Artificial Biochemistry Combining Stochastic Collectives

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Trento 2006-04-03

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Stochastic Collectives



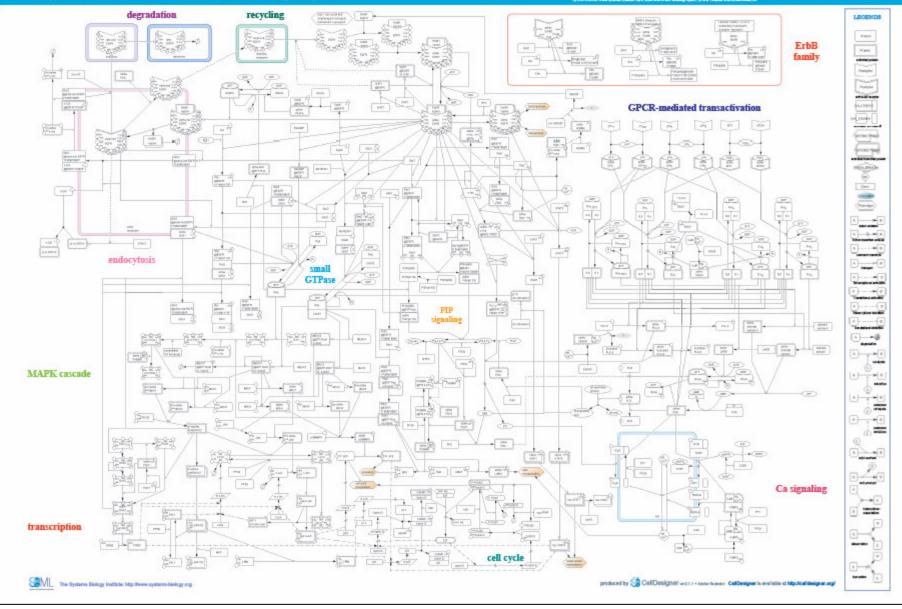
Stochastic Collectives

- "Collective":
 - A large set of interacting finite state automata:
 - Not quite language automata ("large set")
 - Not quite cellular automata ("interacting" but not on a grid)
 - Not quite process algebra ("finite state" and "collective")
 - Not quite calculus (rate of change of "automata"??)
 - Cf. "multi-agent systems" and "swarm intelligence"
- "Stochastic":
 - Interactions have *rates*
- Very much like biochemistry
 - Which is a large set of stochastically interacting molecules/proteins
 - Are proteins finite state and subject to automata-like transitions?
 - Let's say they are, at least because:
 - Much of the knowledge being accumated in Systems Biology is described as state transition diagrams [Kitano].

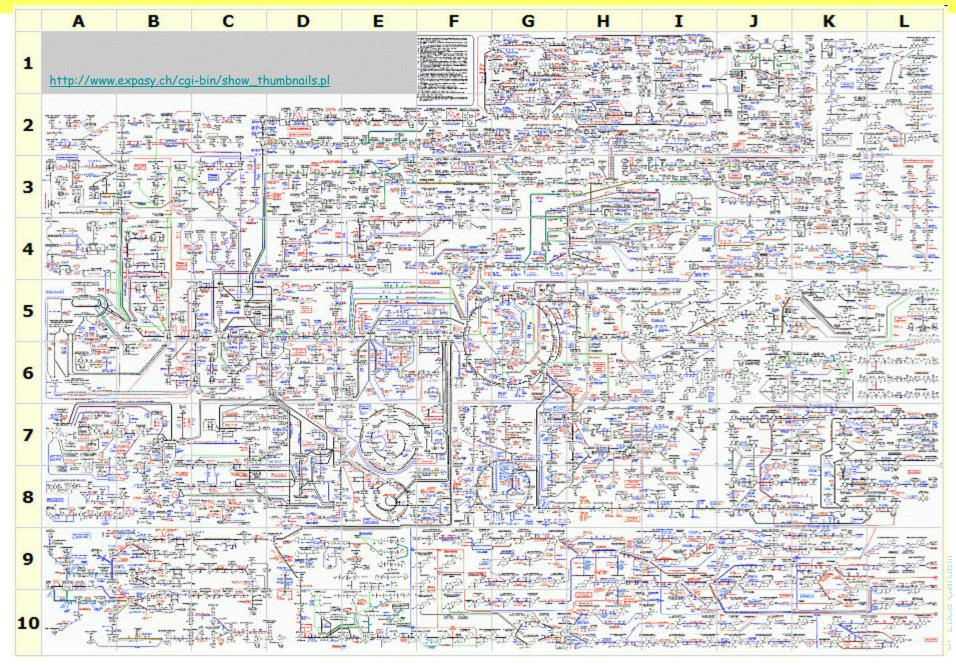
State Transitions

Epidermal Growth Factor Receptor Pathway Map

Kanae Oda (17), Yukiko Matsuoka (9, Hinseki Kitano (174) () Telekenking mila: (Createric Letteric Internet Control (Control (1998))



Even More State Transitions

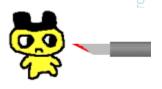


Reverse Engineering Nature

- That's what Systems Biology is up against
 - Exemplified by a technological analogy:
- Tamagotchi: a technological organism
 - Has inputs (buttons) and outputs (screen/sound)
 - It has state: happy or needy (or hungry, sick, dead...)
 - Has to be petted at a certain rate (or gets needy)
 - Each one has a slightly different behavior
- Reverse Engineering Tamagotchi
 - Running experiments that elucidate their behavior
 - Building models that explain the experiments
- Applications
 - Engineering: Can we build our own Tamagotchi? (Sadly, no longer made.)
 - Maintenance: Can we fix a broken Tamagotchi?



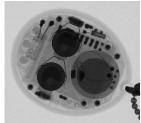
How often do I have to exercise my Tamagotchi? Every Tamagotchi is different. However we do recommend exercising at least three times a day



Understanding T.Nipponensis

- Tamagotchi Nipponensis: a stochastic interactive automata
 - 40 million sold worldwide; discontinued in 1998
 - Still found "in the wild" in Akihabara
- Traditional scientific investigations fail
 - Design-driven understanding fails
 - We cannot read the manual (Japanese)
 - What does a Tamagotchi "compute"? What is its "purpose"?
 - Why does it have 3 buttons?
 - Mechanistic understanding fails
 - Few moving parts. Removing components mostly ineffective or "lethal"
 - The "tamagotchi folding problem" (sequence of manufacturing steps) is too hard and gives little insight on function
 - Behavioral understanding fails
 - Subjecting to extreme conditions reveals little and may void warranty
 - Does not answer consistently to individual stimuli, nor to sequences of stimuli
 - There are stochastic variations between individuals
 - Ecological understanding fails
 - Difficult to observe in its native environment (kids' hands)
 - Mass produced in little-understood automated factories
 - It evolved by competing with other products in the baffling Japanese market
 - Mathematical understanding fails
 - What differential equations does it obey? (Uh?)

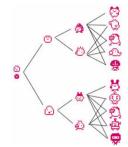




Tamagotchi X-ray



Tamagotchi Surgery http://necrobones.com/tamasurg/

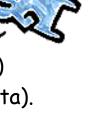


A New Approach

- "Systems Technology" of T. Nipponensis
 - High-throughput experiments (get all the information you possibly can)
 - Decode the entire software and hardware
 - Take sequences of tamagotchi screen dumps under different conditions
 - Put 300 in a basket and shake them; make statistics of final state
 - Modeling (organize all the information you got)
 - Ignore the "folding" (manufacturing) problem
 - Ignore materials (it's just something with buttons, display, and a program.)
 - Abstract until you find a conceptual model (ah-ha: it's a stochastic automata).
- Do we understand what stochastic automata collectives can do?

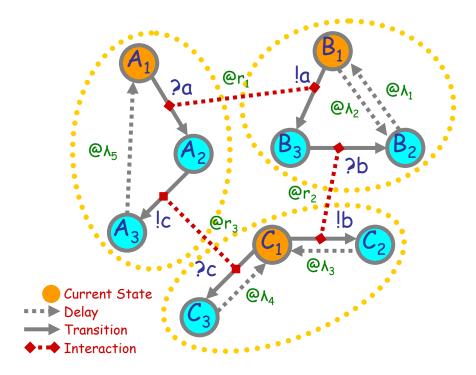


Communicating Tamagotchi



Automata Collectives

Interacting Automata



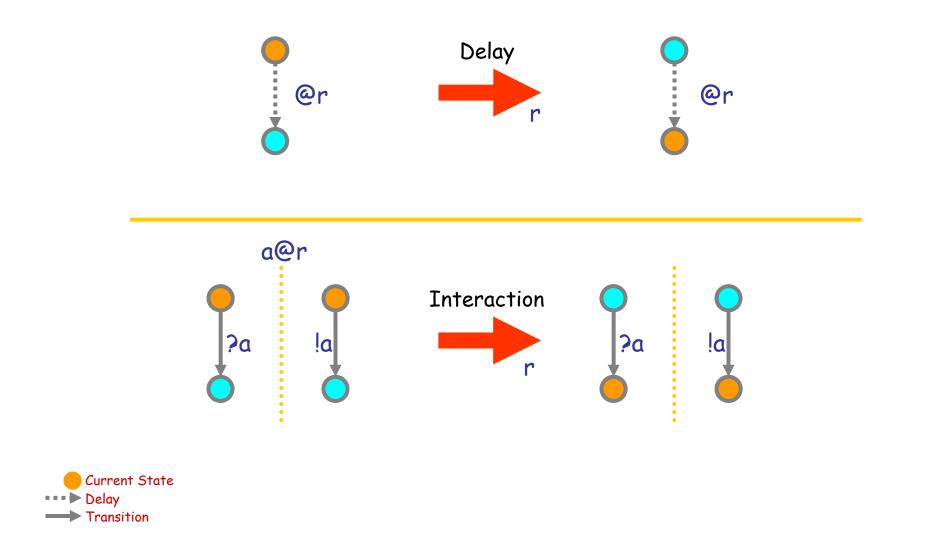
Communicating automata: a graphical FSA-like notation for "finite state restriction-free π -calculus processes". Interacting automata do not even exchange values on communication.

The stochastic version has *rates* on communications, and delays.

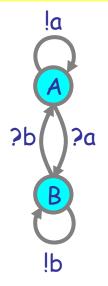
new a@r1 Communication new b@r₂ channels new c@r₃ $A_1 = ?a; A_2$ $A_2 = !c; A_3$ $A_3 = @\Lambda_5; A_1$ $B_1 = @A_2; B_2 + !a; B_3$ Automata $B_2 = @A_1; B_1$ $B_3 = ?b; B_2$ *C*₁ = !b; *C*₂ + ?c; *C*₃ $C_2 = @\Lambda_3; C_1$ $C_3 = @\Lambda_4; C_2$ The system and $A_1 | B_1 | C_1$ initial state

"Finite state" means: no composition or restriction inside recursion. Analyzable by standard Markovian techniques, by first computing the "product automata" to obtain the underlying finite Markov transition system. [Buchholz]

Interacting Automata Transition Rules

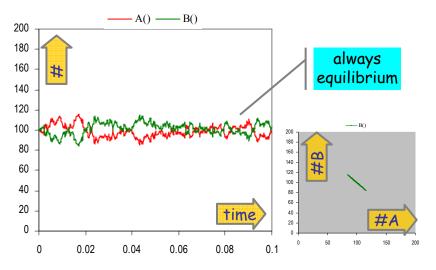


Groupies and Celebrities

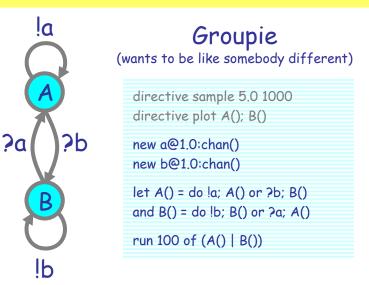




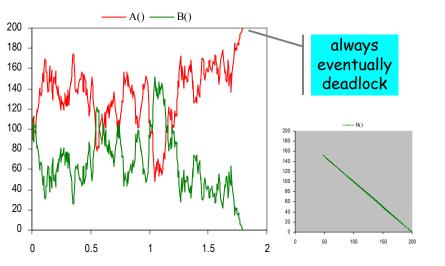
A stochastic collective of celebrities:



Stable because as soon as a A finds itself in the majority, it is more likely to find somebody in the same state, and hence change, so the majority is weakened.

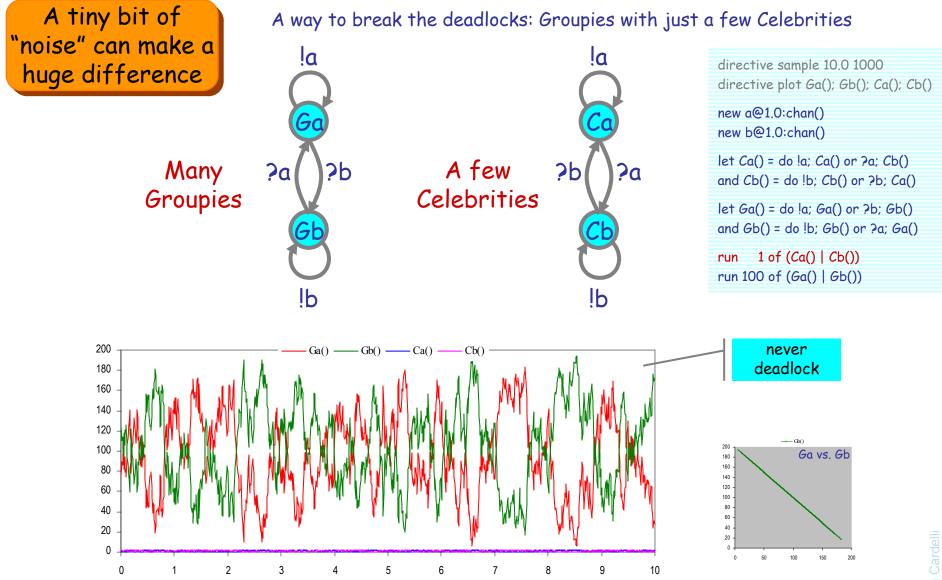


A stochastic collective of groupies:



Unstable because within an A majority, an A has difficulty finding a B to emulate, but the few B's have plenty of A's to emulate, so the majority may switch to B. Leads to deadlock when everybody is in the same state and there is nobody different to emulate.

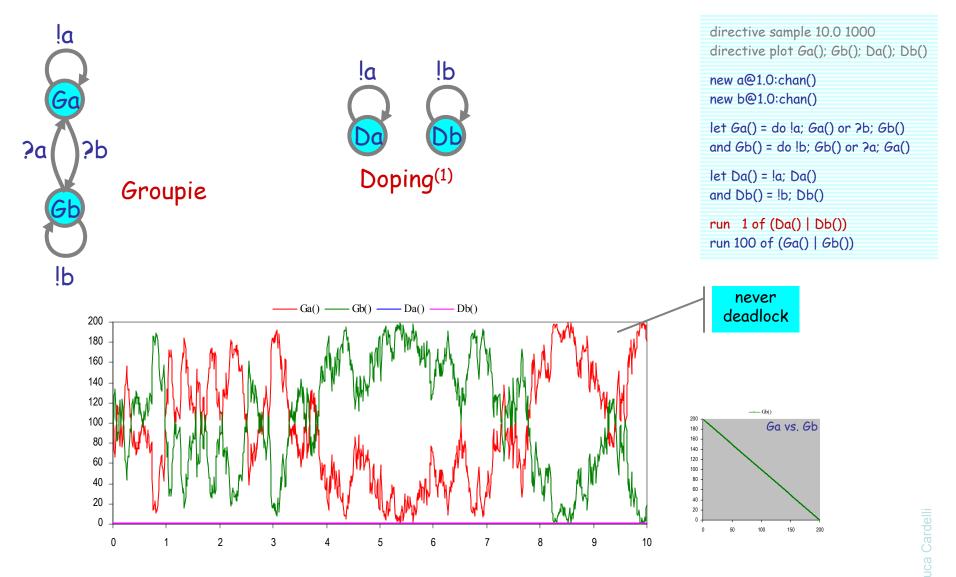
Both Together



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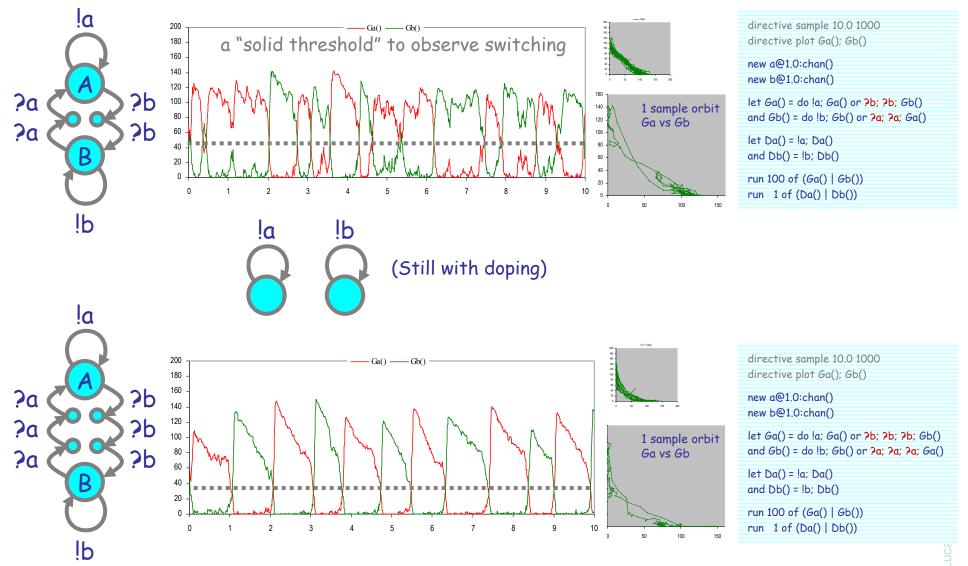
Doped Groupies

A similar way to break the deadlocks: destabilize the groupies by a small perturbation.

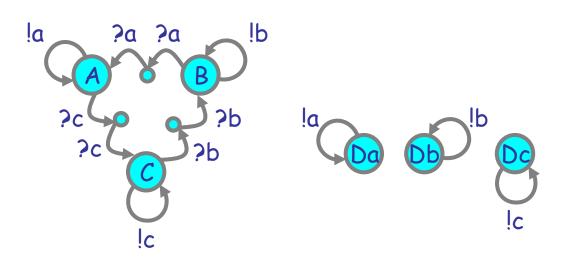


Hysteric Groupies

We can get more regular behavior from groupies if they "need more convincing", or "hysteresis" (history-dependence), to switch states.



Hysteric 3-Way Groupies



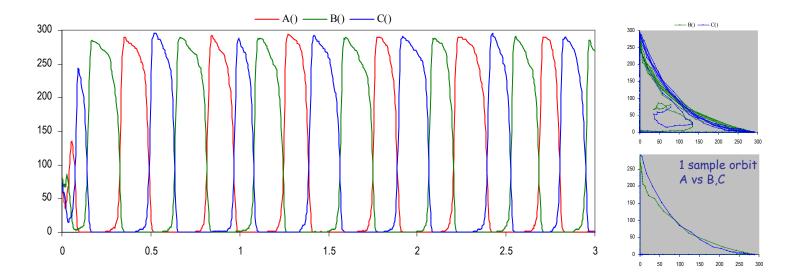
directive sample 3.0 1000 directive plot A(); B(); C()

new a@1.0:chan() new b@1.0:chan() new c@1.0:chan()

let A() = do !a; A() or ?c; ?c; C() and B() = do !b; B() or ?a; ?a; A() and C() = do !c; C() or ?b; ?b; B()

let Da() = !a; Da() and Db() = !b; Db() and Dc() = !c; Dc()

run 100 of (A() | B() | C()) run 1 of (Da() | Db() | Dc())



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The Strength of Populations

At size 2N, on a shared channel, μ is N times stronger than λ : interaction easily wins over delay.

<u>la</u>

?a

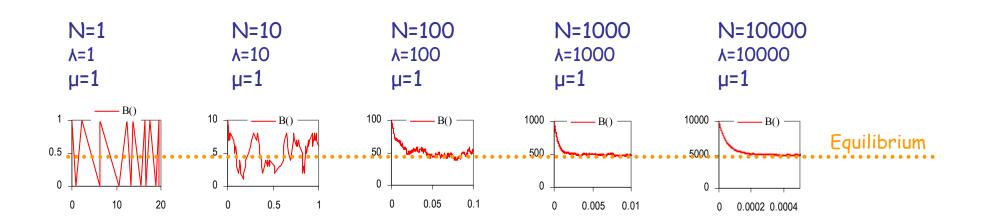
B

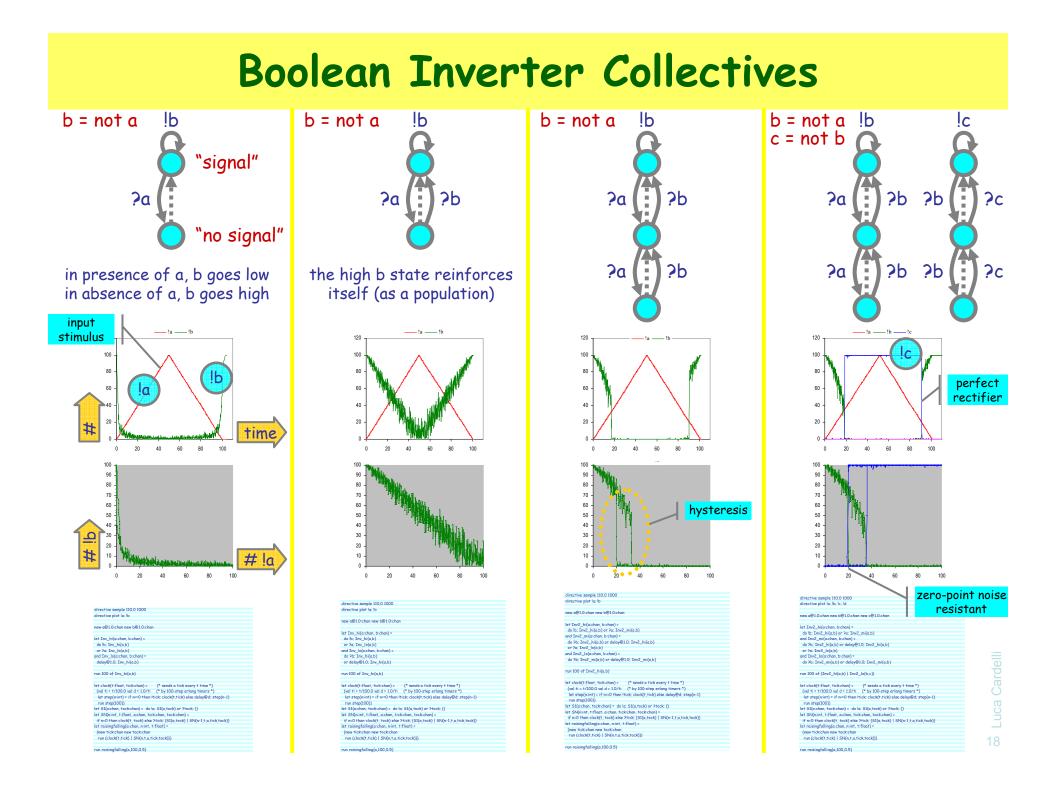
@μ

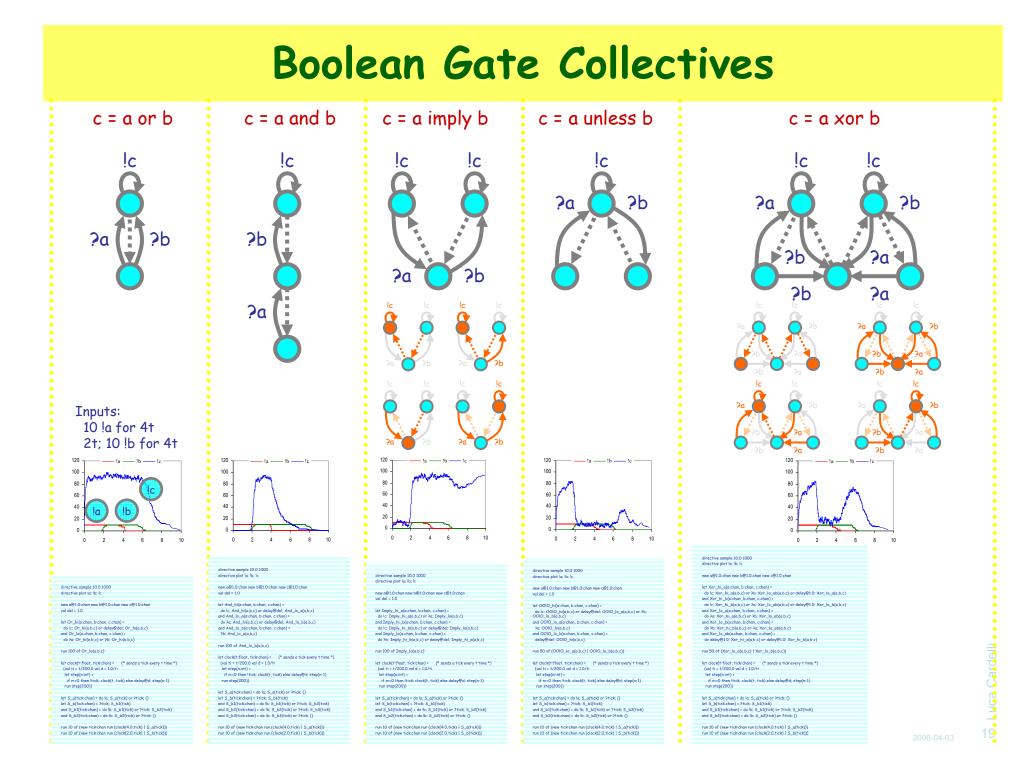
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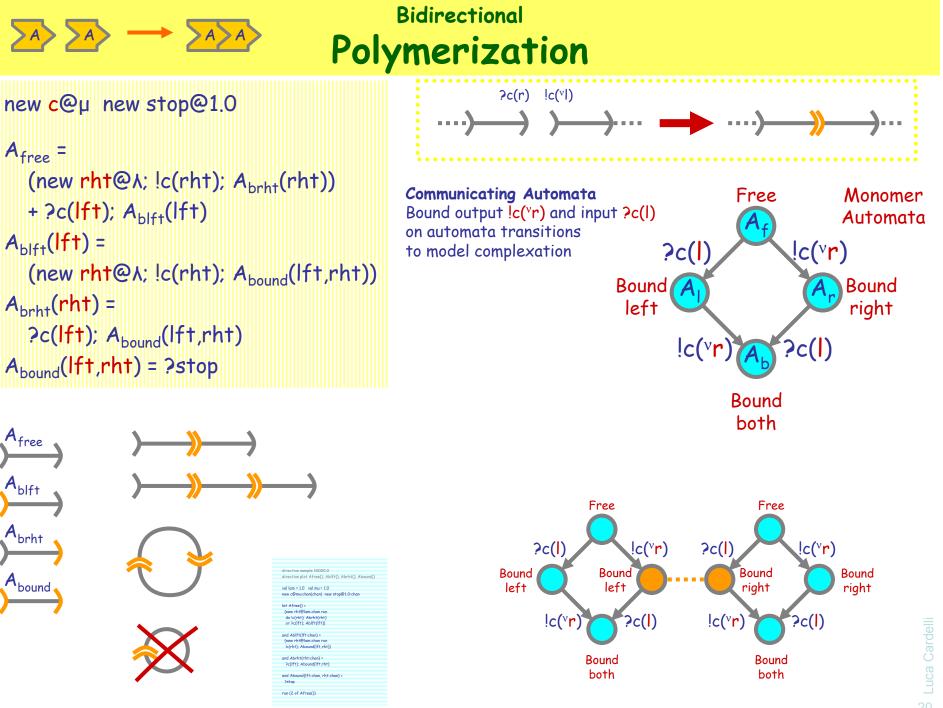
fight!

directive sample 0.01 1000 directive plot B()
val lam = 1000.0 val mu = 1.0
new a@mu:chan let A() = !a; A() and B() = ?a; C() and C() = delay@lam; B()
run 1000 of (A() B())





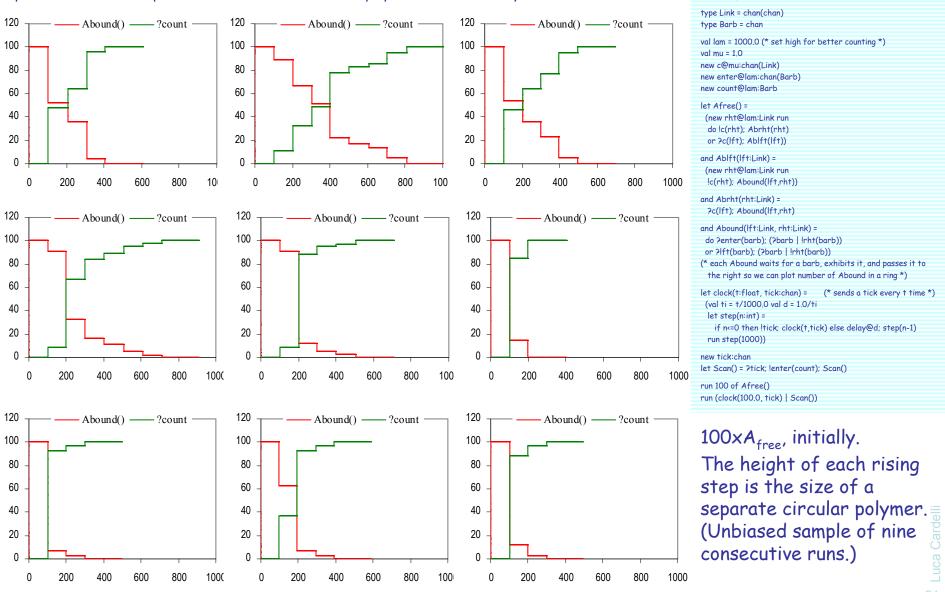




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Bidirectional Polymerization Circular Polymer Lengths

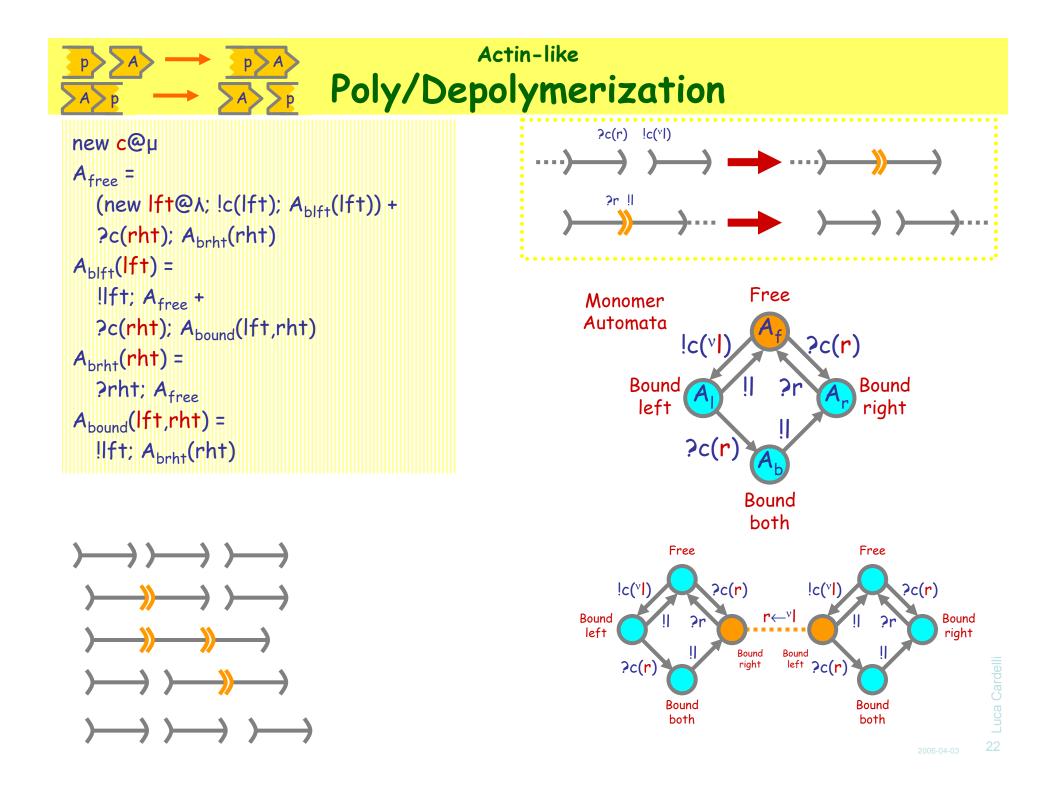
Scanning and counting the size of the circular polymers (by a cheap trick). Polymer formation is complete within 10t; then a different polymer is scanned every 100t.



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directive sample 1000.0

directive plot Abound(); ?count

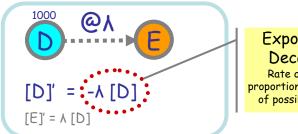


The Law of Mass Interaction

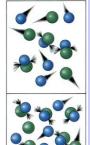
Law of Mass Interaction

The speed of interaction[†] is proportional to the number of *possible interactions*.

Decay



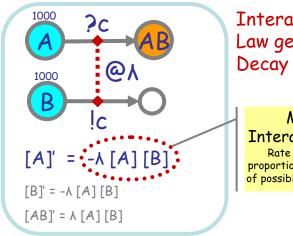
Exponential Decay law Rate of change proportional to number of possible decays.



Chemical Law of Mass Action http://en.wikipedia.org/wiki/Chemical_kinetics The **speed** of a chemical reaction is proportional to the **activity** of the reacting substances.

(Activity = concentration, for wellstirred aqueous medium) (Concentration = number of moles per liter of solution) (Mole = 6.022141×10²³ particles)

Mass interaction



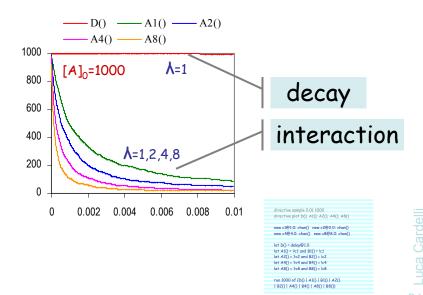
Interaction Law generalizes Decay Law

Mass Interaction law Rate of change proportional to number of possible interactions

[†] speed of interaction (formally definable)

= number of interactions over time

not proportional to the number of interacting processes! [P] is the number of processes P (this is informal; it is only meaningful for a set of processes offering a given action, but a set of such processes can be counted and plotted)



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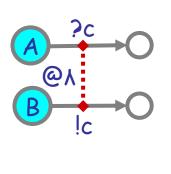
Activity and Speed

stochastic algebras disagree!

The speed of interaction is proportional to the number of possible interactions.

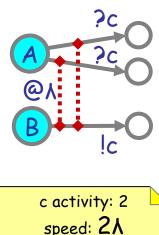
The *activity* (= "concentration") on a channel is the number of *possible interactions* on that channel.

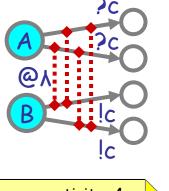
The *speed of interaction* on a channel, is the activity multiplied by the base rate of the channel.



c activity: 1

speed: $\mathbf{\lambda}$

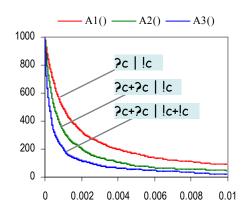




c activity: 4 speed: **4**1

The mass interaction law [Buchholz] [Priami-Regev-Shapiro-Silverman] is compatible with chemistry [Gillespie] and *incompatible* with any other stochastic algebra in the literature! (including [Priami]; see [Hermanns])

Other algebras assign rates to actions, not channels, with speed laws: $2\lambda^*2\lambda = 4\lambda^2$ max $(2\lambda,2\lambda) = 2\lambda$ [Goetz] min $(2\lambda,2\lambda) = 2\lambda$ [Priami] $1/(1/(2\lambda)+1/(2\lambda)) = \lambda$ [PEPA] $2\lambda^*1 = 2\lambda$ (passive inputs) directive sample 0.01 10000 directive plot A1(): A2(): A3() new c1@1.0:chan new c2@1.0:chan new c3@1.0:chan let A1() = ?c1 and B1() = !c1 let A2() = do ?c2 or ?c2 and B2() = !c2 let A3() = do ?c3 or ?c3 and B3() = do !c3 or !c3 run 1000 of (A1() | B1() | A2() | B2() | A3() | B3())



Possible Interactions

The speed of interaction is proportional to the number of possible interactions. But a process cannot interact with itself.

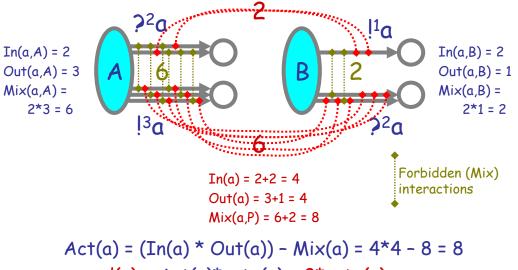
Assume each process P is in restrictedsum-normal-form. For each channel x:

In(x,P) = Num of active ?x in P Out(x,P) = Num of active !x in P Mix(x,P) = In(x,P)*Out(x,P) #interactions that cannot happenin a given summation P In(x) = Sum P of In(x,P) Out(x) = Sum P of Out(x,P) Mix(x) = Sum P of Mix(x,P) total #interactions that cannot happen

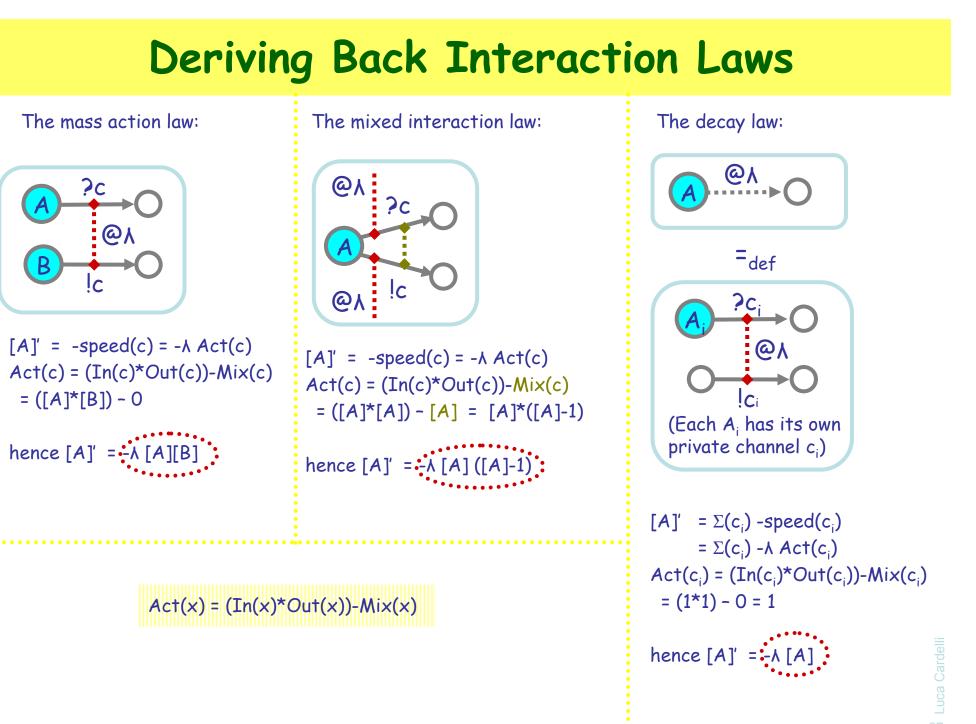
The global Activity on channel x:

Act(x) = (In(x)*Out(x))-Mix(x) total cross product of inputs and outputs minus total #interactions that cannot happen The global speed of interaction on a channel x:

speed(x) = Act(x)*rate(x)



speed(a) = Act(a)*rate(a) = 8*rate(a)



Conclusions

Conclusions

- Stochastic Collectives
 - Complex global behavior from simple components
 - Emergence of collective functionality from "non-functional" components
 - (C.f. "swarm intelligence": simple global behavior from complex components)
- Artificial Biochemistry
 - Stochastic collectives with Law of Mass Interaction kinetics
 - Connections to classical Markov theory, chemical Master Equation, and Rate Equation
- The agent/automata/process point of view
 - "Individuals" that transition between states
 (vs. transmutation between "unrelated" chemical species)
 - More appropriate for Systems Biology
 - Stochastic π -calculus (SPiM) for investigating stochastic collectives
 - \bullet Restriction+Communication \Rightarrow Polymerization: FSA that "stick together"