structure of binary switches and binding sites. But not all may be always accessible.





Switching of accessible switches.

- May cause other switches and binding sites to become (in)accessible.
- May be triggered or inhibited by nearby specific proteins in specific states.



Binding on accessible sites.

- May cause other switches and binding sites to become (in)accessible.
- May be triggered or inhibited by nearby specific proteins in specific states.

Notations for the Protein Machine

• Stochastic π -Calculus

- Priami (following Hillston's PEPA) formalizes a stochastic version of p-calculus where channels have communication *rates*.

BioSPi

- Regev-Shapiro-Silverman propose modeling chemical interactions (exchange of electrons and small molecules) as "communication".
- Standard stochastic simulation algorithms (Gillespie) can be used to run in-silico experiments.
- Complex formation is encoded via p-restriction.

PEPA

Calder Gilmore and Hillston model the ERK pathway.

k-calculus

 Danos and Laneve (following Kitano's BioCalculus) define a calculus where complex formation is primitive.

• (Stochastic) Petri Nets

- S.Reddy'94 modeling pathways.
- Srivastava Perterson and Bentley analyze and simulate E.coli stress response circuit.

Bio State Charts

- Harel uses State Charts to model biological interactions via a semi-graphical FSM notation.

Pathway Logic

Talcott-Eker-Knapp-Lincoln use term-rewriting.

BioCham

 ChabrierRivier-Fages-Soliman use term-rewriting and CLT modelchecking.

Kohn Diagrams, Kitano Diagrams

- SBML (Systems Biology Markup Language)
 - XML dialect for MIM's:
 - Compartments (statically nested)
 - Reagents with concentrations
 - Reactions with various rate laws
 - Read and written by many tools via the Systems Biology Workbench protocol

MAPK Cascade

Ultrasensitivity in the mitogen-activated protein cascade, Chi-Ying F. Huang and James E. Ferrell, Jr., 1996, Proc. Natl. Acad. Sci. USA, 93, 10078-10083.

Reservoirs

Biochemistry: Huang and Ferrell

Proc. Natl. Acad. Sci. USA 93 (1996)

Table 2. Predicted Hill coefficients for MAP kinase cascade components: Varying the assumed K_m values

| | | Range of effective Hill coefficients (nH) predicted for | | |
|--------------------------------------|-----------------------------------|---|---------|-----------|
| | Range of assumed K_m | | | |
| Reaction | values | MAPKKK | MAPKK | MAPK |
| MAPKKK → MAPKKK* | 60-1500 nM | 1.0 | 1.7 | 4.9 |
| MAPKKK* → MAPKKK | 60 1500 nM | 1.0 | 1.7 | 4.9 |
| MAPKK → MAPKK-P | 60-1500 nM | 1.0 | 1.3-2.3 | 4.0 - 5.1 |
| MAPKK-P → MAPKK | 60-1500 nM | 1.0 | 1.5-1.9 | 3.6-6.7 |
| 5. MAPKK-P \rightarrow MAPKK-PP | 60-1500 nM | 1.0 | 1.3-2.4 | 3.8-5.2 |
| MAPKK-PP → MAPKK-P | 60-1500 nM | 1.0 | 1.7-1.8 | 4.1 - 6.4 |
| 7. MAPK \rightarrow MAPK-P | 60-1500 nM (300 nM [†]) | 1.0 | 1.7 | 3.7-6.2 |
| 8. MAPK-P \rightarrow MAPK | 60-1500 nM | 1.0 | 1.7 | 4.3-5.2 |
| 9. MAPK-P \rightarrow MAPK-PP | 60-1500 nM | 1.0 | 1.7 | 3.4 - 6.1 |
| 10. MAPK-PP → MAPK-P | 60–1500 nM | 1.0 | 1.7 | 4.7-5.1 |

The assumed K_m values for each reaction were individually varied over the ranges shown, with the assumed K_m values for the other nine reactions held constant. The effective Hill coefficients were calculated from the steepness of the predicted stimulus/response curves, as described in the text.

[†]The K_m value for reaction 7 has been measured to be 300 nM for the phosphorylation of a mammalian MAPK by a MAPKK (N. Ahn, personal communication). All of the other K_m values were initially assumed to be 300 nM as well.

Calculations. Eqs. 1-10 represent the reactions of the MAPK cascade, which are shown schematically in Fig. 1. We have used Goldbeter and Koshland's nomenclature for the rate constantsthe letter a denotes association, d denotes dissociation without catalysis, and k denotes product formation (11). KKK denotes MAPKKK; KK denotes MAPKK; and K denotes MAPK.

$$KKK + E1 \stackrel{a_1}{\rightleftharpoons} KKK \cdot E1 \stackrel{k_1}{\longrightarrow} KKK^* + E1$$
 [1]

$$KKK^* + E2 \xrightarrow{a_2} KKK \cdot E2 \xrightarrow{k_2} KKK + E2$$
 [2

$$KK + KKK^* \stackrel{a_3}{\rightleftharpoons} KK \cdot KKK^* \stackrel{k_3}{\longrightarrow} KK \cdot P + KKK^*$$
 [3]

$$\begin{array}{c} \text{KK-P + KK P'ase} \overset{a_4}{\underset{d_4}{\Longleftrightarrow}} \text{KK-P+KK P'ase} \end{array}$$

$$\stackrel{k_4}{\longrightarrow}$$
 KK + KK P'ase

$$KK-P + KKK^* \underset{d_4}{\Longleftrightarrow} KK-P\cdot KKK^* \xrightarrow{k_5} KK-PP + KKK^*$$
 [5]

KK-PP + KK P'ase
$$\rightleftharpoons$$
 KK-PP·KK P'ase d_6

$$k_6 \longrightarrow$$
 KK-P + KK P'ase

$$KK-PP + K \underset{d_7}{\rightleftharpoons} KK-PP \cdot K \xrightarrow{k_7} KK-PP + K-P$$
 [7]

$$K\text{-}P + K \; P' \text{ase} \overset{a_8}{\underset{d_8}{\Longleftrightarrow}} K\text{-}P\text{+}K \; P' \text{ase} \overset{k_8}{\longrightarrow} K + K \; P' \text{ase} \qquad [8]$$

$$\begin{array}{c} \text{K-P} + \text{KK-PP} \overset{a_9}{\Longleftrightarrow} \text{K-P\cdot KK-PP} \overset{k_9}{\longrightarrow} \text{K-PP} + \text{KK-PP} \quad \text{[9]} \end{array}$$

K-PP + K P'ase
$$\stackrel{a_{10}}{\longleftrightarrow}$$
 KK-PP·K P'ase k_{10}

[10]

10 chemical reactions

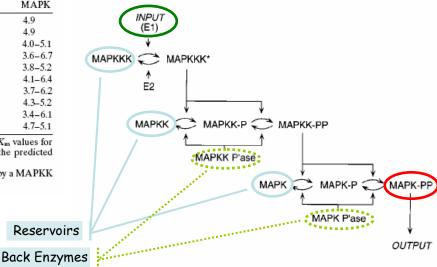


Fig. 1. Schematic view of the MAPK cascade. Activation of MAPK depends upon the phosphorylation of two conserved sites [Thr-183 and Tyr-185 in rat p42 MAPK/Erk2 (4, 5)]. Full activation of MAPKK also requires phosphorylation of two sites [Ser-218 and Ser-222 in mouse Mek-1/MKK1 (6–10)]. Detailed mechanisms for the activation of various MAPKKKs (e.g., Raf-1, B-Raf, Mos) are not vet established; here we assume that MAPKKKs are activated and inactivated by enzymes we denote E1 and E2. MAPKKK* denotes activated MAPKKK. MAPKK-P and MAPKK-PP denote singly and doubly phosphorylated MAPKK, respectively. MAPK-P and MAPK-PP denote singly and doubly phosphorylated MAPK. P'ase denotes phosphatase.

As 18 Ordinary Differential Equations Plus 7 conservation equations

[25]

[26]

[31]

$$\frac{d}{dt}[KKK] = -a_1[KKK][E1] + d_1[KKK \cdot E1]$$

$$+ k_2[KKK^* \cdot E2]$$
[11]

$$\frac{d}{dt}[KKK \cdot E1] = a_1[KKK][E1] - (d_1 + k_1)[KKK \cdot E1]$$
 [12]

$$\begin{split} &\frac{d}{dt}[KKK^*] = -a_2[KKK^*][E2] + d_2[KKK^*\cdot E2] \\ &+ k_1[KKK \cdot E1] + (k_3 + d_3)[KK \cdot KKK^*] - a_3[KKK^*][KK] \\ &+ (k_5 + d_5)[KK \cdot P \cdot KKK^*] - a_5[KK \cdot P][KKK^*] \quad [13] \end{split}$$

$$\frac{d}{dt}[KKK^*\cdot E2] = a_2[KKK^*][E2] - (d_2 + k_2)[KKK^*\cdot E2]$$
 [14]

$$\frac{d}{dt}[KK] = -a_3[KK][KKK^*] + d_3[KK \cdot KKK^*]$$

$$+ k_4[KK \cdot P \cdot KK P' ase]$$
[1:

$$\frac{d}{dt}[KK\cdot KKK^*] = a_3[KK][KKK^*]$$

$$- (d_3 + k_3)[KK \cdot KKK^*]$$
 [16]

$$\frac{d}{dt}[KK-P] = -a_4[KK-P][KK P'ase] + d_4[KK-P\cdot KK P'ase]$$

$$+ k_3[KK \cdot KKK^*] + k_6[KK-PP \cdot KK P'ase]$$

$$+ d_5[KK-P \cdot KKK^*] - a_5[KK-P][KKK^*] \quad [17]$$

+
$$d_5[KK-P\cdot KKK^*]$$
 - $a_5[KK-P][KKK^*]$ [17]

$$\frac{d}{dt}[KK-P\cdot KK P'ase] = a_4[KK-P][KK P'ase]$$

$$- (d_4 + k_4)[KK-P \cdot KKP'ase]$$
 [18]

$$\frac{d}{dt}[KK-P\cdot KKK^*] = a_5[KK-P][KKK^*]$$

$$- (d_5 + k_5)[KK-P \cdot KKK^*]$$
 [19]

$$\frac{d}{dt} [KK-PP] = k_5[KK-P\cdot KKK^*] - a_6[KK-PP][KK P'ase] + d_6[KK-PP \cdot KK P'ase] - a_7[KK-PP][K] + (d_7 + k_7)[K \cdot KK-PP] + (d_9 + k_5)[K-P \cdot KK-PP]$$

$$-a_{9}[K-P][KK-PP]$$
 [20]

$$\frac{d}{dt} [KK-PP\cdot KK P'ase] = a_6 [KK-PP] [KK P'ase]$$

$$- (d_6 + K_6) [KK-PP\cdot KK P'ase]$$
 [21]

$$\frac{d}{dt}[K] = -a_7[K][KK-PP] + d_7[K\cdot KK-PP] + k_8[K-P\cdot KP'ase]$$
[22]

$$\frac{d}{dt}[K\cdot KK-PP] = a_7[K][KK-PP] - (d_7 + k_7)[K\cdot KK-PP]$$

$$\frac{d}{dt}[K-P] = k_7[K-KK-PP] - a_8[K-P][K P'ase]$$

$$+ d_8[K-P \cdot KP'ase] - a_9[K-P][KK-PP]$$

$$+ d_9[K-P \cdot KK-PP] + k_{10}[K-PP \cdot K P'ase]$$
[24]

$$\frac{d}{dt}[\text{K-P-K P'ase}] = a_8[\text{K-P}][\text{K P'ase}]$$

$$\frac{d}{dt}[K-P\cdot KK-PP] = a_9[K-P][KK-PP]$$

$$-(d_9 + k_9)[K-P \cdot KK-PP]$$

 $-(d_8 + k_8)[K-P \cdot KP'ase]$

$$\frac{d}{dt}[K-PP] = -a_{10}[K-PP][K P'ase]$$

+
$$d_{10}[K-PP\cdot KP'ase]$$
 + $k_9[K-P\cdot KK-PP]$ [27]

$$\frac{d}{dt}[K-PP\cdot K P'ase] = a_{10}[K-PP][K P'ase]$$

$$- \ (d_{10} \ + \ k_{10})[K-PP\cdot K\ P'ase] \quad [28]$$

The 10 reactions described above give rise to 18 rate equations.

One equation for each species (8) and complex (10), but not for constant concentration enzymes (4)

$$[E1_{tot}] = [E1] + [KKK \cdot E1]$$
 [30]

$$[E2_{tot}] = [E2] + [KKK*-E2]$$

$$[KK_{tot}] = [KK] + [KK-P] + [KK-PP] + [KK\cdot KKK^*]$$

$$+ [KK-PP \cdot K] + [KK-PP \cdot K-P]$$
 [32]

$$[KK P'ase_{tot}] = [KK P'ase] + [KK P'ase \cdot KK - P]$$

$$[K_{tot}] = [K] + [K-P] + [K-PP] + [KK-PP-K]$$

$$+ \ \textit{KK-PP} \cdot \textit{K-P}] \ + \ [\textit{K-P} \cdot \textit{KP'ase}] \ + \ [\textit{K-PP} \cdot \textit{KP'ase}] \ \ [34]$$

$$[K P'ase_{tot}] = [K P'ase] + [K-P \cdot K P'ase]$$

+
$$[K-PP \cdot K P'ase]$$
 [35]

These equations were solved numerically using the Runge-Kutta-based NDSolve algorithm in Mathematica (Wolfram Research, Champaign, IL). An annotated copy of the Mathematica code for the MAPK cascade rate equations can be obtained from J.E.F. In addition, there are seven conservation equations (Eqs. 29-35).

$$[KKK_{tot}] = [KKK] + [KKK*] + [KKK*E1]$$

$$+ [KKK* \cdot E2]$$

$$+ [KKK* \cdot K] + [KKK* \cdot K-P]$$
 [29]
in exactly one state

As 12 processes (in SPiM)

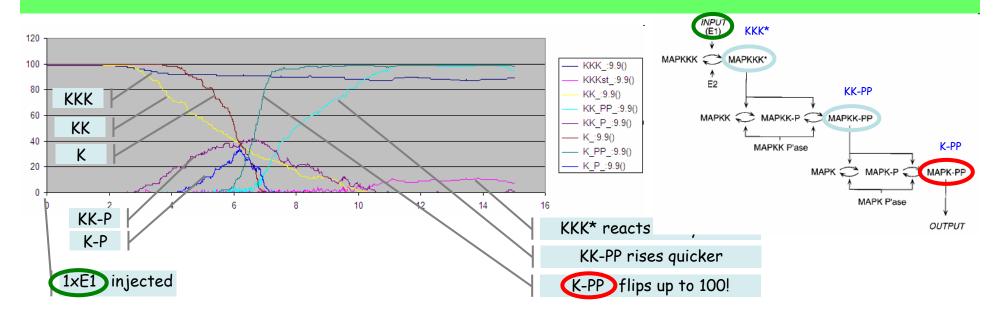
```
let KKK() =
                                                                  and KK PP() =
                                                                     (new u6@d6:Release
  (new u1@d1:Release
  !a1(u1); (do !u1;KKK() or !k1;KKKst()))
                                                  [1]substrate
                                                                     do !a6(u6); (do !u6;KK PP() or !k6;KK P())
                                                                                                                      [6]substrate
                                                                     or ?a7(u7): (da
                                                                                                                      [7]kinase
                          KKK:E1 complex
                                                                                  One process for each
and KKKst() =
                                                                     or ?a9(u9); (d
                                                                                                                      [9]kinase
                                                                                  component (12) including
  (new u2@d2:Release
                                                                                  enzymes, but not for
                                                                  and KKPse() =
  do !a2(u2); (do !u2;KKKst() or !k2;KKK())
                                                  [2]substrate
                                                                                  complexes.
  or ?a3(u3); (do ?u3;KKKst() or ?k3;KKKst())
                                                  [3]kinase
                                                                    do ?a4(u4); (du .u-, .xxxxx sc/, vr .xx-, xxxx sc//
                                                                                                                      [4]phtase
  or ?a5(u5); (do ?u5;KKKst() or ?k5;KKKst()))
                                                  [5]kinase
                                                                    or ?a6(u6); (do ?u6;KKPse() or ?k6;KKPse())
                                                                                                                      [6]phtase
let E1() =
                                                                              No need for conservation
                                                                  let K() =
  ?a1(u1); (do ?u1;E1() or ?k1;E1())
                                                                    (new u7@ requations: implicit in "choice"
                                                  [1]enzyme
                                                                     !a7(u7); (coperator in the calculus.
                                                                                                                      [7]substrate
                   E1:KKK complex
let E2() =
  ?a2(u2); (do ?u2;E2() or ?k2;E2())
                                                  [2]enzyme
                                                                  and KP() =
                                                                     (new u8@d8:Release new u9@d9:Release
let KK() =
                                                                     do !a8(u8); (do !u8;K_P() or !k8;K())
                                                                                                                      [8]substrate
  (new u3@d3:Release
                                                                     or !a9(u9); (do !u9;K_P() or !k9;K_PP()))
                                                                                                                      [9]substrate
  !a3(u3); (do !u3;KK() or !k3;KK_P()))
                                                  [3]substrate
                                                                  and K PP() =
and KK P() =
                                                                     (new u10@d10:Release
  (new u4@d4:Release new u5@d5:Release
                                                                     !a10(u10); (do !u10;K_PP() or !k10;K_P()))
                                                                                                                      [10]substrate
  do !a4(u4); (do !u4;KK_P() or !k4;KK())
                                                   [4]substrate
  or !a5(u5); (do !u5;KK_P() or !k5;KK_PP()))
                                                  [5]substrate
                                                                  and KPse() =
                                                                    do ?a8(u8); (do ?u8;KPse() or ?k8;KPse())
                                                                                                                      [8]phtase
                                                                    or ?a10(u10); (do ?u10;KPse() or ?k10;KPse())
                                                                                                                      [10]phtase
```

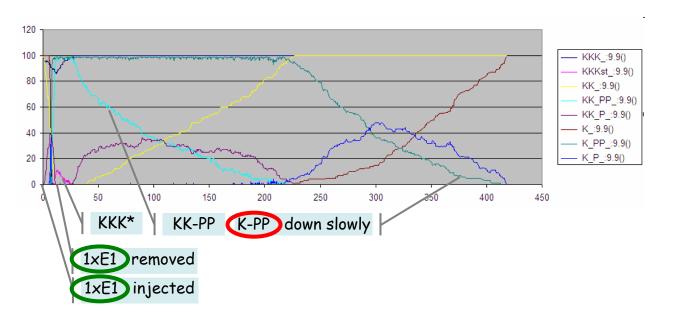
... and 20 Interaction Channels

```
type Release = chan()
type Bond = chan(Release)
type React = chan()
new a1@1.0:Bond val d1=1.0 new k1@1.0:React
new a2@1.0:Bond val d2=1.0 new k2@1.0:React
new a3@1.0:Bond val d3=1.0 new k3@1.0:React
new a4@1.0:Bond val d4=1.0 new k4@1.0:React
new a5@1.0:Bond val d5=1.0 new k5@1.0:React
new a6@1.0:Bond val d6=1.0 new k6@1.0:React
new a7@1.0:Bond val d7=1.0 new k7@1.0:React
new a8@1.0:Bond val d8=1.0 new k8@1.0:React
new a9@1.0:Bond val d9=1.0 new k9@1.0:React
new a10@1.0:Bond val d10=1.0 new k10@1.0:React
• • •
run 100 of KKK() run 100 of KK() run 100 of K()
run 1 of E2() run 1 of KKPse() run 1 of KPse()
run 1 of E1()
```

a_i,k_i: Two channels for each reversible chemical reaction of 2 molecules. (No behaavior attached to channels except interaction rate.)

MAPK Cascade Simulation in SPiM

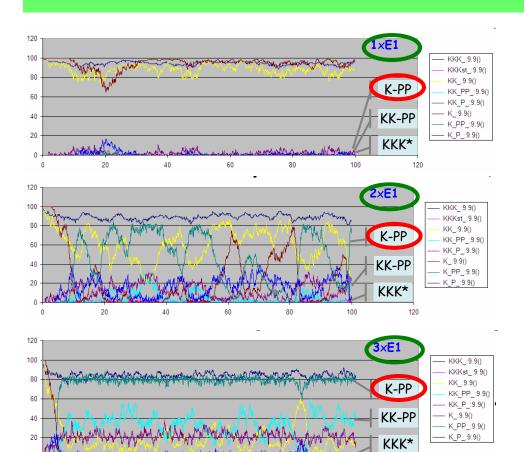


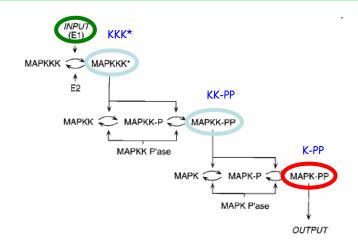


All coefficients 1.0 !!! 100×KKK, 100×KK, 100×KK, 100×KK, 1xE2, 1xKKPse, 1xKPse.

Input is 1xE1.
Output is 100xK-PP (ultrasensitivity).

MAPK Cascade Simulation in SPiM



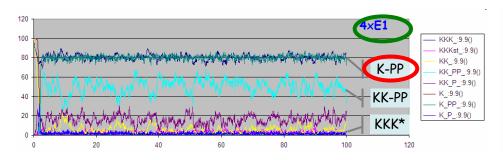


All coefficients 1.0 !!!

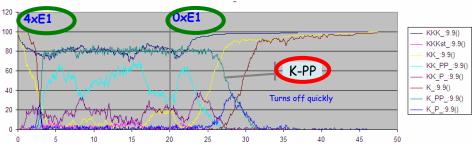
100×KKK, 100×KK, 100×K,

10×E2, 10×KKPse, 10×KPse.

(so 1×E1 is no longer sufficient to produce an output)



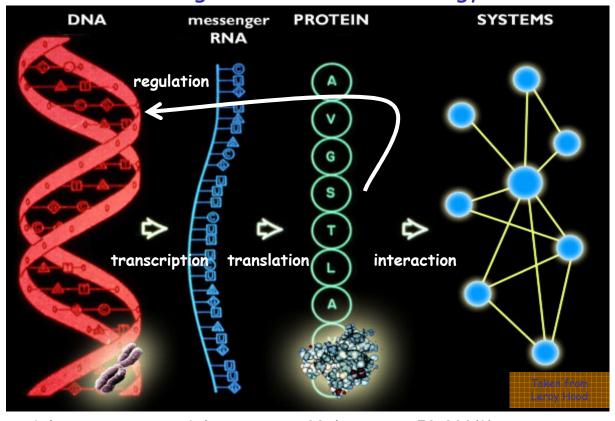
100



2. The Gene Machine

Pretty far from the atoms.

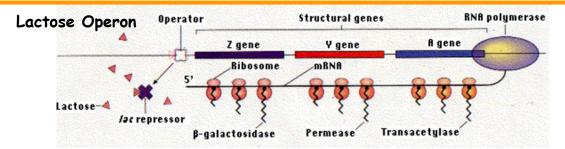
The "Central Dogma" of Molecular Biology

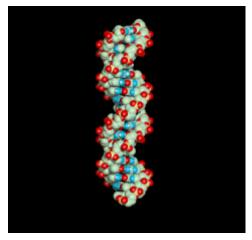


4-letter digital code

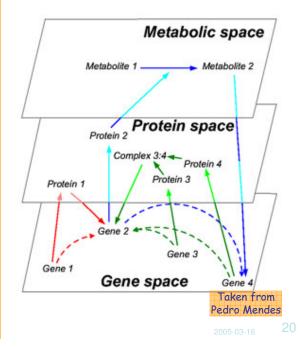
4-letter digital code

20-letter digital code 50.000(?) shapes



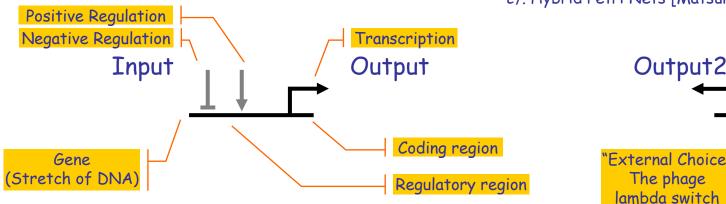


DNA Tutorial



The Gene Machine "Instruction Set"

cf. Hybrid Petri Nets [Matsuno, Doi, Nagasaki, Miyano]



Output2

"External Choice"
The phage lambda switch

Regulation of a gene (positive and negative) influences transcription. The regulatory region has precise DNA sequences, but not meant for coding proteins: meant for binding regulators.

Transcription produces molecules (RNA or, through RNA, proteins) that bind to regulatory region of other genes (or that are end-products).

Human (and mammalian) Genome Size

3Gbp (Giga base pairs) 750MB @ 4bp/Byte (CD)

Non-repetitive: 16bp 250MB

In genes: 320Mbp 80MB Coding: 160Mbp 40MB

Protein-coding genes: 30,000-40,000

M.Genitalium (smallest true organism)

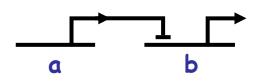
580,073bp 145KB (eBook)

E.Coli (bacteria): 4Mbp 1MB (floppy)

Yeast (eukarya): 12Mbp 3MB (MP3 song)

Wheat 176bp 4.256B (DVD)

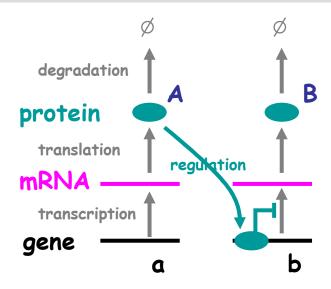
Gene Composition



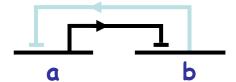
Is a shorthand for:

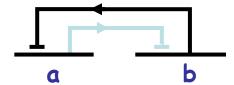
Under the assumptions [Kim & Tidor]

- 1) The solution is well-stirred (no spatial dependence on concentrations or rates).
- 2) There is no regulation cross-talk.
- 3) Control of expression is at transcription level only (no RNA-RNA or RNA-protein effects)
- 4) Transcriptions and translation rates monotonically affect mRNA and protein concentrations resp.

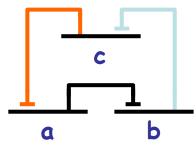


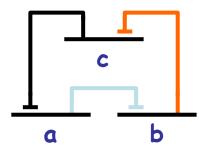
Ex: Bistable Switch

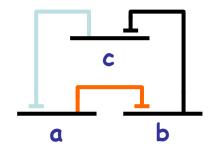




Ex: Oscillator







Expressed
Repressed
Expressing

Indirect Gene Effects

No combination of standard high-throughput experiments can reconstruct an a-priori known gene/protein network [Wagner].

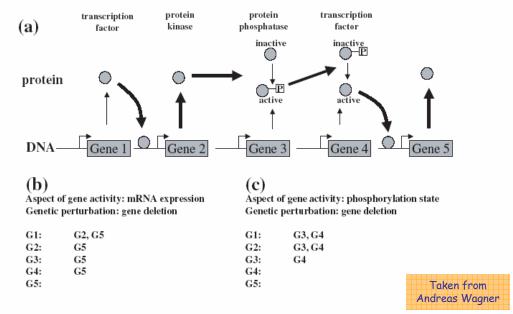
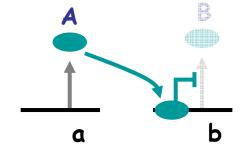
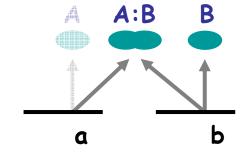


Fig. 1. The importance of specifiying gene activity when reconstructing genetic networks. (a) A hypothetical biochemical pathway involving two transcription factors, a protein kinase, and a protein phosphatase, as well as the genes encoding them. See text for details. (b) Shown is a list of perturbation effects for each of the five genes in (a), when perturbing individual genes by deleting them, and when using mRNA expression level as an indicator of gene activity. The left-most symbol in each line stands for the perturbed gene. To the right of each colon is a list of genes whose activity is affected by the perturbation. (c) Analogous to (b) but for a different notion of gene activity (phosphorylation state).

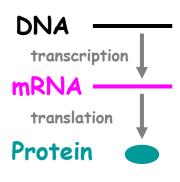
One of many bistable switches that cannot be described by pure gene regulatory networks [Francois & Hakim].





Structure of the Coding Region

The Central Dogma

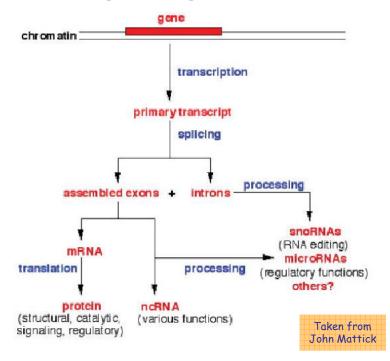


RNA is not just an intermediary; it can:

- Fold-up like a protein
- Act like an enzyme
- Regulate other transcribed RNA
- Direct protein editing

- ...

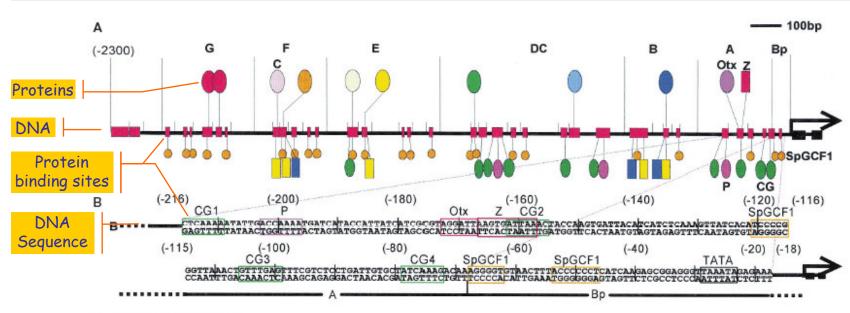
Challenging the Dogma (in higher organisms)



97-98% of the transcriptional output of the human genome is non-protein-coding RNA.

30-40,000 "protein genes" (1.5% of genome) 60-100,000 "transcription units" (>30% of genome is transcribed)

Structure of a Regulatory Region



2300bp!

> average protein

Module A functions:

Vegetal plate expression in early development:

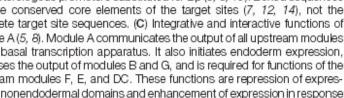
Synergism with modules B and G enhancing endoderm expression in later development:

Repression in ectoderm (modules E and F) and skeletogenic mesenchyme (module DC):

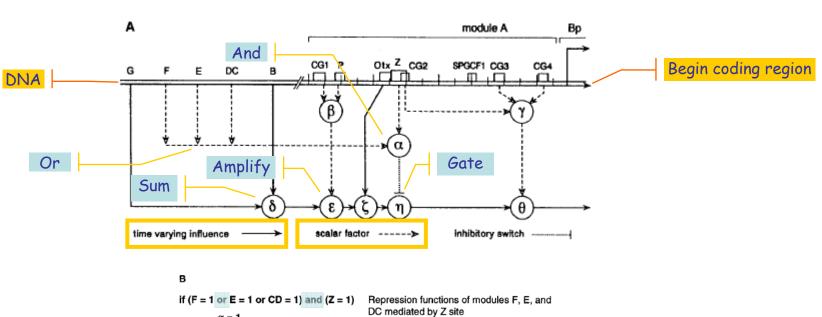
Modules E, F and DC with LiCI treatment:

Fig. 1. Endo16 cis-regulatory system and interactive roles of module A. (A) Diversity of protein binding sites and organization into modular subregions [modified from (7)]. Specific DNA binding sites are indicated as red blocks: modular subregions are denoted by letters G to A (Bp, basal promoter). Proteins binding at the target sites considered in this work are indicated: Otx. SpOtx-1 (12); SpGCF1 (14); the proteins CG, Z, and P, which are not yet cloned; and protein C [a CREB family protein (18)] in subregion F. Proteins for which sites occur in multiple regions of the DNA sequence (indicated by the black line) are shown beneath. (B) Sequence of module A and location of protein binding sites. Sites are indicated in the same colors as in (A). A fragment containing CG2 and CG3 sites as well as Bp has no endoderm-

specific activity and services other upstream cis-regulatory systems promiscuously; similarly, the Endo16 cis-regulatory system functions specifically with heterologous promoters substituted for Bp (5, 8, 19). Boxed sequences indicate conserved core elements of the target sites (7, 12, 14), not the complete target site sequences. (C) Integrative and interactive functions of module A (5, 8). Module A communicates the output of all upstream modules to the basal transcription apparatus. It also initiates endoderm expression. increases the output of modules B and G, and is required for functions of the upstream modules F, E, and DC. These functions are repression of expression in nonendodermal domains and enhancement of expression in response to LiCI.



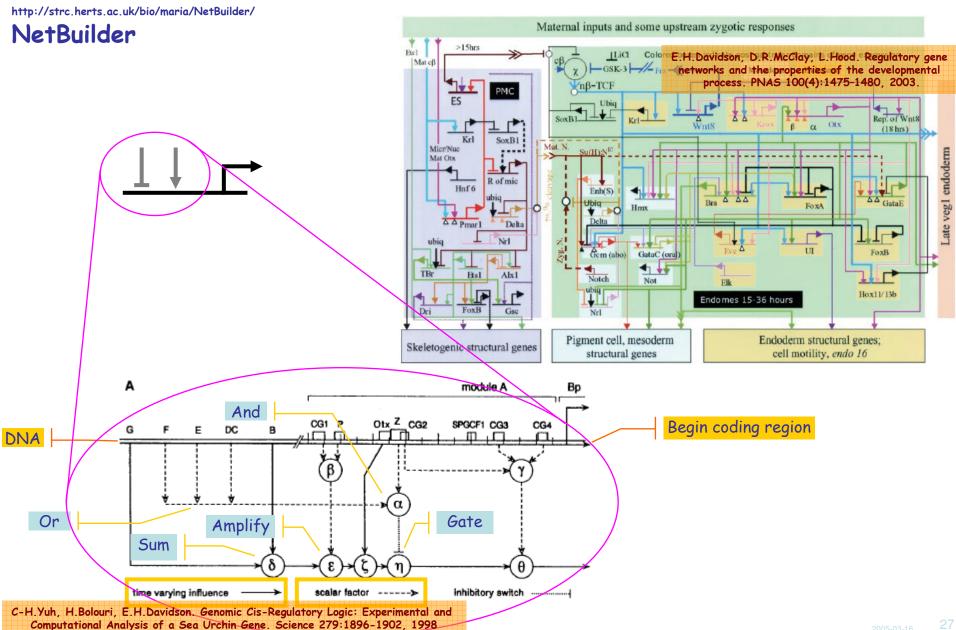
Function of a Regulatory Region



```
\alpha = 1
else
          \alpha = 0
if (P = 1 and CG, = 1)
                                                  Both P and CG, needed for synergistic link
                                                  with module B
          \beta = 2
         \beta = 0
if (CG, = 1 and CG, = 1 and CG, = 1)
                                                  Final step up of system output
          \gamma = 2
       \gamma = 1
\delta(t) = B(t) + G(t)
                                                  Positive input from modules B and G
\varepsilon(t) = \beta^* \delta(t)
                                                  Synergistic amplification of module B
                                                  output by CG,-P subsystem
                                                  Switch determining whether Otx site in
if (\varepsilon(t) = 0)
                                                  module A, or upstream modules (i.e.,
          \xi(t) = Otx(t)
                                                  mainly module B), will control level of
else
          \xi(t) = \varepsilon(t)
                                                  activity
if (\alpha = 1)
                                                  Repression function inoperative in
                                                  endoderm but blocks activity elsewhere
          \eta(t) = 0
else
         \eta(t) = \xi(t)
\Theta(t) = \gamma^* \eta(t)
                                                  Final output communicated to BTA
```

C-H.Yuh, H.Bolouri, E.H.Davidson. Genomic Cis-Regulatory Logic: Experimental and Computational Analysis of a Sea Urchin Gene. Science 279:1896-1902, 1998

Gene Regulatory Networks



The Programming Model

Strange facts about genetic networks:

- Not an operator algebra. The output of each gate is fixed and pre-determined; it is never a function of the input!
- Not term-rewriting, nor Petri nets. Inhibition is widespread.
- Not Communicating Sequential Processes. Feedback is widespread: asynchronous communication needed to avoid immediate self-deadlocks. Even the simplest gates cannot be modeled as a single synchronous automata.
- Not Message-Passing between genes. Messages themselves have behavior (e.g., they stochastically decay and combine), hence messages are processes as well.
- Not Data-Flow. Any attempt to use data-flow-style modeling seems doomed because
 of widespread loops that lead to deadlocks.

How can it possibly work?

- Stochastic broadcasting. The apparently crude idea of broadcasting a whole bunch of asynchronous decaying messages to activate a future gate, means there are never any "pipeline full" deadlocks, even in presence of abundant feedback loops.
- Stochastic degradation. Degradation is fundamental for system stability, and at the same time can lead to sudden instability and detection of concentration levels.

Notations for the Gene Machine

- Many of the same techniques as for the Protein Machine apply.
 - Process Calculi, Petri Nets, Term-Rewriting Systems...
- But the "programming model" is different.
 - Asynchronous stochastic control.
 - Biologically poorly understood.
 - Network "motifs" are being analyzed.

- Specific techniques:
 - Hybrid Petri Nets
 - [Matsuno, Doi, Nagasaki, Miyano] Gene Regulation
 - Genomic Object Net www.genomicobject.net
- Gene Regulation Diagrams
- Mixed Gene-Protein Diagrams

Gene Gates and Circuits

```
A gene gate \begin{array}{ccc} \textbf{A gene gate} & \text{neg(a,b)} \triangleq \\ \textbf{a} & & \Rightarrow \textbf{b} \\ & & \uparrow \textbf{a_r}; \ \tau_{\eta}; \ \text{neg(a,b)} + \\ & & \tau_{\epsilon}; \ (\text{tr(b)} \mid \text{neg(a,b)}) \\ & & & \text{tr(p)} \triangleq (!p_r; \ \text{tr(p)}) + \tau_{\delta} \end{array}
```

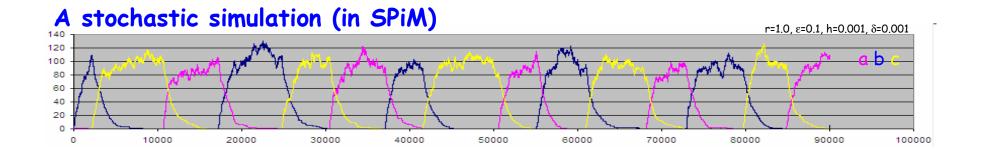
```
A genetic circuit (engineered in E.Coli)

c neg(a,b) |
neg(b,c) |
neg(c,a)

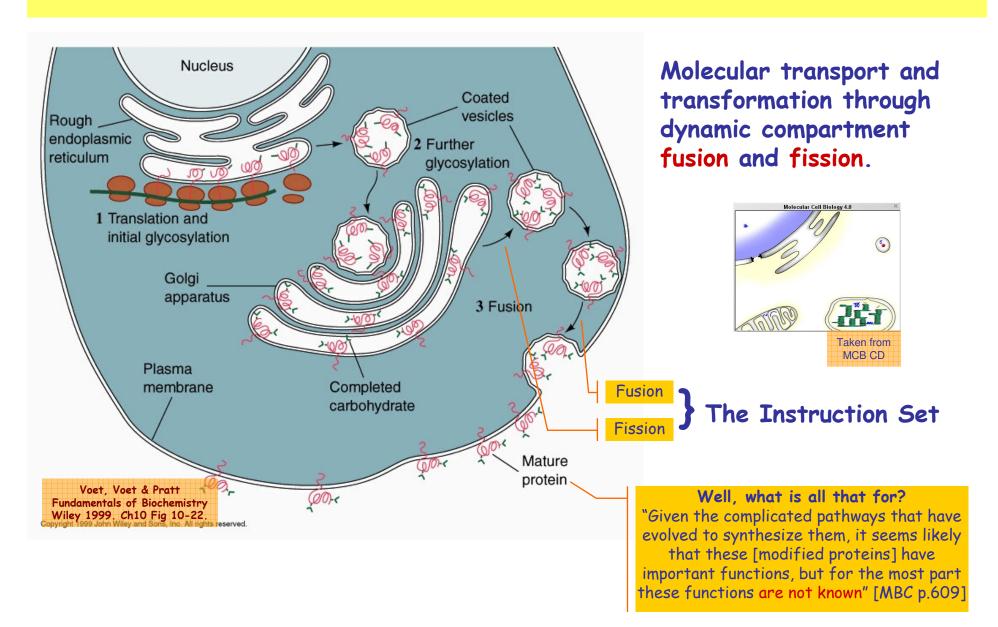
neg
neg
```

The stochastic- π program

```
val dk = 0.001
                  (* Decay rate *)
val inh = 0.001
                 (* Inhibition rate *)
val cst = 0.1
                  (* Constitutive rate *)
let tr(p:chan()) =
   do !p; tr(p) or delay@dk
let neg(a:chan(), b:chan()) =
  do ?a; delay@inh; neg(a,b)
  or delay@cst; (tr(b) | neg(a,b))
(* The circuit *)
val bnd = 1.0
                  (* Protein binding rate *)
new a@bnd:chan() new b@bnd:chan()
run (neg(c,a) \mid neg(a,b) \mid neg(b,c))
```

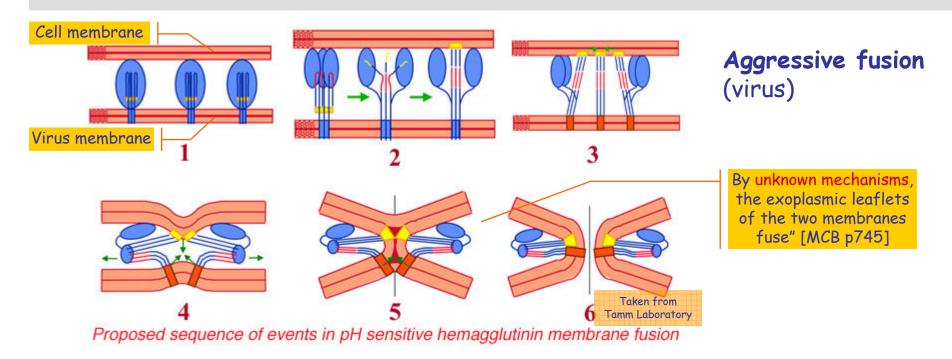


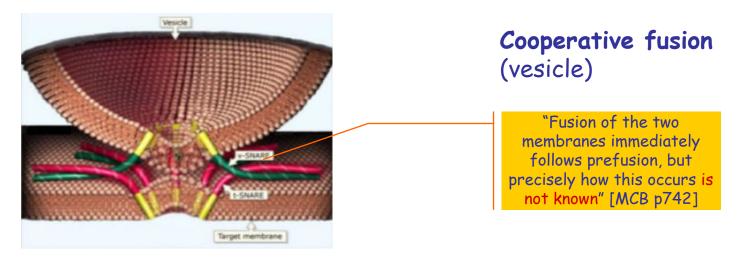
3. The Membrane Machine Very far from the atoms.



Membrane Fusion

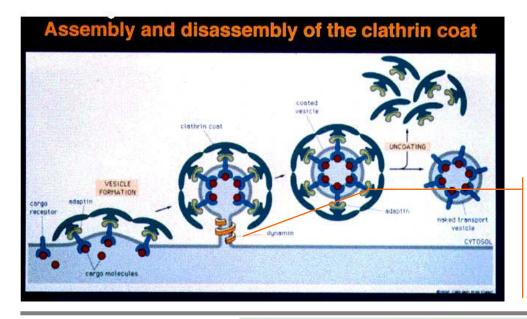
Positive curvature to Negative curvature transition in 3D





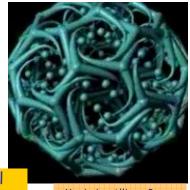
Negative curvature to Positive curvature transition in 3D

Membrane Fission

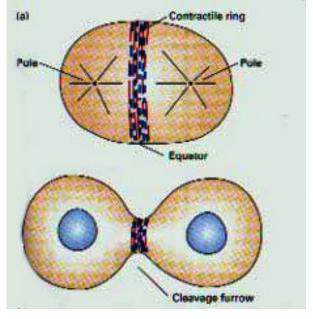


Vesicle Formation

"Nonetheless, the actual process whereby a segment of phospholipid bilayer is 'pinched off' to form a pit and eventually a new vesicle is still not understood" [MCB p.746]

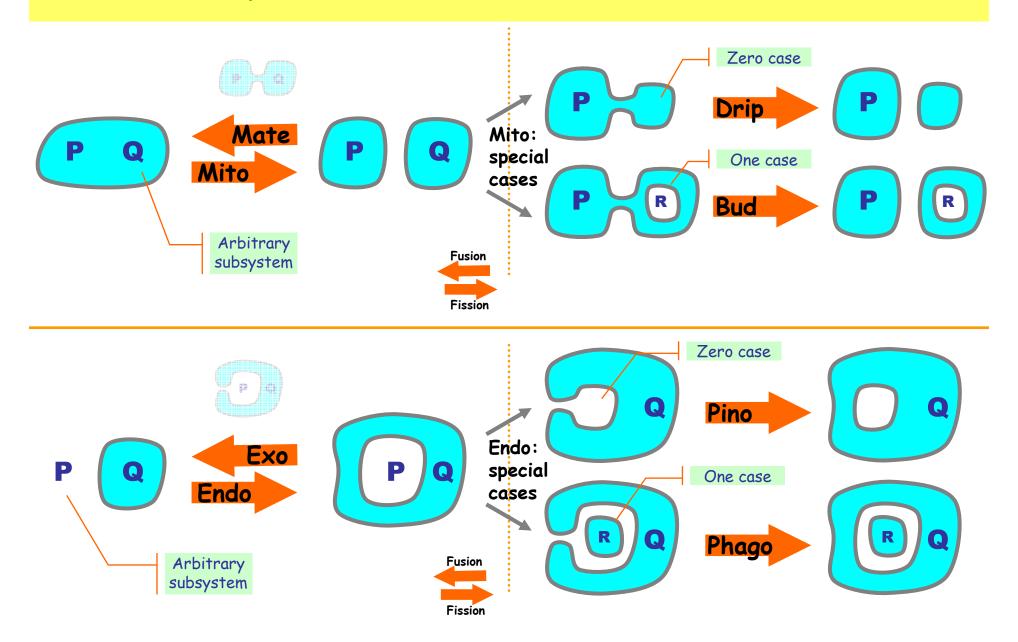


Movie by Allison Bruce

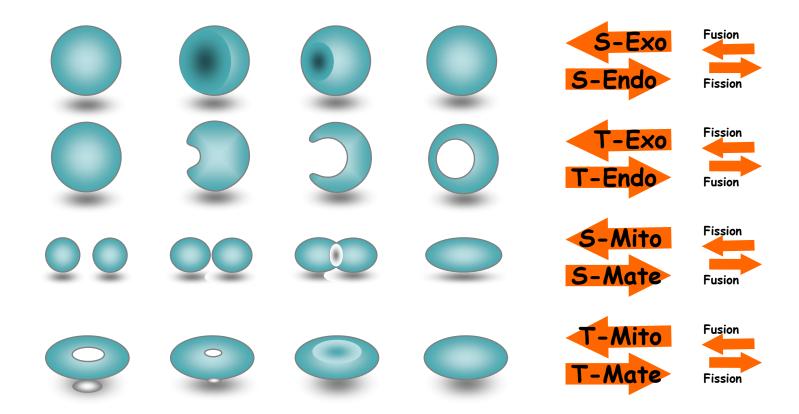


Cytokinesis (Mitosis)

The Membrane Machine "Instruction Set"

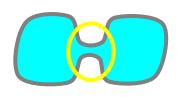


... in 3D

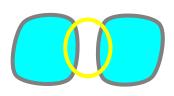


Locally Implementable!

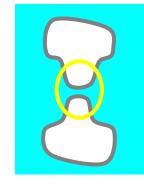
Global Views



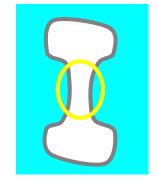




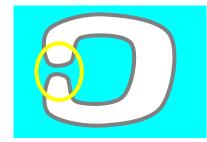
(Fission)



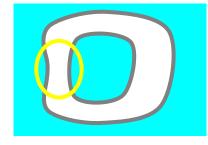




(Fusion)







(Fission)











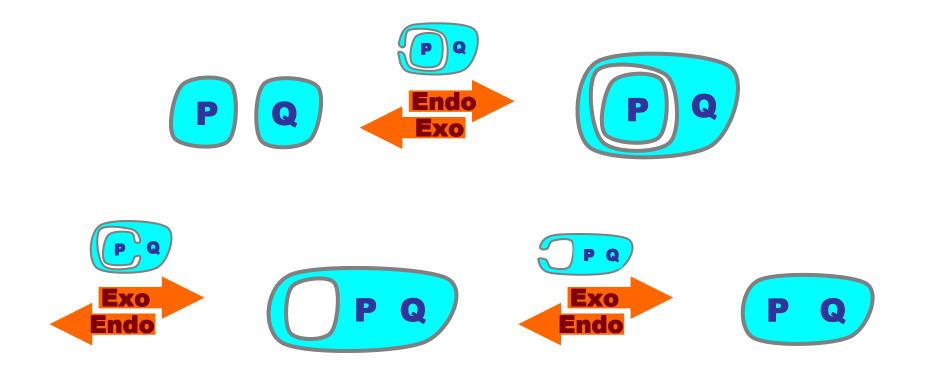






(Fusion)

Mito/Mate by 3 Endo/Exo



Notations for the Membrane Machine

- "Snapshot" diagrams
 - In biology literature.
- P-Systems
 - G.Paun uses ideas from the theory of grammars and formal languages to model "Membrane Computing" (book 2002).
 - http://psystems.disco.unimib.it/.

BioAmbients

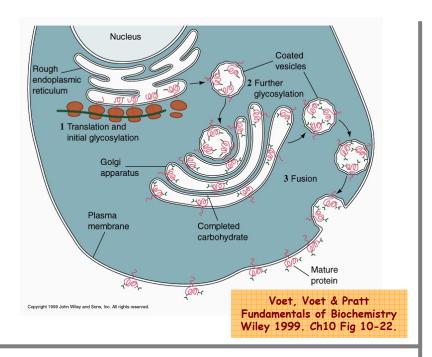
 An extension of BioSPI along Ambient Calculus lines (with more bio-relevant mobility primitives) to model dynamic compartments.

Brane Calculi

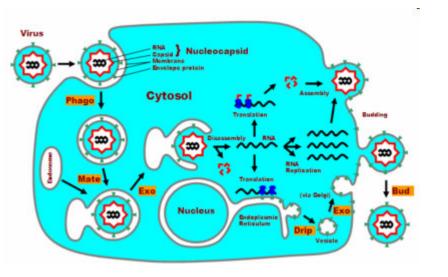
- Computation on the membrane...

Membrane Algorithms

Protein Production and Secretion

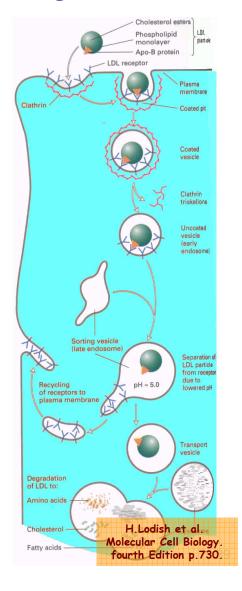


Viral Replication

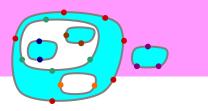


Adapted from: B. Alberts et al.
Molecular Biology of the Cell
third edition p. 279.

LDL-Cholesterol Degradation



Brane Calculi



systems
$$P,Q := \diamond | P \circ Q | !P | \sigma(P)$$

nests of membranes

branes
$$\sigma, \tau := 0 | \sigma | \tau | !\sigma | a.\sigma$$

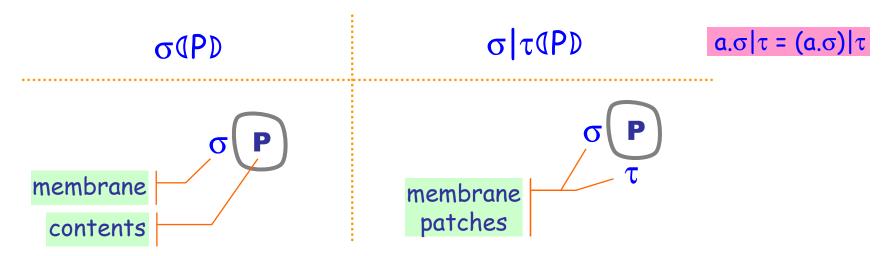
combinations of actions

actions
$$a := 1 | \dots$$

(fill in as needed)

1D fluids (σ) inside a 2D fluid (P)

TWO commutative monoids instead of ONE of normal process calculi



N.B. Restriction (vn) could be added to both systems and branes. It usually would originate in branes, but would extrude to whole systems.

Brane Reactions (Cartoons)

A Turing-Complete language [Busi Gorrieri]

Brane-Molecule Reactions (Cartoons)

With molecule multisets p,q:



•••

Phago
$$\mathfrak{D}_{n}.\sigma|\sigma'(PD) \circ \mathfrak{D}_{n}'(\rho).\tau|\tau'(QD) \to \tau|\tau'(\rho(\sigma|\sigma'(PDD)\circ QD))$$

Exo $\mathfrak{D}_{n}.\tau|\tau'(\mathfrak{D}_{n}.\sigma|\sigma'(PD\circ QD) \to P \circ \sigma|\sigma'|\tau|\tau'(QD)$

Pino $\mathfrak{D}(\rho).\sigma|\sigma'(PD) \to \sigma|\sigma'(\rho(\circ D\circ PD))$

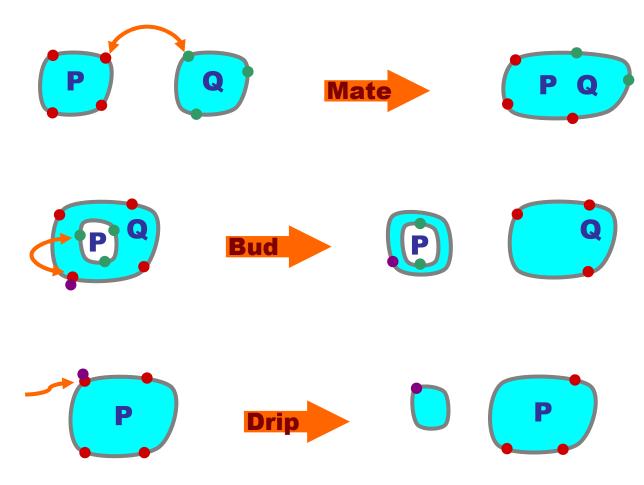
N.B.: the parity of nesting of P and Q is preserved; this makes the reactions preserve bitonality.

B&R
$$p_1 \circ p_1(p_2) \Rightarrow q_1(q_2).\alpha |\sigma(p_2 \circ PD \rightarrow q_1 \circ \alpha |\sigma(q_2 \circ PD))$$

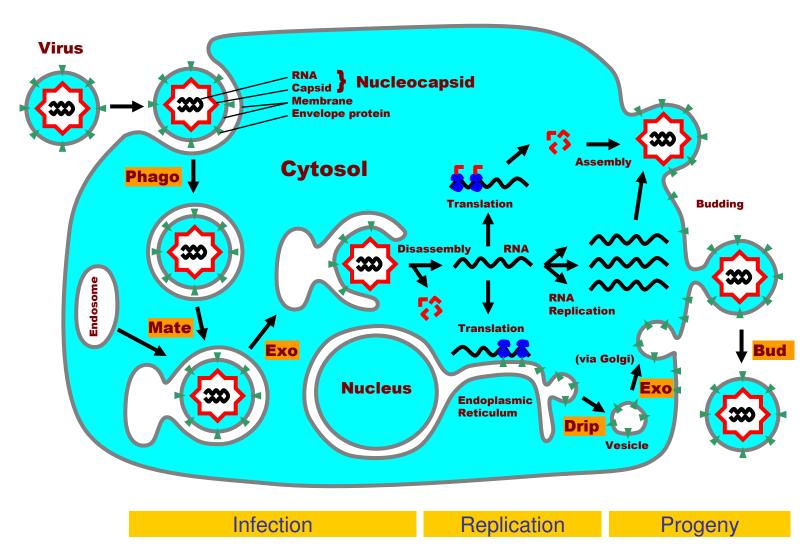
(multiset rewriting, inside and outside membranes)

Derivable Reactions (Cartoons)

A Decidable-Termination language [Busi Gorrieri]



Viral Reproduction

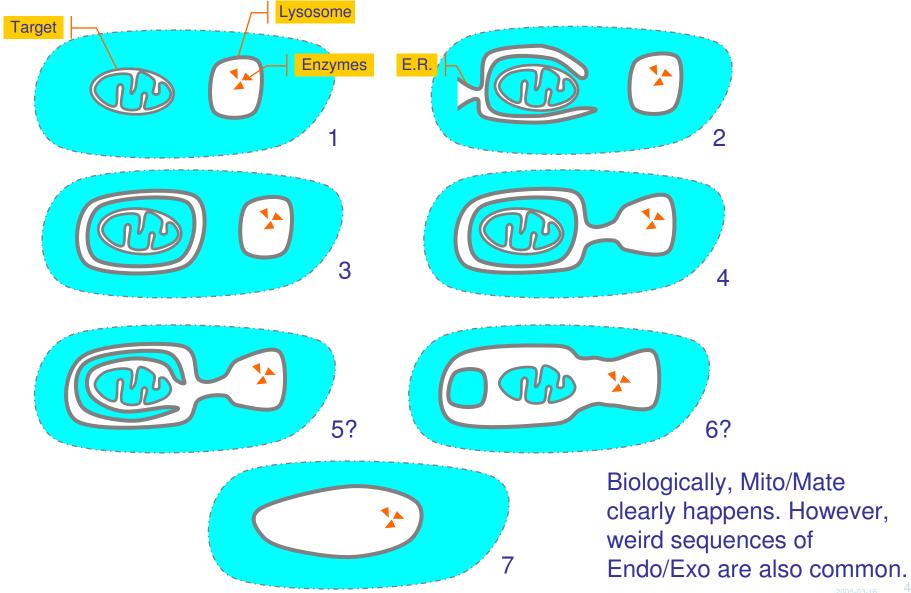


Ex: Viral Progeny

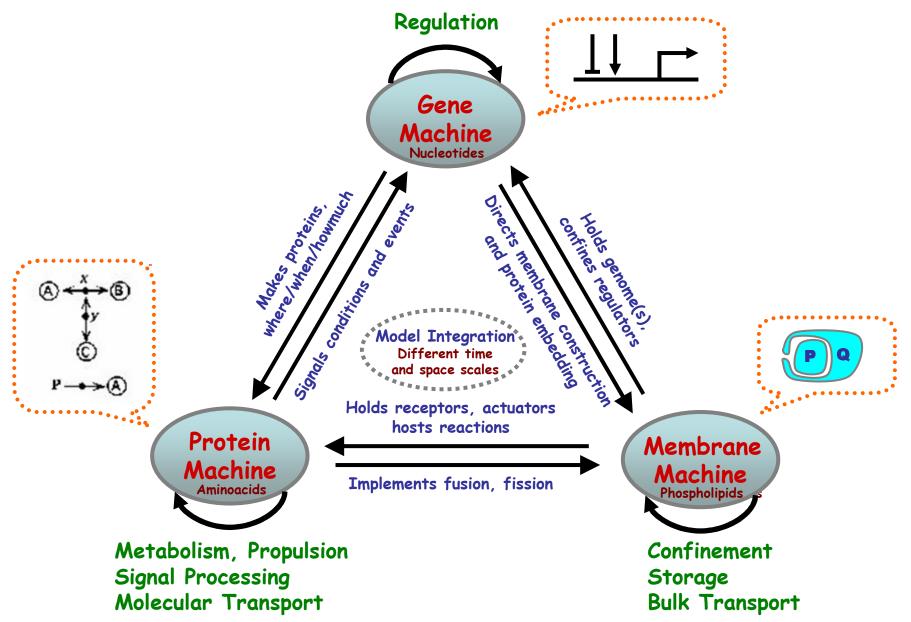
Assume: $nucap \circ cytosol \longrightarrow \longrightarrow nucap^n \circ envelope-vesicle^m \circ cytosol'$ by available cellular machinery Then: cell !o-(o.bud-(o.o)(o)o!bud|σ(vRNA)ocytosol"D envelope vesicle nucap !&+|bud+(&.&)(!bud|σ(vRNA)°cytosol") Bud nugap envelope !S¹(cytosol") ∘ ≥.5(nucap) cell virus

Ex: Autophagic Process

Lysosome and target don't just merge.



Abstract Machines of Systems Biology



Importance of Stochastic Effects

Surprisingly enough, we have found that parameter values that give rise to a stable steady state in the deterministic limit continue to produce reliable oscillations in the stochastic case, as shown in Fig. 5. Therefore, the presence of noise not only changes the behavior of the system by adding more disorder but can also lead to marked qualitative differences.

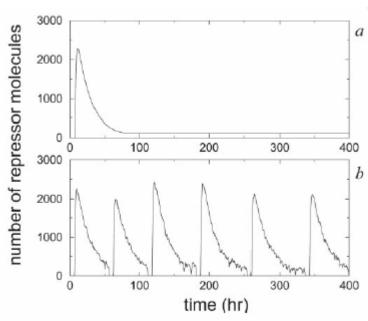


Fig. 5. Time evolution of R for the deterministic Eq. [1] (a) and stochastic (b) versions of the model. The values of the parameters are as in the caption of Fig. 1, except that now we set $\delta_R = 0.05 \, \mathrm{h^{-1}}$. For these parameter values, $\tau < 0$, so that the fixed point is stable.

Mechanisms of noise-resistance in genetic oscillators Jose' M. G. Vilar, Hao Yuan Kueh, Naama Barkai, and Stanislas Leibler

PNAS April 30, 2002 vol. 99 no. 9 5991

Scaling up to Big Systems: ODE's vs Processes

Stochastic π -calculus Executive Summary

A process calculus:

- The modular representation of concurrent (and stochastic) processes of all kinds.
- Cuts down to CTMCs
 (Continuous Time Markov
 Chains) in the finite case (not
 always). Then, standard tools
 are applicable.
- Can be given friendly automatalike scalable graphical syntax (work in progress: Andrew Phillips).
- Is directly executable (e.g. via Gillespie).
- Is analyzable (large body of literature, at least in the non-stochastic case).

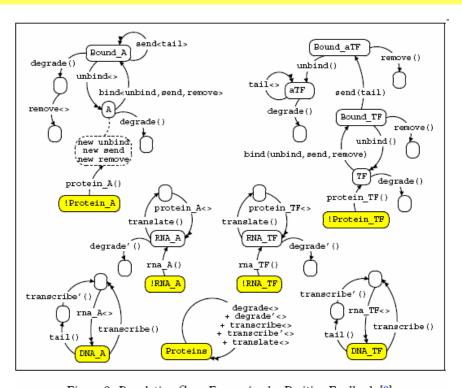


Figure 2. Regulating Gene Expression by Positive Feedback [9]

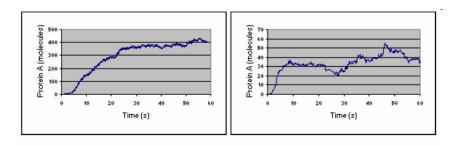
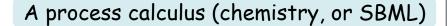


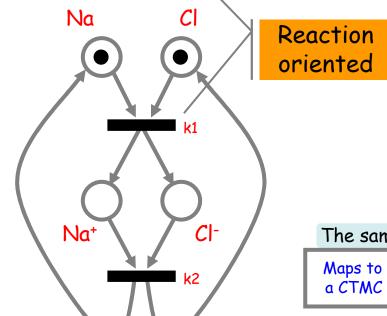
Figure 3. Protein A molecules v.s. time in presence (left) and absence (right) of TF

Chemistry vs. π -calculus



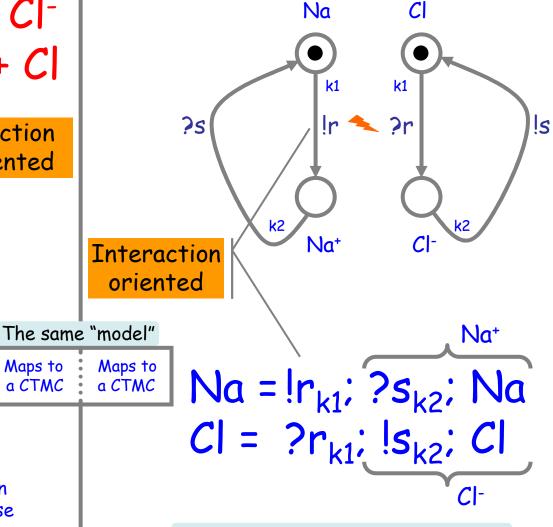
$$Na + Cl \rightarrow_{k1} Na^{+} + Cl^{-}$$

 $Na^{+} + Cl^{-} \rightarrow_{k2} Na + Cl^{-}$



This Petri-Net-like graphical representation degenerates into spaghetti diagrams: precise and dynamic, but not scalable, structured, or maintainable.

A compositional graphical representation, and the corresponding calculus.



A different process calculus (π)

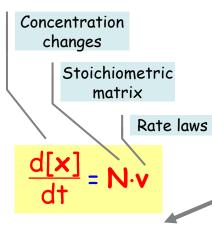
From Reactions to ODE's

$$r_1: A+B \rightarrow k_1 C+C$$

$$r_2: A+C \rightarrow k_2 D$$

$$r_3: C \rightarrow k_3 E+F$$

$$r_4: F \rightarrow k_4 B$$

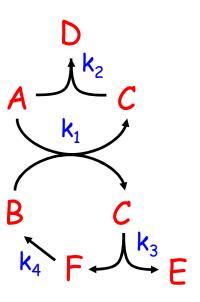


Write the coefficients by columns

reactions

| | 2 | r_1 | r ₂ | r ₃ | r ₄ |
|---|---|-------|----------------|----------------|----------------|
| | A | -1 | -1 | | |
| | В | -1 | | | 1 |
| | C | 2 | -1 | -1 | |
| _ | D | | 1 | | |
| | E | | | 1 | |
| | ۴ | | | 1 | -1 |

Stoichiometric Matrix



 $d[A]/dt = -v_1 - v_2$

$$d[B]/dt = -v_1 + v_4$$

$$d[C]/dt = 2 \cdot v_1 - v_2 - v_3$$

$$d[D]/dt = v_2$$

$$d[E]/dt = v_3$$

$$d[F]/dt = v_3 - v_4$$

Read the concentration changes from the rows

E.g.
$$d[A]/dt = -k_1 \cdot [A] \cdot [B] - k_2 \cdot [A] \cdot [C]$$

Read the rate laws from the columns

$$v_i(x,e_i,k_i)$$

| V | | | | | | | |
|-----------------------|--|--|--|--|--|--|--|
| V_1 | $k_1 \cdot [A] \cdot [B]$ | | | | | | |
| V ₂ | k ₂ ⋅[A]⋅[C] | | | | | | |
| V ₃ | k ₃ ⋅[C] | | | | | | |
| V ₄ | k ₄ ·[F] | | | | | | |

x: chemical species

[-]: concentrations

v: rate laws

k: kinetic parameters

N: stoichiometric matrix

e: catalysts (if any)

From Reactions to Processes

$$r_1: A+B \rightarrow k_1 C+C$$

 $r_2: A+C \rightarrow k_2 D$

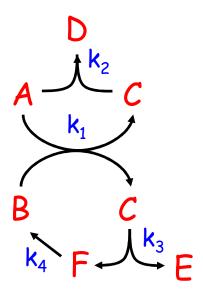
 $r_3: C \longrightarrow k_3 E+F$

 $r_4: F \rightarrow k_4 B$

For binary reactoins, first species in the column does an input and produces result, second species does an ouput, For unary reactions, species does a tau action and produces result. No ternary reactions. Write the coefficients by columns

interactions

| | 2 | r_1 | r ₂ | r ₃ | r ₄ |
|---|---|-------|----------------|----------------|----------------|
| | Α | -1 | -1 | | |
| | В | -1 | | | 1 |
| | С | 2 | -1 | -1 | |
| | D | | 1 | | |
| • | E | | | 1 | |
| | ۱ | | | 1 | -1 |



$$A = \frac{2}{2} v_1 k_1 \cdot (C|C) + \frac{2}{2} v_2 k_2 \cdot D + \frac{2}{2} a$$

$$B = |v_1k_1 + ?b|$$

$$C = \frac{1}{2} v_2 k_2 + \tau k_3 (E|F) + 2c$$

$$b = 0 + 2d$$

$$E = 0 + 2e$$

$$F = \tau k_3 \cdot B + ?f$$

Add a barb for counting and plotting

Read the process interactions from the rows

(Rate laws are implicit in stochastic semantics)

Stoichiometric Matrices Blow Up

- Can Translate Chemistry to ODE's or Processes
 - It is standard to go from chemical equations to ODE's via stoichiometric matrices.
 - It is similarly possible to go from chemical equations to processes via stoichiometric matrices.
- But there is a better way:
 - Stoichiometric matrices blow-up exponentially for biochemical systems (unlike for ordinary chemical systems) because proteins have combinatorial state and complexes are common.
 - To avoid this, we should describe biochemical systems compositionally without going through stochiometric matrices (and hence without ODE's).

Complexes: The ODE Way





domain reactions
$$C = 0$$







 $ABC = A_{D}BC$ $ABC = AB_{D}C$ $ABC = ABC_{D}$ $A_{p}BC \Rightarrow A_{p}B_{p}C$ $A_{p}BC \Rightarrow A_{p}BC_{p}$ $AB_{p}C = A_{p}B_{p}C$ $AB_{D}C = AB_{D}C_{D}$ $ABC_p = A_pBC_p$ $ABC_{p} = AB_{p}C_{p}$ $A_{\rm p}B_{\rm p}C \Rightarrow A_{\rm p}B_{\rm p}C_{\rm p}$ $A_{p}BC_{p} = A_{p}B_{p}C_{p}$ $AB_{p}C_{p} = A_{p}B_{p}C_{p}$

The matrix is very sparse, so the corresponding ODE system is not dense. But it still has 2n equations, one per species, plus conservation equations $([ABC]+[A_pBC]=constant, etc.).$

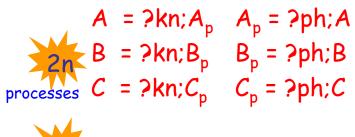
System description is exponential in the number of basic components.

Stoichiometric Matrix

| N | v ₁ | V ₂ | v ₃ | v ₄ | v ₅ | v ₆ | v ₇ | v ₈ | v ₉ | v ₁₀ | v ₁₁ | v ₁₂ | v ₁₃ | v ₁₄ | v ₁₅ | v ₁₆ | V ₁₇ | v ₁₈ | v ₁₉ | V ₂₀ | V ₂₁ | V ₂₂ | V ₂₃ | V ₂₄ |
|-------------------------|-----------------------|----------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|-----------------|-----------------|-----------------|
| ABC | | | | | | | | | | | | | | | | | | | | | | | | |
| ApBC | | | | | | | | | | | | | | | | | | | | | | | | |
| ABpC | | | | | | | | | | | | | | | | | | | | | | | | |
| АВСр | | | | | | | \ | | 2n x | 2n | (2n | -1) | | ì | | | | | | | | | | |
| АрВрС | | | | | | | | — | - ^ | | (- | , | | / | | | | | | | | | | |
| <i>А</i> рВ <i>С</i> р | | | | | | | 1 | | | | | | | | | | | | | | | | | |
| АВрСр | | | | · | | | | · | | | | | | | | | | | | | | | | |
| <i>А</i> рВр <i>С</i> р | | | | | | · | | · | | , | | | | | | | | | | | | | | |

Complexes: The Process Way

$$A \leq A_p$$
 $B \leq B_p$
domain
reactions



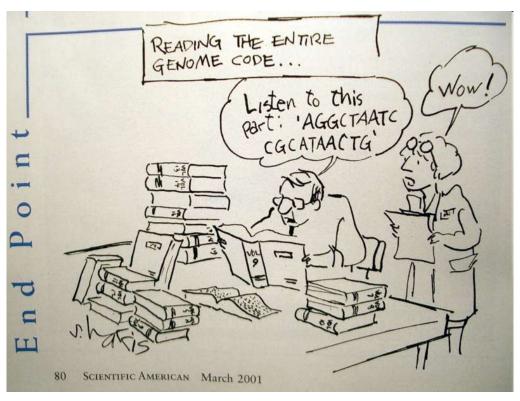


Where the local domain reactions are not independent, we can use lateral communication so that each component is aware of the relevant others.

System description is <u>linear</u> in the number of basic components.

(Its "run-time" behavior or analysis potentially blows-up just as in the previous case.)

Conclusions



Q: "The data are accumulating and the computers are humming, what we are lacking are the words, the grammar and the syntax of a new language..."

D. Bray (TIBS 22(9):325-326, 1997)

A: "The most advanced tools for computer process description seem to be also the best tools for the description of biomolecular systems."

E. Shapiro (Lecture Notes)

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```
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  Knowledge (Ph.D. Thesis).
Papers
    BioAmbients
        a stochastic calculus with compartments.
     Brane Calculi
        process calculi with computation "on" the membranes, not inside them.
     Bitonal Systems
        membrane reactions and their connections to "local" patch reactions.
    Abstract Machines of Systems Biology
        the abstract machines implemented by biochemical toolkits.
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